

Reliable Multicast Transport  
Internet Draft

E. Stauffer  
Broadcom  
B. Shen  
Broadcom  
S. Chakraborty  
Broadcom  
D. Tujkovic  
Broadcom  
J. Huang  
Broadcom  
S. Shet  
Broadcom  
K. Rath  
Broadcom

Intended status: Standards Track  
Expires: March 2014

September 26, 2013

**Supercharged Codes**  
**draft-stauffer-rmt-bb-fec-supercharged-03.txt**

Status of this Memo

This Internet-Draft is submitted in full conformance with the provisions of [BCP 78](#) and [BCP 79](#).

Internet-Drafts are working documents of the Internet Engineering Task Force (IETF), its areas, and its working groups. Note that other groups may also distribute working documents as Internet-Drafts.

Internet-Drafts are draft documents valid for a maximum of six months and may be updated, replaced, or obsoleted by other documents at any time. It is inappropriate to use Internet-Drafts as reference material or to cite them other than as "work in progress."

The list of current Internet-Drafts can be accessed at <http://www.ietf.org/ietf/1id-abstracts.txt>

The list of Internet-Draft Shadow Directories can be accessed at <http://www.ietf.org/shadow.html>

This Internet-Draft will expire on March 26, 2014.

## Copyright Notice

Copyright (c) 2012 IETF Trust and the persons identified as the document authors. All rights reserved.

This document is subject to [BCP 78](http://trustee.ietf.org/license-info) and the IETF Trust's Legal Provisions Relating to IETF Documents (<http://trustee.ietf.org/license-info>) in effect on the date of publication of this document. Please review these documents carefully, as they describe your rights and restrictions with respect to this document. Code Components extracted from this document must include Simplified BSD License text as described in Section 4.e of the Trust Legal Provisions and are provided without warranty as described in the Simplified BSD License.

## Abstract

This document describes a fully-specified FEC scheme for the Supercharged forward error correction code. Supercharged codes are designed for use on the erasure channel. Coding for the erasure channel commonly arises for data transmission over the internet, where lower layers either successfully deliver packets or fail to deliver them. Coding is required to insure that data is not lost, even if packets are lost at the lower layers. Error free reception is important for multimedia applications, such as streaming, where it may not be possible to correct an error in time by any other means. Coding insures that lost packets can be recovered.

## Table of Contents

<a href="#">1. Introduction.....</a>	<a href="#">3</a>
<a href="#">2. Supercharged Code.....</a>	<a href="#">3</a>
<a href="#">2.1.1. Definitions.....</a>	<a href="#">3</a>
<a href="#">2.2. Overview.....</a>	<a href="#">4</a>
<a href="#">2.3. Matrix Representation.....</a>	<a href="#">5</a>
<a href="#">2.4. Systematic Encoding.....</a>	<a href="#">6</a>
<a href="#">2.5. Erasure Channel.....</a>	<a href="#">6</a>
<a href="#">2.6. Decoding.....</a>	<a href="#">7</a>
<a href="#">2.7. Matrix P Construction.....</a>	<a href="#">7</a>
<a href="#">2.7.1. Function Prototypes.....</a>	<a href="#">7</a>
<a href="#">2.7.2. Parallel Filter Code T Construction.....</a>	<a href="#">8</a>
<a href="#">2.7.3. Repetition Code R Construction.....</a>	<a href="#">10</a>
<a href="#">2.7.4. Block Code B_1 Construction.....</a>	<a href="#">11</a>
<a href="#">2.7.5. Block Code B_2 and B_3 Construction.....</a>	<a href="#">11</a>
<a href="#">2.7.6. SC_Parameters.....</a>	<a href="#">13</a>
<a href="#">2.7.7. K Table.....</a>	<a href="#">13</a>



<a href="#">2.7.8</a>	Random Number Generator.....	<a href="#">18</a>
<a href="#">2.7.9</a>	Random Permutation.....	<a href="#">22</a>
<a href="#">2.7.10</a>	RS Generator.....	<a href="#">23</a>
<a href="#">2.7.11</a>	RS Code.....	<a href="#">24</a>
<a href="#">2.7.12</a>	SC_Filter_Data.....	<a href="#">24</a>
<a href="#">2.7.13</a>	GF(256) Operations.....	<a href="#">25</a>
<a href="#">3</a>	FEC Packets.....	<a href="#">25</a>
<a href="#">3.1</a>	Segmentation.....	<a href="#">25</a>
<a href="#">3.1.1</a>	Transmit Blocks.....	<a href="#">25</a>
<a href="#">3.1.2</a>	Working Blocks.....	<a href="#">26</a>
<a href="#">3.1.3</a>	Padding.....	<a href="#">26</a>
<a href="#">4</a>	Parameter Selection.....	<a href="#">26</a>
<a href="#">5</a>	Control Messages.....	<a href="#">27</a>
<a href="#">5.1</a>	FEC Payload ID.....	<a href="#">27</a>
<a href="#">5.2</a>	FEC Object Transmission Information.....	<a href="#">27</a>
<a href="#">5.2.1</a>	FEC Encoding ID.....	<a href="#">27</a>
<a href="#">5.2.2</a>	Common.....	<a href="#">27</a>
<a href="#">5.2.3</a>	Scheme Specific.....	<a href="#">28</a>
<a href="#">6</a>	Conventions used in this document.....	<a href="#">29</a>
<a href="#">7</a>	Security Considerations.....	<a href="#">29</a>
<a href="#">8</a>	IANA Considerations.....	<a href="#">29</a>
<a href="#">9</a>	References.....	<a href="#">29</a>
<a href="#">9.1</a>	Normative References.....	<a href="#">29</a>
<a href="#">9.2</a>	Informative References.....	<a href="#">29</a>
<a href="#">10</a>	Acknowledgments.....	<a href="#">30</a>

## [1](#). Introduction

This document describes a fully-specified FEC scheme for the Supercharged forward error correction code. The Supercharged code is designed for the erasure channel with performance very close to the ideal Maximum Distance Separable(MDS) code and with very low complexity. [Section 2](#) describes the architecture of the code and defines the generator matrices used by the code. [Section 3](#) describes how to construct FEC packets. [Section 4](#) discusses code parameter selection for a particular usage context. [Section 5](#) defines the protocol information elements. [Section 6](#) considers security. [Section 7](#) considers IANA.

## [2](#). Supercharged Code

### [2.1.1](#). Definitions

ceil(a): rounds a to the nearest integer towards infinity

floor(a): rounds a to the nearest integer towards minus infinity



`min(a,b)`: returns the minimum of a and b

`max(a,b)`: returns the maximum of a and b

`a % b`: is a modulo b

`a + b`: is a plus b

`a * b`: is a multiplied by b.

`a ^ b`: the bitwise XOR of a and b

`a ^^ b`: raises a to the b power

`I_a`: the a x a identity matrix

`zeros(a,b)`: the a x b zero matrix

## 2.2. Overview

Figure 1 shows a general block diagram of the supercharged code. It consists of a network of codes including block codes, repetition codes, and parallel filter codes. Block code 1 consists of a Vandermonde matrix in GF(256), a non-systematic Reed Solomon code. Block code 2 and 3 consist of binary block codes.

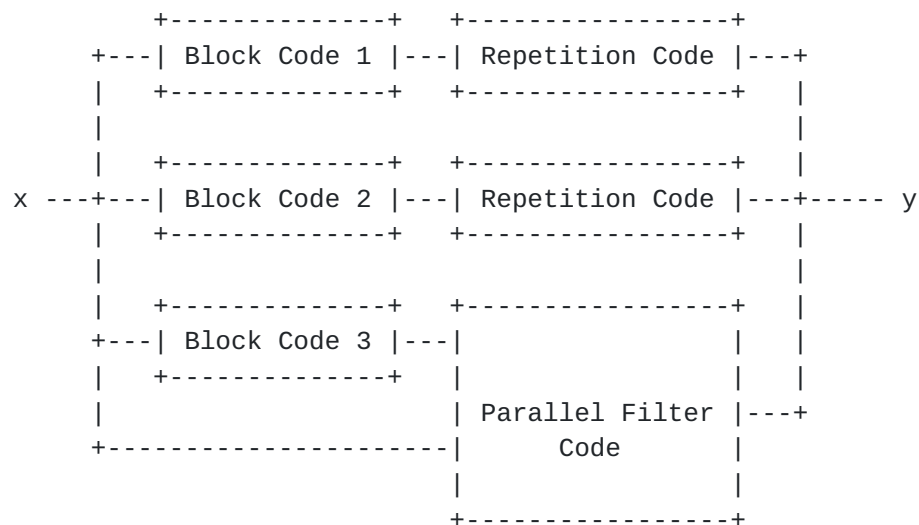


Figure 1 Block Diagram of the SC Code



The parallel filter code of Figure 1 is detailed in Figure 2. It consists of interleavers, tailbiting FIR filters, and a multiplexer to select the output of the filters.

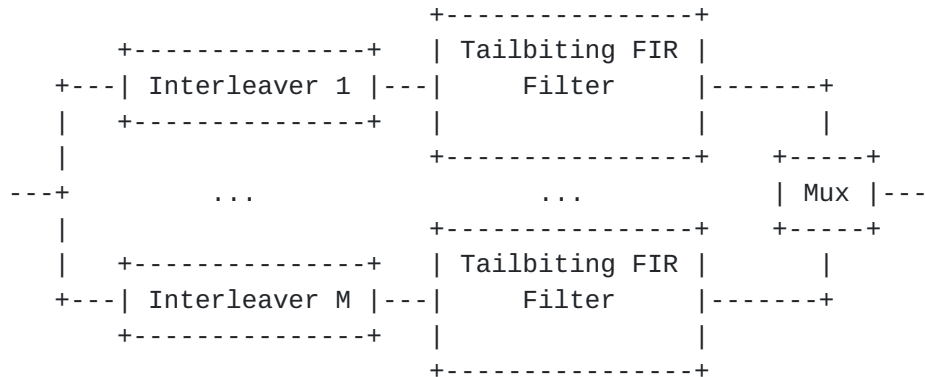


Figure 2 An example parallel filter code showing individual data interleavers and tailbiting FIR filters as coding components.

An example of one of the tailbiting FIR filters is illustrated in Figure 3, where the state of the filter is initialized with the final state to make it tailbiting.

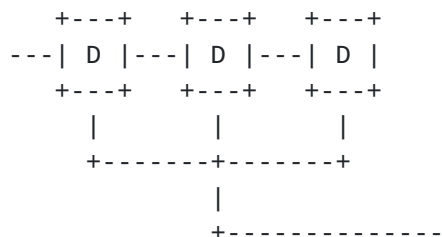


Figure 3 An example 3 tap FIR filter that can be used for the tailbiting FIR filter coding component. An XOR operation is applied at the output of the delay elements to produce the final output.

Optionally, if the number of transmit symbols  $N$  is signaled to be limited such that  $N \leq 256$ , then the code can achieve ideal performance by utilizing a Reed Solomon code.

### 2.3. Matrix Representation

Since supercharged codes are linear, an output codeword can be expressed as a matrix multiplied by an input vector. Given  $K \times 1$



encoding state vector  $x$ , consisting of binary transmit symbols, the output  $N \times 1$  codeword,  $y$ , can be written as

$$y = (T*[I_K; B_3] + R_1*B_1 + R_2*B_2)*x \quad (1)$$

where  $T$  is the  $N \times (K + \text{Num\_B\_3})$  generator matrix for the FIR structure,  $B_1$  is the  $\text{Num\_V\_RS} \times K$  generator matrix for the first block code,  $B_2$  is the  $\text{Num\_B\_2} \times K$  generator for the second block code,  $B_3$  is the  $\text{Num\_B\_3} \times K$  generator matrix of the third block code, and  $R_1$  is a  $N \times \text{Num\_V\_RS}$  stack and  $R_2$  is a  $N \times \text{Num\_B\_2}$  stack of identity matrices which facilitates repetition. For example, matrix  $R_1$  would consist of  $\text{floor}(N/\text{Num\_V\_RS})$  copies of the identity matrix stacked vertically, with a fractional identity matrix below consisting of  $N \bmod \text{Num\_V\_RS}$  rows. The "+" operator indicates the bitwise XOR operation. For convenience, denote the generator matrix  $P = (T*[I_K; B_3] + R_1*B_1 + R_2*B_2)$ , such that  $y = Px$ .

#### 2.4. Systematic Encoding

Supercharged codes are not inherently systematic codes. Non-systematic codes are commonly transformed into an effective systematic code by pre-processing the input data before using it as the input to the encoder,  $y = Px$ . The encoder input is calculated by decoding the desired input data and running the decoder to determine the encoder input vector  $x$ . Let matrix  $P_{\text{enc}}$  be the  $K \times K$  generating matrix corresponding to the first  $K$  elements of  $y$ , the encoder input  $x$  can be computed using the following

$$x = P_{\text{enc}}^{-1} * d.$$

Now,  $x$  can be used to encode using equation (1) to generate  $y$ . The first  $K$  elements of vector  $y$  will be equal to  $d$ .

#### 2.5. Erasure Channel

After encoding, the  $N$  transmit symbols of codeword vector  $y$  are transmitted on the channel. Some of these transmit symbols are erased by the channel. Suppose that the  $N \times r$  matrix  $E$  represents the erasure pattern of the channel in that it selects out the  $r$  received transmit symbols  $y_r$  from the transmitted symbols  $y$ . If the  $i$ th received symbol is the  $j$ th transmit symbol, then  $E(i,j)=1$ . This results in

$$y_r = E*y.$$

At the decoder, the effective generator matrix at the receiver is  $P_r = E*P$ .



## 2.6. Decoding

Decoding is the process of determining  $x$  given  $y_r$  and  $P_r$ . Decoding can be implemented in several different ways, but each are equivalent to solving the least squares problem  $x = (P_r^{AT}P_r)^{-1} * P_r^{AT} * y_r$ . Modern sparse matrix factorization techniques can take advantage of the sparse structure imposed by the parallel filter structure if (1) is rewritten in the following equivalent form

$$z = Gw, \quad (2)$$

with augmented generator matrix  $G$  defined as

$$G = [ [B_3; B_2; B_1] \ I_L; \ T \ R_2 \ R_1 ]$$

and where the augmented output vector  $z=[zeros(L,1); y]$ , the augmented input vector  $w=[x; B_3*x; B_2*x; B_1*x]$ , and where  $L=Num\_V\_RS+Num\_B\_2+Num\_B\_3$ . The bottom  $L$  elements of vector  $w$  contain the outputs, before repetition, of the block codes. These  $L$  values are appended to vector  $x$  to form the augmented input vector  $w$ . The first  $L$  rows of  $G$  implement the block code and XOR the block code output with itself to generate the  $L$  zeros at the top of the  $z$  vector. The subsequent  $N$  rows of  $G$  implement the FIR structure and XOR the output with the output of the block codes.

This problem can be efficiently solved using direct sparse matrix factorization techniques described in [3-8]. It is RECOMMENDED that the Dulmage-Mendelsohn based solver in chapter 8 of [5] be used with addition, multiplication, and division updated to support a finite field. This algorithm utilizes pivoting based on node degrees in the equivalent graph to minimize fill-in. The solution is completed by performing forward and backward substitutions. Iterative solvers are also possible.

Once the encoder state vector  $x$ , or equivalently the augmented encoder state vector  $w$ , has been determined, the task remains to determine the data vector  $d$ . For any elements of  $d$  that are missing, then can be recovered by using appropriate rows of (1) or (2).

## 2.7. Matrix P Construction

### 2.7.1. Function Prototypes

The following functions are utilized to construction the Supercharged code.



```
[K_eff, Num_V_RS, Num_B_2, Num_B_3] = SC_Parameters(K, N)

K_eff=SC_K_table(K)

b=RNG(a)

a=RNG_2(a,b)

[permutation,the_seed]= Generate_Permutation(a,b)

G_V_RS = RS_gen(K,N)

[filter_data, filter_N]=SC_filter_data(z)

b=GF_exp(a)

C=GF_Multiply(A,B)
```

#### **2.7.2. Parallel Filter Code T Construction**

The parallel filter code matrix T can be generated using the following pseudo code. The code generates multiple random interleavers and selects which output of which interleaver depending on the SID, where the SID is defined in [section 3](#). Note that at the receiver, only filter outputs corresponding to the received SID's are required. The following code generates filter outputs for SIDs 0 to N-1. Determination of the filter output is a function of the SID only, not any other filter output, making it simple to generate only the filter outputs needed at encoding or decoding. The Generate\_Permutation function is defined in [section 2.7.9](#), the SC\_filter\_data function is defined in [section 2.7.12](#), and the RNG function is defined in [section 2.7.8](#).

```
seed1 = 758492

seed2 = ( (K_eff*874) ^ (seed1) )

seed3 = 23091

base_permutation = Generate_Permutation(K_eff+Num_B_3,seed2)

filter_data = SC_filter_data(K_eff+Num_B_3)
```

```
T = zeros(N,K_eff+NUM_B_3)

for SID=0:N-1

    %Determine which filter to select

    rn1 = min( RNG(15*(SID+1)+2*seed3) , 2^^32 )

    index = 0

    while(rn1>(filter_data[index]))

        index = index+1

    end

    tdeg=index+1

    %Determine which interleaver to select

    rn2 = min( RNG(2*K_eff+3*(SID+1)) , 2^^32 )

    interleaver_number = ( (rn2) % (K_eff+Num_B_3) )

    %Determine which part of the interleaver to select

    rn3 = min( RNG(98573+2*(SID+1)+rn1) , 2^^32 )

    interleaver_part = ((rn3) % (K_eff+Num_B_3))

    for tap_loop=0:tdeg

        filter_tap = (tap_loop+interleaver_part) %
(K_eff+Num_B_3)

        tap_location = (base_permutation[filter_tap] +
base_permutation[interleaver_number]) % (K_eff+Num_B_3)

        T[Num_V_RS+Num_B_2+Num_B_3+SID,tap_location] = 1

    end

end
```

```
        end
    end
```

### **2.7.3. Repetition Code R Construction**

The repetition code matrix  $R_1$  and  $R_2$  can be constructed via the following pseudo code. Note that at the receiver, only filter outputs corresponding to the received SID's are required. The following code generates filter outputs for SIDs 0 to N-1 for  $R_1$ .

```
R_1 = zeros(N, Num_V_RS)

for SID = 0:N-1

    for k = 0:Num_V_RS-1

        if( ((SID-k) % (Num_V_RS)) == 0 )

            R_1[SID,k] = 1

        end

    end

end

end
```

The following code generates filter outputs for SIDs 0 to N-1 for  $R_2$ .

```
R_2 = zeros(N, Num_B_2)

for SID = 0:N-1

    for k = 0: Num_B_2-1

        if( ((SID-k) % (Num_B_2)) == 0 )

            R_2[SID,k] = 1

        end

    end

end
```

```
end
```

#### **2.7.4. Block Code B\_1 Construction**

The Vandermonde matrix of block code B\_1 can be constructed via the following pseudo code. The GF\_exp function is defined in [section 2.7.13](#).

```
B_1 = zeros(Num_V_RS,K_eff)

for i = 0:Num_V_RS-1

    for k = 0:K_eff-1

        B_1[i+1,k+1] = GF_exp( ((i+1)*k) % (2^8-1) )

    end

end
```

#### **2.7.5. Block Code B\_2 and B\_3 Construction**

The block code B\_2 and B\_3 can be constructed jointly via the following pseudo code, where B\_23=[B\_3; B\_2].

```
B_23 = zeros(Num_B_2 + Num_B_3,K_eff)

for i = 0:K_eff-1

    for k = 0: Num_B_2 + Num_B_3 - 1

        if( ( (k-i) % (Num_B_2 + Num_B_3) ) == 0)

            B_23[k,i] = 1

        end

    end

end
```

```
end

m=1

for i = 0:K_eff-1

    for k = 0: Num_B_2 + Num_B_3 - 1

        if( ( (k-i-2*floor(m/( Num_B_2 + Num_B_3))) % (Num_B_2 +
Num_B_3) ) == 0)

            B_23[k,i] = 1

        end

        m = m+1

    end

end

end

m=2

for i = 0:K_eff-1

    for k = 0: Num_B_2 + Num_B_3 - 1

        if( ( (k-i-3*floor(m/( Num_B_2 + Num_B_3))) % (Num_B_2 +
Num_B_3) ) == 0)

            B_23[k,i] = 1

        end

        m = m+1

    end

end
```

end

#### **2.7.6. SC\_Parameters**

The following pseudo code determines a set of parameters needed for matrix construction. The SC\_K\_table is defined in [section 2.7.7](#).

```
function [K_eff, Num_V_RS, Num_B_2, Num_B_3] = SC_Parameters(K, N)

    K_eff = SC_K_table(K)

    Num_V_RS = 11 + floor(K_eff/10000)

    Num_B = floor(K_eff^(0.62)) + 3

    if( K_eff >= 17376 )

        Num_B = ceil( K_eff*0.0152 + 163 )

    end

    Num_B_3 = ceil(0.75*( Num_B ))

    Num_B_2 = Num_B - Num_B_3
```

#### **2.7.7. K Table**

The function `K_eff=SC_K_table(K)` is implemented based on the following table, by returning the smallest `K_eff` such that `K_eff>=K`.

```
10,11,12,13,14,15,16,17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,32,
33,34,35,36,37,38,39,40,41,42,43,44,45,46,47,48,49,50,51,52,53,54,55,
56,57,58,59,60,61,62,63,64,65,66,67,69,70,71,72,73,74,75,76,77,78,79,
80,81,82,83,84,85,86,87,88,89,90,91,92,93,94,95,96,97,98,99,100,101,1
02,103,104,105,106,107,108,109,110,111,112,113,114,115,116,117,118,11
9,120,121,122,123,124,125,126,127,128,129,130,131,133,134,135,136,137
,138,139,140,141,142,143,144,145,146,147,148,149,150,151,152,153,154,
155,156,157,158,159,160,161,162,163,164,165,166,167,168,169,170,171,1
```

72, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 314, 315, 316, 320, 321, 324, 328, 329, 335, 337, 338, 340, 341, 344, 347, 349, 352, 355, 357, 358, 360, 362, 364, 366, 368, 372, 377, 380, 381, 382, 384, 385, 388, 389, 393, 394, 395, 397, 399, 405, 408, 409, 410, 411, 416, 418, 424, 426, 428, 431, 432, 434, 438, 443, 447, 448, 451, 452, 453, 457, 460, 465, 466, 467, 469, 473, 476, 477, 478, 482, 483, 484, 485, 486, 490, 491, 492, 493, 494, 496, 497, 498, 500, 501, 502, 503, 504, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 524, 526, 527, 528, 529, 530, 532, 533, 534, 535, 536, 537, 539, 541, 542, 543, 545, 546, 549, 551, 552, 553, 554, 555, 557, 558, 559, 561, 562, 563, 564, 566, 569, 571, 572, 573, 574, 576, 577, 578, 579, 580, 582, 583, 585, 586, 587, 588, 589, 590, 592, 593, 594, 597, 598, 599, 600, 602, 603, 606, 607, 608, 609, 610, 612, 614, 615, 616, 617, 619, 620, 622, 625, 626, 627, 628, 629, 630, 631, 633, 635, 636, 637, 638, 640, 643, 645, 648, 650, 652, 653, 654, 655, 656, 659, 660, 661, 662, 664, 666, 667, 668, 669, 672, 673, 674, 675, 677, 687, 688, 691, 692, 693, 694, 695, 696, 698, 699, 700, 701, 703, 710, 711, 712, 715, 716, 717, 718, 726, 727, 730, 731, 734, 736, 737, 741, 744, 747, 748, 751, 752, 753, 757, 759, 760, 762, 764, 766, 769, 771, 772, 773, 774, 775, 777, 778, 779, 786, 788, 790, 792, 793, 794, 795, 797, 798, 799, 800, 801, 802, 804, 805, 810, 811, 812, 813, 815, 820, 821, 822, 823, 825, 827, 829, 830, 831, 834, 835, 837, 838, 839, 840, 843, 844, 845, 846, 848, 849, 851, 852, 853, 854, 857, 858, 860, 863, 864, 866, 868, 869, 870, 875, 877, 879, 883, 886, 887, 890, 891, 894, 897, 898, 899, 900, 902, 903, 904, 905, 906, 907, 909, 912, 913, 914, 917, 922, 926, 927, 928, 931, 934, 938, 940, 942, 944, 945, 948, 950, 953, 954, 960, 961, 963, 967, 968, 970, 971, 972, 974, 977, 979, 980, 981, 985, 987, 989, 990, 995, 996, 1000, 1002, 1003, 1005, 1006, 1007, 1009, 1010, 1015, 1020, 1021, 1022, 1024, 1025, 1027, 1032, 1033, 1034, 1035, 1037, 1041, 1042, 1043, 1046, 1048, 1050, 1051, 1054, 1056, 1057, 1059, 1060, 1062, 1065, 1069, 1070, 1071, 1074, 1076, 1078, 1079, 1082, 1083, 1085, 1086, 1087, 1088, 1089, 1095, 1098, 1099, 1106, 1110, 1111, 1118, 1120, 1123, 1124, 1125, 1131, 1132, 1134, 1136, 1139, 1140, 1142, 1144, 1150, 1152, 1157, 1161, 1162, 1165, 1169, 1173, 1175, 1176, 1179, 1181, 1182, 1183, 1194, 1200, 1201, 1204, 1205, 1206, 1208, 1209, 1212, 1213, 1214, 1218, 1219, 1220, 1222, 1225, 1227, 1228, 1229, 1232, 1236, 1238, 1240, 1242, 1243, 1245, 1248, 1250, 1252, 1253, 1255, 1258, 1261, 1269, 1273, 1278, 1279, 1280, 1283, 1284, 1292, 1293, 1302, 1303, 1306, 1310, 1311, 1315, 1318, 1319, 1321, 1325, 1330, 1331, 1342, 1343, 1347, 1348, 1352, 1357, 1359, 1361, 1365, 1374, 1380, 1382, 1384, 1388, 1389, 1390, 1391, 1392, 1395, 1397, 1403, 1404, 1407, 1413, 1417, 1418, 1420, 1425, 1429, 1431, 1435, 1436, 1437, 1447, 1450, 1461, 1462, 1464, 1473, 1474, 1475, 1477, 1485, 1490, 1494, 1496, 1497, 1502, 1503, 1507, 1513, 1514, 1516, 1521, 1522, 1526, 1530, 1534, 1539, 1541, 1549, 1552, 1554, 1555, 1561, 1564, 1569, 1572, 1579, 1585, 1586, 1590, 1591, 1593, 1595, 1596, 1597, 1598, 1600, 1604, 1608, 1610, 1611, 1612, 1616, 1617, 1624, 1631, 1633, 1636, 1641, 1646, 1649, 1650, 1658, 1660, 1665, 1667, 1671, 1673, 1679, 1683, 1689, 16



92, 1696, 1698, 1703, 1705, 1707, 1708, 1713, 1716, 1722, 1728, 1733, 1734, 1739, 1740, 1742, 1744, 1745, 1756, 1759, 1760, 1764, 1768, 1771, 1776, 1777, 1780, 1782, 1787, 1800, 1807, 1814, 1824, 1826, 1827, 1842, 1844, 1854, 1857, 1863, 1867, 1873, 1874, 1878, 1881, 1883, 1887, 1889, 1890, 1891, 1892, 1894, 1896, 1903, 1905, 1906, 1910, 1919, 1924, 1926, 1931, 1933, 1943, 1944, 1948, 1952, 1954, 1967, 1971, 1973, 1976, 1979, 1985, 1986, 1987, 1989, 1992, 1994, 1995, 1998, 2000, 2005, 2006, 2018, 2019, 2030, 2040, 2043, 2048, 2054, 2055, 2057, 2061, 2070, 2071, 2074, 2077, 2082, 2084, 2087, 2089, 2093, 2096, 2098, 2103, 2104, 2107, 2111, 2120, 2122, 2125, 2128, 2138, 2150, 2152, 2155, 2160, 2175, 2177, 2182, 2189, 2195, 2200, 2201, 2203, 2217, 2219, 2225, 2226, 2231, 2234, 2235, 2236, 2237, 2245, 2247, 2274, 2276, 2278, 2280, 2282, 2283, 2286, 2292, 2303, 2304, 2306, 2310, 2315, 2316, 2319, 2320, 2321, 2330, 2333, 2336, 2339, 2343, 2344, 2345, 2351, 2367, 2368, 2371, 2374, 2382, 2389, 2392, 2395, 2396, 2400, 2402, 2407, 2410, 2412, 2416, 2421, 2422, 2434, 2442, 2446, 2447, 2462, 2473, 2477, 2478, 2481, 2486, 2490, 2492, 2495, 2502, 2505, 2507, 2509, 2512, 2513, 2522, 2525, 2527, 2528, 2536, 2543, 2549, 2556, 2559, 2561, 2563, 2565, 2583, 2587, 2590, 2592, 2596, 2598, 2601, 2603, 2604, 2606, 2617, 2622, 2625, 2626, 2636, 2638, 2640, 2643, 2654, 2660, 2668, 2673, 2677, 2679, 2688, 2695, 2699, 2701, 2713, 2714, 2723, 2737, 2741, 2747, 2753, 2762, 2764, 2769, 2772, 2775, 2776, 2785, 2796, 2802, 2805, 2808, 2826, 2828, 2830, 2831, 2834, 2836, 2853, 2875, 2877, 2878, 2884, 2906, 2938, 2945, 2948, 2950, 2961, 2964, 2966, 2968, 2979, 2980, 2985, 2989, 2998, 3008, 3011, 3015, 3018, 3022, 3027, 3048, 3049, 3051, 3053, 3056, 3062, 3071, 3075, 3080, 3093, 3094, 3095, 3097, 3101, 3107, 3109, 3119, 3122, 3128, 3149, 3150, 3151, 3158, 3166, 3167, 3173, 3178, 3180, 3181, 3182, 3186, 3190, 3195, 3200, 3201, 3203, 3204, 3205, 3208, 3216, 3217, 3223, 3224, 3232, 3236, 3240, 3248, 3251, 3253, 3269, 3276, 3278, 3279, 3286, 3292, 3299, 3306, 3309, 3336, 3340, 3342, 3344, 3351, 3352, 3356, 3357, 3371, 3375, 3380, 3387, 3396, 3404, 3407, 3410, 3423, 3430, 3445, 3451, 3463, 3466, 3471, 3478, 3479, 3502, 3513, 3520, 3528, 3531, 3534, 3539, 3540, 3546, 3551, 3565, 3577, 3579, 3603, 3606, 3608, 3612, 3614, 3616, 3620, 3647, 3650, 3653, 3658, 3664, 3677, 3682, 3686, 3694, 3697, 3705, 3707, 3724, 3728, 3744, 3749, 3751, 3754, 3761, 3765, 3776, 3778, 3781, 3792, 3797, 3799, 3801, 3834, 3840, 3841, 3848, 3861, 3863, 3883, 3901, 3903, 3919, 3924, 3941, 3943, 3960, 3965, 3970, 3971, 3989, 3992, 4007, 4013, 4015, 4037, 4039, 4045, 4050, 4055, 4069, 4072, 4073, 4091, 4096, 4106, 4112, 4124, 4129, 4133, 4140, 4146, 4156, 4165, 4188, 4207, 4209, 4210, 4215, 4221, 4236, 4237, 4247, 4252, 4253, 4257, 4261, 4266, 4270, 4318, 4330, 4341, 4346, 4359, 4363, 4365, 4366, 4388, 4415, 4418, 4436, 4438, 4453, 4468, 4474, 4477, 4503, 4512, 4513, 4519, 4522, 4538, 4548, 4567, 4575, 4576, 4577, 4583, 4590, 4621, 4639, 4651, 4659, 4681, 4693, 4698, 4700, 4702, 4729, 4731, 4739, 4741, 4742, 4748, 4749, 4758, 4764, 4765, 4771, 4772, 4780, 4785, 4803, 4804, 4838, 4840, 4843, 4868, 4871, 4878, 4885, 4898, 4901, 4918, 4924, 4933, 4939, 4954, 4959, 4979, 4982, 4988, 4991, 4999, 5000, 5008, 5021, 5023, 5030, 5039, 5060, 5062, 5063, 5096, 5116, 5137, 5143, 5145, 5162, 5163, 5167, 5172, 5186, 5218, 5225, 5238, 5240, 5252, 5260, 5279, 5285, 5295, 5301, 5310, 5314, 5317, 5331, 5332, 5334, 5348, 5353, 5354, 5390, 5391, 5392, 5405, 5407, 5432, 5449, 5451, 5453, 5460, 5464, 5466, 5471, 5473, 5477, 5492, 5506, 5508, 5537, 5540, 5543, 5554, 5561, 5566, 5570, 5576, 5579, 5587, 5616, 5637, 5672, 5674, 5676, 5684, 5694, 5716, 5732, 5774, 5792, 5798, 5800, 5808, 5823, 5838, 5844, 5863, 5896, 5897, 5899, 5900, 5916, 5921, 5930, 5960, 5975, 6039, 6055, 6057, 6059, 6067, 6068, 6078, 6092, 6099,



6102, 6107, 6136, 6151, 6169, 6189, 6191, 6218, 6233, 6249, 6271, 6274, 6296, 6318  
, 6352, 6363, 6376, 6407, 6430, 6435, 6441, 6463, 6486, 6491, 6502, 6512, 6518, 652  
0, 6534, 6542, 6549, 6553, 6589, 6590, 6593, 6599, 6614, 6625, 6634, 6643, 6655, 66  
70, 6680, 6684, 6691, 6692, 6701, 6708, 6711, 6724, 6730, 6732, 6752, 6799, 6803, 6  
809, 6812, 6834, 6849, 6855, 6877, 6878, 6879, 6899, 6907, 6919, 6936, 6945, 6946,  
6954, 6955, 6956, 6958, 6981, 7000, 7011, 7030, 7032, 7033, 7108, 7111, 7127, 7164  
, 7171, 7175, 7179, 7181, 7185, 7225, 7226, 7281, 7288, 7295, 7307, 7325, 7359, 736  
0, 7390, 7392, 7411, 7476, 7520, 7535, 7548, 7552, 7558, 7567, 7589, 7596, 7616, 76  
45, 7675, 7679, 7714, 7726, 7747, 7770, 7780, 7785, 7805, 7818, 7855, 7870, 7883, 7  
923, 7935, 7936, 7953, 7974, 7999, 8028, 8030, 8069, 8074, 8093, 8104, 8111, 8122,  
8150, 8154, 8172, 8173, 8189, 8192, 8193, 8194, 8223, 8236, 8290, 8304, 8377, 8425  
, 8438, 8439, 8464, 8481, 8492, 8521, 8556, 8559, 8575, 8582, 8595, 8602, 8606, 862  
4, 8628, 8648, 8654, 8666, 8672, 8689, 8738, 8739, 8744, 8775, 8787, 8837, 8841, 88  
42, 8860, 8928, 8929, 8970, 8977, 8993, 9009, 9019, 9020, 9029, 9041, 9051, 9087, 9  
111, 9151, 9195, 9208, 9298, 9303, 9327, 9344, 9352, 9360, 9364, 9388, 9400, 9402,  
9446, 9448, 9449, 9461, 9462, 9470, 9485, 9497, 9512, 9539, 9546, 9560, 9572, 9601  
, 9612, 9642, 9649, 9653, 9677, 9689, 9692, 9704, 9708, 9758, 9765, 9794, 9813, 986  
0, 9916, 9922, 9927, 9949, 9971, 9978, 9981, 9986, 9987, 10017, 10040, 10065, 1007  
3, 10084, 10097, 10105, 10120, 10124, 10134, 10166, 10187, 10197, 10202, 10204, 1  
0241, 10242, 10279, 10308, 10324, 10336, 10351, 10361, 10458, 10460, 10567, 1064  
3, 10676, 10705, 10712, 10717, 10759, 10786, 10787, 10857, 10883, 10899, 10911, 1  
0933, 10944, 10958, 10963, 11011, 11015, 11024, 11036, 11039, 11049, 11060, 1111  
9, 11130, 11146, 11172, 11203, 11210, 11216, 11219, 11230, 11245, 11316, 11358, 1  
1371, 11376, 11423, 11475, 11534, 11590, 11649, 11653, 11677, 11686, 11707, 1171  
1, 11740, 11748, 11751, 11780, 11823, 11829, 11843, 11890, 11896, 11919, 11947, 1  
1956, 11976, 12026, 12037, 12045, 12072, 12087, 12108, 12119, 12154, 12160, 1220  
8, 12215, 12216, 12228, 12229, 12235, 12247, 12294, 12333, 12400, 12437, 12455, 1  
2458, 12460, 12469, 12471, 12510, 12528, 12567, 12569, 12593, 12685, 12694, 1270  
4, 12721, 12726, 12754, 12790, 12817, 12857, 12914, 12928, 12936, 12956, 13002, 1  
3012, 13026, 13030, 13035, 13038, 13057, 13067, 13082, 13114, 13143, 13159, 1319  
3, 13204, 13214, 13270, 13278, 13284, 13326, 13335, 13417, 13421, 13423, 13460, 1  
3479, 13558, 13607, 13695, 13696, 13742, 13764, 13816, 13827, 13833, 13837, 1387  
4, 13879, 13974, 13987, 14022, 14100, 14115, 14140, 14202, 14272, 14342, 14350, 1  
4370, 14376, 14385, 14393, 14408, 14409, 14415, 14417, 14442, 14486, 14509, 1456  
0, 14565, 14713, 14729, 14743, 14755, 14798, 14862, 14874, 14913, 14934, 14990, 1  
5007, 15011, 15120, 15170, 15194, 15217, 15227, 15235, 15285, 15314, 15321, 1532  
5, 15332, 15438, 15499, 15573, 15611, 15651, 15668, 15732, 15735, 15741, 15757, 1  
5780, 15808, 15813, 15847, 15870, 15941, 15953, 15977, 16002, 16017, 16060, 1610  
8, 16161, 16286, 16287, 16304, 16336, 16374, 16377, 16384, 16414, 16505, 16563, 1  
6623, 16665, 16670, 16674, 16689, 16691, 16710, 16727, 16743, 16794, 16828, 1685  
1, 16900, 16974, 17005, 17024, 17029, 17038, 17039, 17051, 17086, 17098, 17148, 1  
7151, 17195, 17206, 17266, 17316, 17323, 17326, 17331, 17357, 17376, 17466, 1748  
9, 17531, 17559, 17642, 17681, 17791, 17868, 17926, 17929, 17988, 17991, 18009, 1  
8026, 18027, 18056, 18116, 18168, 18232, 18307, 18309, 18438, 18503, 18504, 1851  
1, 18590, 18628, 18629, 18630, 18636, 18647, 18672, 18691, 18694, 18719, 18909, 1  
8988, 19023, 19036, 19096, 19126, 19132, 19139, 19193, 19204, 19210, 19277, 1930  
4, 19314, 19325, 19539, 19544, 19547, 19631, 19632, 19635, 19675, 19700, 19705, 1



9740, 19748, 19921, 19939, 19951, 19972, 19985, 20042, 20052, 20133, 20141, 20152, 20173, 20230, 20245, 20269, 20287, 20335, 20355, 20396, 20407, 20455, 20501, 20564, 20580, 20583, 20664, 20683, 20710, 20768, 20776, 20778, 20789, 20794, 20988, 21058, 21087, 21141, 21143, 21151, 21186, 21199, 21216, 21224, 21385, 21412, 21468, 21475, 21478, 21479, 21486, 21487, 21515, 21569, 21616, 21629, 21673, 21702, 21729, 21737, 21747, 21852, 21927, 21969, 22060, 22062, 22068, 22073, 22114, 22131, 22244, 22301, 22320, 22366, 22433, 22450, 22482, 22490, 22498, 22536, 22727, 22787, 22947, 22994, 23010, 23026, 23063, 23084, 23135, 23158, 23180, 23252, 23392, 23457, 23491, 23500, 23568, 23607, 23721, 23730, 23787, 23935, 23971, 23991, 24023, 24185, 24215, 24232, 24398, 24406, 24476, 24548, 24550, 24555, 24562, 24566, 24591, 24592, 24616, 24633, 24673, 24721, 24735, 24743, 24761, 24832, 24891, 24967, 24976, 25062, 25080, 25230, 25391, 25407, 25433, 25463, 25493, 25543, 25613, 25668, 25756, 25919, 26022, 26048, 26050, 26092, 26291, 26297, 26329, 26342, 26371, 26535, 26566, 26582, 26676, 26741, 26838, 26908, 26910, 26973, 26984, 27111, 27119, 27163, 27256, 27296, 27353, 27392, 27428, 27492, 27594, 27644, 27666, 27682, 27771, 27885, 27895, 27959, 27987, 28088, 28116, 28134, 28137, 28248, 28263, 28365, 28466, 28548, 28549, 28787, 28816, 28845, 28966, 29002, 29042, 29054, 29072, 29127, 29138, 29265, 29326, 29345, 29434, 29481, 29487, 29500, 29588, 29731, 29816, 29827, 29868, 29905, 29964, 30037, 30097, 30153, 30169, 30280, 30346, 30405, 30433, 30461, 30493, 30513, 30550, 30583, 30646, 30654, 30909, 30915, 30921, 30930, 30974, 30997, 31052, 31056, 31142, 31199, 31283, 31285, 31303, 31505, 31578, 31605, 31948, 31957, 31997, 32124, 32139, 32142, 32272, 32403, 32555, 32601, 32630, 32631, 32648, 32699, 32768, 32807, 32849, 32912, 32932, 32961, 32965, 33129, 33171, 33200, 33282, 33334, 33623, 34258, 34302, 34654, 34708, 35024, 35031, 35388, 35395, 35462, 35488, 35586, 35600, 35747, 35750, 35774, 35802, 36071, 36112, 36189, 36252, 36254, 36294, 36328, 36357, 36448, 36476, 36477, 36479, 36485, 36637, 36749, 36849, 36874, 36894, 37170, 37185, 37187, 37227, 37612, 37695, 37701, 37767, 37793, 37805, 37815, 37826, 37906, 37992, 38008, 38010, 38046, 38080, 38130, 38236, 38385, 38763, 38787, 39166, 39176, 39201, 39237, 39288, 39398, 39482, 39643, 39786, 39831, 39960, 39980, 40089, 40105, 40140, 40152, 40192, 40220, 40274, 40293, 40303, 40398, 40549, 40604, 40625, 40666, 40690, 40816, 40843, 40847, 40894, 40896, 40962, 40969, 41003, 41087, 41107, 41132, 41216, 41226, 41265, 41314, 41321, 41357, 41367, 41539, 41576, 41641, 41717, 41820, 42033, 42067, 42172, 42490, 42662, 42795, 42813, 42916, 43339, 43351, 43388, 43482, 43498, 43691, 43840, 43905, 43924, 43932, 44033, 44129, 44279, 44821, 44883, 44945, 44951, 45097, 45162, 45359, 45389, 45557, 45582, 45638, 45813, 45830, 45919, 45960, 46038, 46086, 46104, 46187, 46281, 46428, 46463, 46481, 46574, 47047, 47324, 47418, 47523, 47717, 48007, 48264, 48334, 48489, 48501, 48702, 48788, 48976, 48994, 49504, 49550, 49703, 49711, 49978, 49995, 50006, 50338, 50511, 50799, 50946, 50947, 50951, 50980, 51017, 51150, 51244, 51530, 51616, 51977, 52007, 52062, 52364, 52441, 52586, 52598, 52768, 52883, 52978, 53047, 53064, 53114, 53127, 54024, 54546, 54578, 54735, 54803, 55123, 55289, 55510, 55661, 55744, 55843, 55885, 55921, 56297, 56403, 56696, 57113, 57424, 57614, 57779, 58294, 58326, 58721, 58908, 59346, 59541, 59651, 59882, 60076, 60164, 60250, 60618, 60799, 61144, 61208, 61217, 61617



### **2.7.8. Random Number Generator**

The SC code utilizes two random number generators. The first uses the second. The first is described by the following pseudo code:

```
function b=RNG(a)

for i = 0:7

    a = RNG_2( a, ( (a) % (89) ) )

    b = (b) % (a)

end
```

The second random number generator uses a selectable set of feedback taps. The second is described by the following pseudo code:

```
function a=RNG_2(a,b)

tap_list=[32, 31, 30, 10

32, 31, 29, 1

32, 31, 26, 18

32, 31, 26, 9

32, 31, 26, 7

32, 31, 23, 10

32, 31, 22, 17

32, 31, 21, 16

32, 31, 21, 5

32, 31, 18, 10

32, 31, 16, 2

32, 31, 15, 10

32, 31, 14, 4
```

32, 31, 13, 8  
32, 31, 9, 7  
32, 31, 5, 4  
32, 30, 29, 23  
32, 30, 29, 20  
32, 30, 29, 16  
32, 30, 29, 15  
32, 30, 27, 24  
32, 30, 27, 21  
32, 30, 27, 12  
32, 30, 27, 8  
32, 30, 26, 25  
32, 30, 26, 13  
32, 30, 25, 16  
32, 30, 23, 16  
32, 30, 23, 14  
32, 30, 23, 4  
32, 30, 21, 14  
32, 30, 19, 8  
32, 30, 19, 4  
32, 30, 17, 3  
32, 30, 15, 6  
32, 30, 11, 8  
32, 30, 11, 5

32, 30, 8, 3

32, 30, 7, 4

32, 29, 28, 19

32, 29, 27, 23

32, 29, 27, 21

32, 29, 27, 6

32, 29, 26, 6

32, 29, 25, 6

32, 29, 22, 18

32, 29, 19, 16

32, 29, 17, 15

32, 29, 15, 8

32, 29, 6, 5

32, 29, 6, 4

32, 28, 25, 15

32, 28, 25, 11

32, 28, 25, 6

32, 28, 23, 6

32, 28, 15, 13

32, 28, 9, 7

32, 27, 26, 14

32, 27, 25, 20

32, 27, 25, 19

32, 27, 25, 17

32, 27, 25, 7  
32, 27, 25, 5  
32, 27, 23, 6  
32, 27, 21, 6  
32, 27, 20, 18  
32, 27, 18, 14  
32, 27, 15, 14  
32, 27, 14, 12  
32, 27, 14, 9  
32, 27, 8, 6  
32, 26, 25, 10  
32, 26, 23, 12  
32, 26, 22, 7  
32, 26, 20, 11  
32, 26, 19, 9  
32, 26, 19, 7  
32, 26, 18, 13  
32, 26, 15, 7  
32, 25, 24, 7  
32, 25, 22, 15  
32, 25, 17, 7  
32, 25, 14, 13  
32, 24, 22, 13  
32, 23, 21, 16

```
32, 23, 18, 14
32, 21, 20, 19
32, 20, 17, 15
32, 19, 18, 13]
taps[0]=tap_list[b,0]
taps[1]=tap_list[b,1]
taps[2]=tap_list[b,2]
taps[3]=tap_list[b,3]
feedback=2.^(32-taps[0]) + 2.^(32-taps[1]) + 2.^(32-taps[2]) +
2.^(32-taps[3])
if( (a) & (1) )
    a = (a) ^ (feedback)
    a = (a) >> (1)
    a = (2^31) || (a)
else
    a = (a) >> (1)
end
```

#### **2.7.9. Random Permutation**

The SC code utilizes a random permutation of length K to facilitate the construction of the random interleavers needed for the parallel filter codes. The random permutation is given by the following pseudocode. The RNG\_2 function is defined in [section 2.7.8](#).

```
function [permutation,the_seed]= Generate_Permutation(a,b)
for i=0:a-1
    permutation[i] = i + 1
```

```
end

for i=0:a-1

    c = RNG_2(b,1)

    b = ( (c) % (a-(i-1)) ) + i

    d = permutation[i]

    permutation[i] = permutation[b]

    permutation[b] = d

end
```

#### **2.7.10. RS Generator**

A Reed Solomon code is utilized in the construction of the SC code. Its construction is described by the following pseudo code. The GF\_exp and the GF\_Multiply functions are defined in [section 2.7.13](#).

```
function G_V_RS = RS_gen(K,N)

Gt=zeros[N,K]

for i=0:N-1

    for k=0:K-1

        a = ((i+1)*k) % (2^8-1)

        Gt[i,k]=GF_exp(a)

    end

end

G1=Gt[1:K,1:K]

G2=Gt[K+1:N,1:K]
```

```
G_V_RS = GF_Multiply(G2,G1^^-1)
```

GF\_Multiply implements  $G2 \cdot G1_{inv}$  where the multiplication and addition are performed in the GF field. The matrix inverse  $G1^{-1}$  can be easily implemented using Gaussian Elimination for the small matrix  $G1$ .

#### [2.7.11](#). RS Code

If the number of transmit symbols  $N$  is optionally limited to  $N \leq 256$  and signaled using  $R=1$ , then the following pseudo code is used to generate matrix  $P$ . The RS\_gen function is defined in [section 2.7.10](#).  $N$  is given by the FEC-OTI-Max-Number-of-Encoding-Symbols.

```
Num_V_RS = N - K
```

```
B_1 = RS_gen(K,K+Num_V_RS)
```

```
P = [I[K]
```

```
      B_1 ]
```

```
Num_B = 0
```

```
K_eff = K
```

#### [2.7.12](#). SC\_Filter\_Data

```
[Filter_data, filter_N]=SC_filter_data(z)
```

```
Filter_data=[0,2147483648,2863311531,3221225472,3435973837,3579139413,
3681400539,3758096384,3817748708,3865470566,3904515724,3937053355,39
64585196,3988183918,4008636143,4026531840,4042322161,4056358002,40689
16386,4080218931,4090445044,4099741510,4108229587,4116010325,41231686
04,4129776246,4135894433,4141575607,4146864975,4151801719,4156419964,
4160749568,4164816772,4168644728,4172253945,4175662649,4178887099,418
1941841,4184839929,4187593114,4190211996,4192706170,4195084336,419735
4403,4199523578,4201598442,4203585013,4205488811,4207314902,420906795
0,4210752251,4212371771,4213930177,4215430865,4216876982,4218271451,4
219616993,4220916136,4222171240,4223384508,4224557996,4225693630,4226
793212,4227858432,4228890876,4229892034,4230863307,4231806012,4232721
```

```
393,4233610620,4234474799,4235314972,4236132128,4236927197,4237701065  
,4238454568,4239188500,4239903613,4240600621,4241280205,4241943008,42  
42589646,4243220702,4243836733,4244438269,4245025816,4245599856,42461  
60849,4246709236,4247245437,4247769853,4248282869,4248784852,42492761  
55,4249757114,4250228053,4250689283,4251141099,4251583788,4294967295]
```

```
filter_N=min(100,z)
```

```
Filter_data[Filter_N-1]=4294967295
```

### **2.7.13. GF(256) Operations**

The SC code utilizes Galois field arithmetic in GF(256). The primitive polynomial is  $D^8 + D^4 + D^3 + D^2 + 1$ . The `b=GF_exp(a)` function raises the primitive element to the supplied power, `a`. The function `C=GF_Multiply(A,B)` multiplies two matrices in the Galois field.

## **3. FEC Packets**

Encoded packets are constructed using a 4 byte FEC Payload ID followed by transmit symbols. The Source ID field (SID) of the FEC Payload ID identifies the Source ID of the first transmit symbol in the packet. Subsequent transmit symbols have sequential increasing SIDs. If the last transmit symbol of a packet contains source padding, these padding bytes may be excluded from the packet. Otherwise, packets must contain only whole transmit symbols.

It is RECOMMENDED that each packet include exactly one transmit symbol. Multiple transmit symbols per packet SHALL also be supported.

### **3.1. Segmentation**

In order to encode large files within the working memory constraint, the source file may need to be segmented into transmit blocks and working blocks.

#### **3.1.1. Transmit Blocks**

Given a source file of size `F` bytes and a transmit symbol size of `T` bytes, the file can be divided into  $K_{total} = \text{ceil}(F/T)$  transmit symbols. A source transmit block is a collection of `KL` or `KS` of these transmit symbols. `KL` and `KS` may be different if the total number of source transmit blocks does not evenly divide the number of transmit symbols required to represent the file. The number of



source transmit blocks with  $K_L$  transmit symbols and the number of source transmit blocks with  $K_S$  transmit symbols are communicated to the decoder using parameter  $Z$ . After encoding, a transmit block consists of a source transmit block and a repair transmit block.

The transmit blocks are ordered such that the first  $ZL$  transmit block are encoded from source transmit blocks of size  $K_L$  transmit symbols. The remaining  $ZS$  transmit blocks are encoded from source transmit blocks are of size  $K_S$  transmit symbols. Given  $Z$ , the first  $ZL = \text{ceil}(K_{\text{total}}/Z) * Z - K_{\text{total}}$  transmit blocks are of size  $K_L = \text{floor}(K_{\text{total}}/Z)$  and the remaining  $ZS = K_{\text{total}} - \text{floor}(K_{\text{total}}/Z) * Z$  transmit blocks are of size  $K_S = \text{ceil}(K_{\text{total}}/Z)$ .

### **3.1.2. Working Blocks**

In order to satisfy the working memory requirement, the transmit symbols can be further subdivided into working symbols. The working symbols are ordered in a packet such that the first  $\text{ceil}(T/AL/N_s) * N_s - T/AL$  working-blocks are of size  $TWL = \text{floor}(T/AL/N_s)$  and the remaining  $T/AL - \text{floor}(T/AL/N_s) * N_s$  working-blocks are of size  $TWS = \text{ceil}(T/AL/N_s)$  in a given packet. A working block is then a collection of working symbols. The size of the working symbols are selected such that an entire source working block can fit into the working memory, where the source working block is the portion of the working block consisting of only source data and not repair data. The  $i$ th working block consists of the  $i$ th working symbol of transmit symbols of a transmit block. The  $K_L$  (or  $K_S$ ) transmit symbols of a source transmit block can be viewed as a collection of working symbols or equivalently as a collection of source working blocks.

After encoding, a working block consists of a source working block and a repair working block. The receiver attempts to decode on a subset of the source and repair working symbols in a working block.

### **3.1.3. Padding**

In cases where effective number of transmit symbols used by the encoder and decoder,  $K_{\text{eff}}$ , is  $K_{\text{eff}} > K$ , then  $K_{\text{eff}} - K$  transmit symbols must be padded (with 0) to the data before encoding. These padded symbols do not need to be transmitted, as the decoder is aware that they are padding. (Padding SIDs 0 to  $K_{\text{eff}} - K - 1$  MAY be transmitted, but it is RECOMMENDED that they are not.)

## **4. Parameter Selection**

The code requires  $F$ ,  $T$ ,  $Z$ ,  $N_s$ , and  $AL$ .  $F$  is the total file size in Bytes.  $T$  is the transmit symbol size in bytes, and it is RECOMMENDED



that it be equal to the packet payload size. The number of transmit blocks  $Z$  MUST be chosen such that  $KL \leq K_{\max}$ , where  $KL$  is computed in [section 3.1.1](#).  $K_{\max}$  is the maximum value in [section 2.7.7](#).

The number of working symbols,  $N_s$ , MUST be chosen small enough such that  $KL \cdot TWL$  is less than or equal to the working memory requirement. The byte alignment,  $AL$ , is to be chosen based on the protocol and the typical machine architectures, a value of 4 (bytes) is RECOMMENDED.

## 5. Control Messages

This section describes control messages that are used by the FEC. All fields are big-endian.

### 5.1. FEC Payload ID

The FEC payload ID is a 4-byte field defined as follows:

[0:7] TBN, (8 bits, unsigned integer): A non-negative integer identifier indicating the transmit block number.

[8:31] SID, (24 bits, unsigned integer): A non-negative integer identifier indicating the transmit symbols in the packet. SID 0 to  $K-1$  indicate systematic symbols.

The FEC Payload ID is shown in Figure 4.

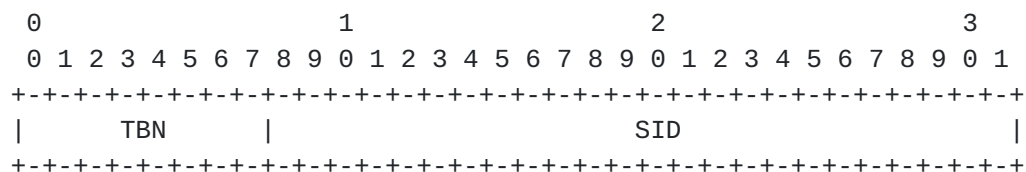


Figure 4 FEC Payload ID format

### 5.2. FEC Object Transmission Information

#### 5.2.1. FEC Encoding ID

The value of the FEC Encoding ID MUST be 7, as assigned by IANA (see [Section 8](#)).

#### 5.2.2. Common

The Common FEC Object Transmission Information elements used by this FEC Scheme are:

[0:39] Transfer Length (F), (40 bits, unsigned integer): A non-negative integer. This is the transfer length of the object in bytes.

[40:47] are reserved.

[48:63] Transmit Symbol Size (T), (16 bits, unsigned integer): A positive integer that is less than  $2^{16}$ . This is the size of a transmit symbol in units of bytes.

The encoded Common FEC Object Transmission Information format is shown in Figure 5.

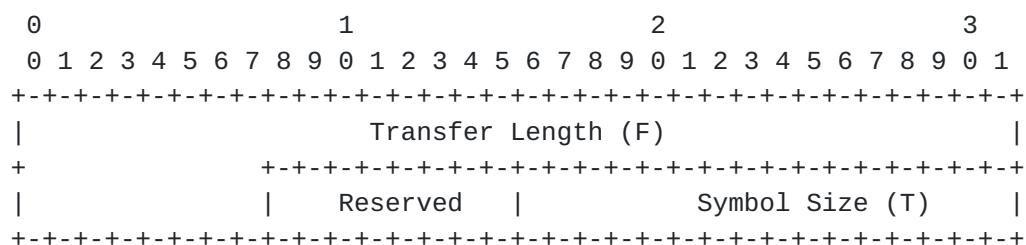


Figure 5 Encoded Common FEC Object Transmission Information for Supercharged FEC Scheme

### 5.2.3. Scheme Specific

The following parameters are carried in the Scheme-Specific FEC Object Transmission Information element for this FEC Scheme:

[0:7] Z: The number of transmit blocks (8 bits, unsigned integer)

[8:23] Ns: The number of working blocks (16 bits, unsigned integer)

[24:30] AL: A symbol alignment parameter (7 bits, unsigned integer)

[31] R: 0: Default 1: OPTIONALLY indicates that the maximum value of N satisfies  $N \leq 256$  (1 bit, boolean)

The encoded Specific FEC Object Transmission Information format is shown in Figure 5.

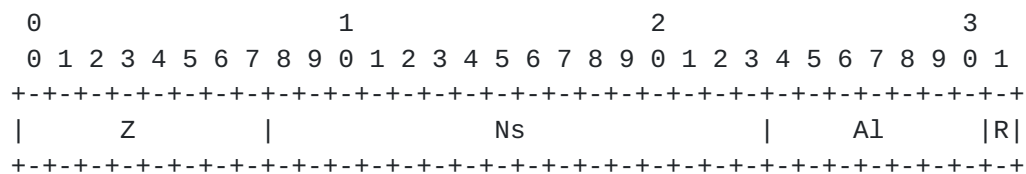


Figure 6 FEC Payload ID format



## **6. Conventions used in this document**

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [RFC-2119](#) [[RFC2119](#)].

In this document, these words will appear with that interpretation only when in ALL CAPS. Lower case uses of these words are not to be interpreted as carrying [RFC-2119](#) significance.

## **7. Security Considerations**

Users could potentially be subject to a denial of service attack if a single erroneous packet is injected into the delivery stream. Therefore, it is RECOMMENDED that source authentication and integrity checking are applied to the file or data object before delivering decoded data to applications. The hashing methodology of SHA-256 is an example [2].

## **8. IANA Considerations**

Values of FEC Encoding IDs and FEC Instance IDs are subject to IANA registration. For general guidelines on IANA considerations as they apply to this document, see [[RFC5052](#)]. IANA is requested to assign a value under the ietf:rmt:fec:encoding name-space to "Supercharged Code" as the FEC Encoding ID value associated with this specification, preferably the value 7.

## **9. References**

### **9.1. Normative References**

- [1] Bradner, S., "Key words for use in RFCs to Indicate Requirement Levels", [BCP 14](#), [RFC 2119](#), March 1997.
- [2] "Secure Hash Standard", National Institute of Standards and Technology FIPS PUB 180-3, October 2008.

### **9.2. Informative References**

- [3] Timothy Vismor, "Matrix Algorithms."
- [4] Sergio Pissanetzky, "Sparse Matrix Technology," Academic Press, London (1984).

- [5] Timothy A. Davis, "Direct Methods for Sparse Linear Systems" SIAM, Philadelphia, Pa (2006)
- [6] Yousef Saad, "Iterative Methods for Sparse Linear Systems" 2nd Ed. SIAM, Philadelphia, Pa (2003)
- [7] I.S. Duff, A.M. Erisman, and J. K. Reid, "Direct Methods for Sparse Matrices" (2008) (ISBN: 978-0198534082)
- [8] John K. Reid, "Solution of linear systems of equations: Direct methods" (1977)
- [9] Golub, G.H. "Numerical methods for solving linear least-squares problems" Numerische Mathematik Volume 7, Number 3 (1965) pp 206-216

## **10. Acknowledgments**

This document was prepared using 2-Word-v2.0.template.dot.

### Authors' Addresses

Erik Stauffer  
Broadcom  
190 Mathilda Place  
Sunnyvale, Ca 94086

Email: [eriks@broadcom.com](mailto:eriks@broadcom.com)

BZ Shen  
Broadcom  
5300 California Avenue  
Irvine, CA 92617

Email: [bzshen@broadcom.com](mailto:bzshen@broadcom.com)

Soumen Chakraborty  
Broadcom  
RMZ Ecospace  
Bellandur  
Bangalore 560037, India

Email: [soumen@broadcom.com](mailto:soumen@broadcom.com)

Djordje Tujkovic  
Broadcom  
190 Mathilda Place  
Sunnyvale, Ca 94086

Email: [djordje@broadcom.com](mailto:djordje@broadcom.com)

Jing Huang  
Broadcom  
190 Mathilda Place  
Sunnyvale, Ca 94086

Email: [jingh@broadcom.com](mailto:jingh@broadcom.com)

Shiv Shet  
Broadcom  
RMZ Ecospace  
Bellandur  
Bangalore 560037, India

Email: [shivaprakash@broadcom.com](mailto:shivaprakash@broadcom.com)

Kamlesh Rath  
Broadcom  
190 Mathilda Place  
Sunnyvale, Ca 94086

Email: [krath@broadcom.com](mailto:krath@broadcom.com)