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CUBIC for Fast and Long-Distance Networks  
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## Abstract

CUBIC is a standard TCP congestion control algorithm that uses a cubic function instead of a linear congestion window increase function to improve scalability and stability over fast and long-distance networks. CUBIC has been adopted as the default TCP congestion control algorithm by the Linux, Windows, and Apple stacks.

This document updates the specification of CUBIC to include algorithmic improvements based on these implementations and recent academic work. Based on the extensive deployment experience with CUBIC, it also moves the specification to the Standards Track, obsoleting [RFC 8312](#). This also requires updating [RFC 5681](#), to allow for CUBIC's occasionally more aggressive sending behavior.

## About This Document

This note is to be removed before publishing as an RFC.

Status information for this document may be found at  
<https://datatracker.ietf.org/doc/draft-ietf-tcpm-rfc8312bis/>.

Discussion of this document takes place on the TCPM Working Group mailing list (<mailto:tcpm@ietf.org>), which is archived at  
<https://mailarchive.ietf.org/arch/browse/tcpm/>.

Source for this draft and an issue tracker can be found at  
<https://github.com/NTAP/rfc8312bis>.

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## [1.](#) Introduction

CUBIC has been adopted as the default TCP congestion control algorithm in the Linux, Windows, and Apple stacks, and has been used and deployed globally. Extensive, decade-long deployment experience in vastly different Internet scenarios has convincingly demonstrated that CUBIC is safe for deployment on the global Internet and delivers substantial benefits over classical Reno congestion control [[RFC5681](#)]. It is therefore to be regarded as the currently most widely deployed standard for TCP congestion control. CUBIC can also be used for other transport protocols such as QUIC [[RFC9000](#)] and SCTP [[RFC4960](#)] as a default congestion controller.

The design of CUBIC was motivated by the well-documented problem classical Reno TCP has with low utilization over fast and long-distance networks [[K03](#)] [[RFC3649](#)]. This problem arises from a slow increase of the congestion window following a congestion event in a network with a large bandwidth-delay product (BDP). [[HLRX07](#)] indicates that this problem is frequently observed even in the range of congestion window sizes over several hundreds of packets. This problem is equally applicable to all Reno-style standards and their variants, including TCP-Reno [[RFC5681](#)], TCP-NewReno [[RFC6582](#)] [[RFC6675](#)], SCTP [[RFC4960](#)], TFRC [[RFC5348](#)], and QUIC

congestion control [[RFC9002](#)], which use the same linear increase function for window growth. We refer to all Reno-style standards and their variants collectively as "Reno" below.

CUBIC, originally proposed in [[HRX08](#)], is a modification to the congestion control algorithm of classical Reno to remedy this problem. Specifically, CUBIC uses a cubic function instead of the linear window increase function of Reno to improve scalability and stability under fast and long-distance networks.

This document updates the specification of CUBIC to include algorithmic improvements based on the Linux, Windows, and Apple implementations and recent academic work. Based on the extensive deployment experience with CUBIC, it also moves the specification to the Standards Track, obsoleting [[RFC8312](#)]. This requires an update to [[RFC5681](#)], which limits the aggressiveness of Reno TCP implementations in its [Section 3](#). Since CUBIC is occasionally more aggressive than the [[RFC5681](#)] algorithms, this document updates [[RFC5681](#)] to allow for CUBIC's behavior.

Binary Increase Congestion Control (BIC-TCP) [[XHR04](#)], a predecessor of CUBIC, was selected as the default TCP congestion control algorithm by Linux in the year 2005 and had been used for several years by the Internet community at large.

CUBIC uses a similar window increase function as BIC-TCP and is designed to be less aggressive and fairer to Reno in bandwidth usage than BIC-TCP while maintaining the strengths of BIC-TCP such as stability, window scalability, and round-trip time (RTT) fairness.

In the following sections, we first briefly explain the design principles of CUBIC, then provide the exact specification of CUBIC, and finally discuss the safety features of CUBIC following the guidelines specified in [[RFC5033](#)].

## [2](#). Conventions

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [BCP 14](#) [[RFC2119](#)] [[RFC8174](#)] when, and only when, they appear in all capitals, as shown here.

### [3.](#) Design Principles of CUBIC

CUBIC is designed according to the following design principles:

Principle 1: For better network utilization and stability, CUBIC uses both the concave and convex profiles of a cubic function to increase the congestion window size, instead of using just a convex function.

Principle 2: To be Reno-friendly, CUBIC is designed to behave like Reno in networks with short RTTs and small bandwidth where Reno performs well.

Principle 3: For RTT-fairness, CUBIC is designed to achieve linear bandwidth sharing among flows with different RTTs.

Principle 4: CUBIC appropriately sets its multiplicative window decrease factor in order to balance between the scalability and convergence speed.

#### [3.1.](#) Principle 1 for the CUBIC Increase Function

For better network utilization and stability, CUBIC [[HRX08](#)] uses a cubic window increase function in terms of the elapsed time from the last congestion event. While most alternative congestion control algorithms to Reno increase the congestion window using convex functions, CUBIC uses both the concave and convex profiles of a cubic function for window growth.

After a window reduction in response to a congestion event detected by duplicate ACKs, Explicit Congestion Notification-Echo (ECN-Echo, ECE) ACKs [[RFC3168](#)], TCP RACK [[RFC8985](#)] or QUIC loss detection [[RFC9002](#)], CUBIC remembers the congestion window size at which it received the congestion event and performs a multiplicative decrease of the congestion window. When CUBIC enters into congestion

avoidance, it starts to increase the congestion window using the concave profile of the cubic function. The cubic function is set to have its plateau at the remembered congestion window size, so that the concave window increase continues until then. After that, the cubic function turns into a convex profile and the convex window increase begins.

This style of window adjustment (concave and then convex) improves the algorithm stability while maintaining high network utilization [CEHRX09]. This is because the window size remains almost constant, forming a plateau around the remembered congestion window size of the last congestion event, where network utilization is deemed highest. Under steady state, most window size samples of CUBIC are close to that remembered congestion window size, thus promoting high network utilization and stability.

Note that congestion control algorithms that only use convex functions to increase the congestion window size have their maximum increments around the remembered congestion window size of the last congestion event, and thus introduce many packet bursts around the saturation point of the network, likely causing frequent global loss synchronizations.

### [3.2.](#) Principle 2 for Reno-Friendliness

CUBIC promotes per-flow fairness to Reno. Note that Reno performs well over paths with short RTTs and small bandwidths (or small BDPs). There is only a scalability problem in networks with long RTTs and large bandwidths (or large BDPs).

A congestion control algorithm designed to be friendly to Reno on a per-flow basis must increase its congestion window less aggressively in small BDP networks than in large BDP networks.

The aggressiveness of CUBIC mainly depends on the maximum window size before a window reduction, which is smaller in small-BDP networks than in large-BDP networks. Thus, CUBIC increases its congestion window less aggressively in small-BDP networks than in large-BDP networks.

Furthermore, in cases when the cubic function of CUBIC would increase the congestion window less aggressively than Reno, CUBIC simply

follows the window size of Reno to ensure that CUBIC achieves at least the same throughput as Reno in small-BDP networks. We call this region where CUBIC behaves like Reno the "Reno-friendly region".

### [3.3.](#) Principle 3 for RTT Fairness

Two CUBIC flows with different RTTs have a throughput ratio that is linearly proportional to the inverse of their RTT ratio, where the throughput of a flow is approximately the size of its congestion window divided by its RTT.

Specifically, CUBIC maintains a window increase rate independent of RTTs outside the Reno-friendly region, and thus flows with different RTTs have similar congestion window sizes under steady state when they operate outside the Reno-friendly region.

This notion of a linear throughput ratio is similar to that of Reno under high statistical multiplexing where packet loss is independent of individual flow rates. However, under low statistical multiplexing, the throughput ratio of Reno flows with different RTTs is quadratically proportional to the inverse of their RTT ratio [[XHR04](#)].

CUBIC always ensures a linear throughput ratio independent of the amount of statistical multiplexing. This is an improvement over Reno. While there is no consensus on particular throughput ratios for different RTT flows, we believe that over wired Internet paths, use of a linear throughput ratio seems more reasonable than equal throughputs (i.e., the same throughput for flows with different RTTs) or a higher-order throughput ratio (e.g., a quadratical throughput ratio of Reno under low statistical multiplexing environments).

### [3.4.](#) Principle 4 for the CUBIC Decrease Factor

To balance between scalability and convergence speed, CUBIC sets the multiplicative window decrease factor to 0.7, whereas Reno uses 0.5.

While this improves the scalability of CUBIC, a side effect of this decision is slower convergence, especially under low statistical multiplexing. This design choice is following the observation that



made: the current Internet becomes more asynchronous with less frequent loss synchronizations under high statistical multiplexing.

In such environments, even strict Multiplicative-Increase Multiplicative-Decrease (MIMD) can converge. CUBIC flows with the same RTT always converge to the same throughput independent of statistical multiplexing, thus achieving intra-algorithm fairness. We also find that in environments with sufficient statistical multiplexing, the convergence speed of CUBIC is reasonable.

## [4.](#) CUBIC Congestion Control

In this section, we discuss how the congestion window is updated during the different stages of the CUBIC congestion controller.

### [4.1.](#) Definitions

The unit of all window sizes in this document is segments of the maximum segment size (MSS), and the unit of all times is seconds. Implementations can use bytes to express window sizes, which would require factoring in the maximum segment size wherever necessary and replacing `_segments_acked_` with the number of bytes acknowledged in Figure 4.

#### [4.1.1.](#) Constants of Interest

`β__cubic_`: CUBIC multiplicative decrease factor as described in [Section 4.6](#).

`α__cubic_`: CUBIC additive increase factor used in Reno-friendly region as described in [Section 4.3](#).

`_C_`: constant that determines the aggressiveness of CUBIC in competing with other congestion control algorithms in high BDP networks. Please see [Section 5](#) for more explanation on how it is set. The unit for `_C_` is

segment  
-----  
3  
second

#### [4.1.2.](#) Variables of Interest

This section defines the variables required to implement CUBIC:

`_RTT_`: Smoothed round-trip time in seconds, calculated as described in [\[RFC6298\]](#).

`_cwnd_`: Current congestion window in segments.

`_ssthresh_`: Current slow start threshold in segments.

`_W_max_`: Size of `_cwnd_` in segments just before `_cwnd_` was reduced in the last congestion event when fast convergence is disabled. However, if fast convergence is enabled, the size may be further reduced based on the current saturation point.

`_K_`: The time period in seconds it takes to increase the congestion window size at the beginning of the current congestion avoidance stage to `_W_max_`.

`_current_time_`: Current time of the system in seconds.

`_epoch_start_`: The time in seconds at which the current congestion avoidance stage started.

`_cwnd_start_`: The `_cwnd_` at the beginning of the current congestion avoidance stage, i.e., at time `_epoch_start_`.

`W_cubic(_t_)`: The congestion window in segments at time `_t_` in seconds based on the cubic increase function, as described in [Section 4.2](#).

`_target_`: Target value of congestion window in segments after the next RTT, that is, `W_cubic(_t_ + _RTT_)`, as described in [Section 4.2](#).

`_W_est_`: An estimate for the congestion window in segments in the Reno-friendly region, that is, an estimate for the congestion window of Reno.

`_segments_acked_`: Number of MSS-sized segments acked when a "new ACK" is received, i.e., an ACK that cumulatively acknowledges the delivery of new data. This number will be a decimal value when a new ACK acknowledges an amount of data that is not MSS-sized. Specifically, it can be less than 1 when a new ACK acknowledges a segment smaller than the MSS.

#### [4.2](#). Window Increase Function

CUBIC maintains the acknowledgment (ACK) clocking of Reno by increasing the congestion window only at the reception of a new ACK.

It does not make any changes to the TCP Fast Recovery and Fast Retransmit algorithms [RFC6582][RFC6675].

During congestion avoidance, after a congestion event is detected by mechanisms described in [Section 3.1](#), CUBIC uses a window increase function different from Reno.

CUBIC uses the following window increase function:

$$W_{\text{cubic}}(t) = C * (t - K)^3 + W_{\text{max}}$$

Figure 1

where `_t_` is the elapsed time in seconds from the beginning of the current congestion avoidance stage, that is,

$$t = \text{current\_time} - \text{epoch\_start}$$

and where `_epoch_start_` is the time at which the current congestion avoidance stage starts. `_K_` is the time period that the above function takes to increase the congestion window size at the beginning of the current congestion avoidance stage to `_W_max_` if there are no further congestion events and is calculated using the following equation:

$$K = \sqrt[3]{\frac{W_{\text{max}} - \text{cwnd}_{\text{start}}}{C}}$$

Figure 2

where `_cwnd_start_` is the congestion window at the beginning of the current congestion avoidance stage.

Upon receiving a new ACK during congestion avoidance, CUBIC computes the `_target_` congestion window size after the next `_RTT_` using Figure 1 as follows, where `_RTT_` is the smoothed round-trip time.

The lower and upper bounds below ensure that CUBIC's congestion window increase rate is non-decreasing and is less than the increase rate of slow start [[SXEZ19](#)].

$$\text{target} = \begin{cases} \text{cwnd} & \text{if } W_{\text{cubic}}(t + \text{RTT}) < \text{cwnd} \\ 1.5 * \text{cwnd} & \text{if } W_{\text{cubic}}(t + \text{RTT}) > 1.5 * \text{cwnd} \\ W_{\text{cubic}}(t + \text{RTT}) & \text{otherwise} \end{cases}$$

The elapsed time `_t_` in Figure 1 MUST NOT include periods during which `_cwnd_` has not been updated due to application-limited behavior (see [Section 5.8](#)).

Depending on the value of the current congestion window size `_cwnd_`, CUBIC runs in three different regions:

1. The Reno-friendly region, which ensures that CUBIC achieves at least the same throughput as Reno.
2. The concave region, if CUBIC is not in the Reno-friendly region and `_cwnd_` is less than `_W_max_`.
3. The convex region, if CUBIC is not in the Reno-friendly region and `_cwnd_` is greater than `_W_max_`.

Below, we describe the exact actions taken by CUBIC in each region.

### 4.3. Reno-Friendly Region

Reno performs well in certain types of networks, for example, under short RTTs and small bandwidths (or small BDPs). In these networks, CUBIC remains in the Reno-friendly region to achieve at least the same throughput as Reno.

The Reno-friendly region is designed according to the analysis in [FHP00], which studies the performance of an AIMD algorithm with an additive factor of  $\alpha$  (segments per \_RTT\_) and a multiplicative factor of  $\beta$ , denoted by AIMD( $\alpha$ ,  $\beta$ ). \_p\_ is the packet loss rate. Specifically, the average congestion window size of AIMD( $\alpha$ ,  $\beta$ ) can be calculated using Figure 3.

$$\text{AVG\_AIMD}(\alpha, \beta) = \frac{\frac{\alpha * (1 + \beta)}{2 * (1 - \beta) * p}}{1}$$

Figure 3

By the same analysis, to achieve the same average window size as Reno that uses AIMD(1, 0.5),  $\alpha$  must be equal to,

$$3 * \frac{1 - \beta}{1 + \beta}$$

Thus, CUBIC uses Figure 4 to estimate the window size \_W\_est\_ in the Reno-friendly region with

$$\alpha_{\text{cubic}} = 3 * \frac{1 - \beta_{\text{cubic}}}{1 + \beta_{\text{cubic}}}$$

which achieves the same average window size as Reno. When receiving a new ACK in congestion avoidance (where \_cwnd\_ could be greater than

or less than `_W_max_`), CUBIC checks whether `W_cubic(_t_)` is less than `_W_est_`. If so, CUBIC is in the Reno-friendly region and `_cwnd_` SHOULD be set to `_W_est_` at each reception of a new ACK.

`_W_est_` is set equal to `_cwnd_start_` at the start of the congestion avoidance stage. After that, on every new ACK, `_W_est_` is updated using Figure 4. Note that this equation is for a connection where Appropriate Byte Counting (ABC) [RFC3465] is disabled. For a connection with ABC enabled, this equation SHOULD be adjusted by using the number of acknowledged bytes instead of acknowledged segments. Also note that this equation works for connections with enabled or disabled Delayed ACKs [RFC5681], as `_segments_acked_` will be different based on the segments actually acknowledged by a new ACK.

$$W_{est} = W_{est} + \alpha_{cubic} * \frac{segments\_acked}{cwnd}$$

Figure 4

Note that once `_W_est_` reaches `_W_max_`, that is, `_W_est_ >= _W_max_`, CUBIC needs to start probing to determine the new value of `_W_max_`. At this point, `α_cubic_` SHOULD be set to 1 to ensure that CUBIC can achieve the same congestion window increment as Reno, which uses AIMD(1, 0.5).

#### [4.4.](#) Concave Region

When receiving a new ACK in congestion avoidance, if CUBIC is not in the Reno-friendly region and `_cwnd_` is less than `_W_max_`, then CUBIC is in the concave region. In this region, `_cwnd_` MUST be incremented by

$$\frac{target - cwnd}{cwnd}$$

for each received new ACK, where `_target_` is calculated as described

in [Section 4.2](#).

#### 4.5. Convex Region

When receiving a new ACK in congestion avoidance, if CUBIC is not in the Reno-friendly region and `_cwnd_` is larger than or equal to `_W_max_`, then CUBIC is in the convex region.

The convex region indicates that the network conditions might have changed since the last congestion event, possibly implying more available bandwidth after some flow departures. Since the Internet is highly asynchronous, some amount of perturbation is always possible without causing a major change in available bandwidth.

Unless it is overridden by the AIMD window increase, CUBIC is very careful in this region. The convex profile aims to increase the window very slowly at the beginning when `_cwnd_` is around `_W_max_` and then gradually increases its rate of increase. We also call this region the "maximum probing phase", since CUBIC is searching for a new `_W_max_`. In this region, `_cwnd_` MUST be incremented by

$$\frac{\text{target} - \text{cwnd}}{\text{cwnd}}$$

for each received new ACK, where `_target_` is calculated as described in [Section 4.2](#).

#### 4.6. Multiplicative Decrease

When a congestion event is detected by mechanisms described in [Section 3.1](#), CUBIC updates `_W_max_` and reduces `_cwnd_` and `_ssthresh_` immediately as described below. In case of packet loss, the sender MUST reduce `_cwnd_` and `_ssthresh_` immediately upon entering loss recovery, similar to [\[RFC5681\]](#) (and [\[RFC6675\]](#)). Note that other mechanisms, such as Proportional Rate Reduction [\[RFC6937\]](#), can be used to reduce the sending rate during loss recovery more gradually. The parameter `β_cubic_` SHOULD be set to 0.7, which is different from the multiplicative decrease factor used in [\[RFC5681\]](#) (and [\[RFC6675\]](#)).

during fast recovery.

In Figure 5, `_flight_size_` is the amount of outstanding data in the network, as defined in [RFC5681]. Note that a rate-limited application with idle periods or periods when unable to send at the full rate permitted by `_cwnd_` may easily encounter notable variations in the volume of data sent from one RTT to another, resulting in `_flight_size_` that is significantly less than `_cwnd_` on a congestion event. This may decrease `_cwnd_` to a much lower value than necessary. To avoid suboptimal performance with such applications, the mechanisms described in [RFC7661] can be used to mitigate this issue as it would allow using a value between `_cwnd_` and `_flight_size_` to calculate the new `_sssthresh_` in Figure 5. The congestion window growth mechanism defined in [RFC7661] is safe to use even when `_cwnd_` is greater than the receive window as it validates `_cwnd_` based on the amount of data acknowledged by the network in an RTT which implicitly accounts for the allowed receive window. Some implementations of CUBIC currently use `_cwnd_` instead of `_flight_size_` when calculating a new `_sssthresh_` using Figure 5.

```

                                flight_size * β      // new ssthresh
sssthresh =                    cubic

                                /max(sssthresh, 2)   // reduction on packet loss, cwnd is at least
cwnd =      |
            <
            |max(sssthresh, 1)   // reduction on ECE, cwnd is at least 1 MSS
            \

                                max(sssthresh, 2)     // ssthresh is at least 2 MSS
sssthresh =
```

Figure 5

A side effect of setting `β_cubic_` to a value bigger than 0.5 is slower convergence. We believe that while a more adaptive setting of `β_cubic_` could result in faster convergence, it will make the analysis of CUBIC much harder.



Note that CUBIC MUST continue to reduce `_cwnd_` in response to congestion events due to ECN-Echo ACKs until it reaches a value of 1 MSS. If congestion events indicated by ECN-Echo ACKs persist, a sender with a `_cwnd_` of 1 MSS MUST reduce its sending rate even further. It can achieve that by using a retransmission timer with exponential backoff, as described in [\[RFC3168\]](#).

#### [4.7.](#) Fast Convergence

To improve convergence speed, CUBIC uses a heuristic. When a new flow joins the network, existing flows need to give up some of their bandwidth to allow the new flow some room for growth, if the existing flows have been using all the network bandwidth. To speed up this bandwidth release by existing flows, the following "Fast Convergence" mechanism SHOULD be implemented.

With Fast Convergence, when a congestion event occurs, we update `_W_max_` as follows, before the window reduction as described in [Section 4.6](#).

$$W_{\max} = \begin{cases} \frac{1 + \beta}{2} \cdot \text{cubic} & \text{if } \text{cwnd} < W_{\max} \text{ and fast convergence is enabled,} \\ \text{further reduce } W_{\max} & \\ \text{otherwise, remember cwnd before reduction} & \end{cases}$$

At a congestion event, if the current `_cwnd_` is less than `_W_max_`, this indicates that the saturation point experienced by this flow is getting reduced because of a change in available bandwidth. Then we allow this flow to release more bandwidth by reducing `_W_max_` further. This action effectively lengthens the time for this flow to increase its congestion window, because the reduced `_W_max_` forces the flow to plateau earlier. This allows more time for the new flow to catch up to its congestion window size.

Fast Convergence is designed for network environments with multiple CUBIC flows. In network environments with only a single CUBIC flow and without any other traffic, Fast Convergence SHOULD be disabled.

#### [4.8.](#) Timeout

In case of a timeout, CUBIC follows Reno to reduce `_cwnd_ [RFC5681]`, but sets `_ssthresh_` using  $\beta_{\text{cubic}}$  (same as in [Section 4.6](#)) in a way that is different from Reno TCP [\[RFC5681\]](#).

During the first congestion avoidance stage after a timeout, CUBIC increases its congestion window size using Figure 1, where `_t_` is the elapsed time since the beginning of the current congestion avoidance, `_K_` is set to 0, and `_W_max_` is set to the congestion window size at the beginning of the current congestion avoidance stage. In addition, for the Reno-friendly region, `_W_est_` SHOULD be set to the congestion window size at the beginning of the current congestion avoidance.

#### [4.9.](#) Spurious Congestion Events

In cases where CUBIC reduces its congestion window in response to having detected packet loss via duplicate ACKs or timeouts, there is a possibility that the missing ACK would arrive after the congestion window reduction and a corresponding packet retransmission. For example, packet reordering could trigger this behavior. A high degree of packet reordering could cause multiple congestion window reduction events, where spurious losses are incorrectly interpreted as congestion signals, thus degrading CUBIC's performance significantly.

For TCP, there are two types of spurious events - spurious timeouts and spurious fast retransmits. In case of QUIC, there are no spurious timeouts as the loss is only detected after receiving an ACK.

##### [4.9.1.](#) Spurious timeout

An implementation MAY detect spurious timeouts based on the mechanisms described in Forward RTO-Recovery [\[RFC5682\]](#). Experimental alternatives include Eifel [\[RFC3522\]](#). When a spurious timeout is detected, a TCP implementation MAY follow the response algorithm described in [\[RFC4015\]](#) to restore the congestion control state and adapt the retransmission timer to avoid further spurious timeouts.

#### [4.9.2.](#) Spurious loss detected by acknowledgements

Upon receiving an ACK, a TCP implementation MAY detect spurious losses either using TCP Timestamps or via D-SACK[RFC2883]. Experimental alternatives include Eifel detection algorithm [RFC3522] which uses TCP Timestamps and DSACK based detection [RFC3708] which uses DSACK information. A QUIC implementation can easily determine a spurious loss if a QUIC packet is acknowledged after it has been marked as lost and the original data has been retransmitted with a new QUIC packet.

In this section, we specify a simple response algorithm when a spurious loss is detected by acknowledgements. Implementations would need to carefully evaluate the impact of using this algorithm in different environments that may experience sudden change in available capacity (e.g., due to variable radio capacity, a routing change, or a mobility event).

When a packet loss is detected via acknowledgements, a CUBIC implementation MAY save the current value of the following variables before the congestion window is reduced.

```
prior_cwnd = cwnd

prior_ssthresh = ssthresh

prior_W      = W
    max      max

prior_K = K

prior_epoch      = epoch
    start        start

prior_W_{est} = W
                est
```

Once the previously declared packet loss is confirmed to be spurious, CUBIC MAY restore the original values of the above-mentioned variables as follows if the current `_cwnd_` is lower than

\_prior\_cwnd\_. Restoring the original values ensures that CUBIC's performance is similar to what it would be without spurious losses.

```

                                \
cwnd = prior_cwnd              |
                                |
ssthresh = prior_ssthresh     |
                                |
W      = prior_W               |
max      max                   |
                                |
                                > if cwnd < prior_cwnd
K = prior_K                   |
                                |
epoch      = prior_epoch      |
start      start              |
                                |
W      = prior_W               |
est      est                   |
                                /
```

In rare cases, when the detection happens long after a spurious loss event and the current \_cwnd\_ is already higher than \_prior\_cwnd\_, CUBIC SHOULD continue to use the current and the most recent values of these variables.

#### [4.10.](#) Slow Start

CUBIC MUST employ a slow-start algorithm, when \_cwnd\_ is no more than \_ssthresh\_. In general, CUBIC SHOULD use the HyStart++ slow start algorithm [[I-D.ietf-tcpm-hystartplusplus](#)], or MAY use the Reno TCP slow start algorithm [[RFC5681](#)] in the rare cases when HyStart++ is not suitable. Experimental alternatives include hybrid slow start [[HR11](#)], a predecessor to HyStart++ that some CUBIC implementations have used as the default for the last decade, and limited slow start [[RFC3742](#)]. Whichever start-up algorithm is used, work might be needed to ensure that the end of slow start and the first multiplicative decrease of congestion avoidance work well together.

When CUBIC uses HyStart++ [[I-D.ietf-tcpm-hystartplusplus](#)], it may exit the first slow start without incurring any packet loss and thus `_W_max_` is undefined. In this special case, CUBIC switches to congestion avoidance and increases its congestion window size using Figure 1, where `_t_` is the elapsed time since the beginning of the current congestion avoidance, `_K_` is set to 0, and `_W_max_` is set to the congestion window size at the beginning of the current congestion avoidance stage.

## 5. Discussion

In this section, we further discuss the safety features of CUBIC following the guidelines specified in [[RFC5033](#)].

With a deterministic loss model where the number of packets between two successive packet losses is always `_1/p_`, CUBIC always operates with the concave window profile, which greatly simplifies the performance analysis of CUBIC. The average window size of CUBIC can be obtained by the following function:

$$AVG\_W_{cubic} = \frac{\frac{4}{|/} \frac{1}{C * (3 + \beta_{cubic})} \frac{4}{|/} \frac{3}{RTT}}{\frac{4}{|/} \frac{1}{4 * (1 - \beta_{cubic})} \frac{4}{|/} \frac{3}{p}} *$$

Figure 6

With `β_cubic_` set to 0.7, the above formula reduces to:

$$AVG\_W_{cubic} = \frac{\frac{4}{|/} \frac{1}{C * 3.7} \frac{4}{|/} \frac{3}{RTT}}{\frac{4}{|/} \frac{1}{1.2} \frac{4}{|/} \frac{3}{p}} *$$

Figure 7

We will determine the value of `_C_` in the following subsection using Figure 7.

### 5.1. Fairness to Reno

In environments where Reno is able to make reasonable use of the available bandwidth, CUBIC does not significantly change this state.

Reno performs well in the following two types of networks:

1. networks with a small bandwidth-delay product (BDP)
2. networks with a short RTTs, but not necessarily a small BDP

CUBIC is designed to behave very similarly to Reno in the above two types of networks. The following two tables show the average window sizes of Reno TCP, HSTCP, and CUBIC TCP. The average window sizes of Reno TCP and HSTCP are from [\[RFC3649\]](#). The average window size of CUBIC is calculated using Figure 7 and the CUBIC Reno-friendly region for three different values of `_C_`.

Loss Rate P	Reno	HSTCP	CUBIC (C=0.04)	CUBIC (C=0.4)	CUBIC (C=4)
1.0e-02	12	12	12	12	12
1.0e-03	38	38	38	38	59
1.0e-04	120	263	120	187	333
1.0e-05	379	1795	593	1054	1874
1.0e-06	1200	12280	3332	5926	10538
1.0e-07	3795	83981	18740	33325	59261
1.0e-08	12000	574356	105383	187400	333250

Table 1: Reno TCP, HSTCP, and CUBIC with RTT = 0.1 seconds

Table 1 describes the response function of Reno TCP, HSTCP, and CUBIC in networks with  $\text{RTT} = 0.1$  seconds. The average window size is in MSS-sized segments.

Loss Rate P	Reno	HSTCP	CUBIC (C=0.04)	CUBIC (C=0.4)	CUBIC (C=4)
1.0e-02	12	12	12	12	12
1.0e-03	38	38	38	38	38
1.0e-04	120	263	120	120	120
1.0e-05	379	1795	379	379	379
1.0e-06	1200	12280	1200	1200	1874
1.0e-07	3795	83981	3795	5926	10538
1.0e-08	12000	574356	18740	33325	59261

Table 2: Reno TCP, HSTCP, and CUBIC with RTT = 0.01 seconds

Table 2 describes the response function of Reno TCP, HSTCP, and CUBIC in networks with  $\text{RTT} = 0.01$  seconds. The average window size is in MSS-sized segments.

Both tables show that CUBIC with any of these three  $\text{C}$  values is more friendly to Reno TCP than HSTCP, especially in networks with a short  $\text{RTT}$  where Reno TCP performs reasonably well. For example, in a network with  $\text{RTT} = 0.01$  seconds and  $p=10^{-6}$ , Reno TCP has an average window of 1200 packets. If the packet size is 1500 bytes, then Reno TCP can achieve an average rate of 1.44 Gbps. In this case, CUBIC with  $\text{C}=0.04$  or  $\text{C}=0.4$  achieves exactly the same rate as Reno TCP, whereas HSTCP is about ten times more aggressive than

Reno TCP.

We can see that `_C_` determines the aggressiveness of CUBIC in competing with other congestion control algorithms for bandwidth. CUBIC is more friendly to Reno TCP, if the value of `_C_` is lower. However, we do not recommend setting `_C_` to a very low value like 0.04, since CUBIC with a low `_C_` cannot efficiently use the bandwidth in fast and long-distance networks. Based on these observations and extensive deployment experience, we find `_C_=0.4` gives a good balance between Reno-friendliness and aggressiveness of window increase. Therefore, `_C_ SHOULD` be set to 0.4. With `_C_` set to 0.4, Figure 7 is reduced to:

$$\text{AVG\_W}_{\text{cubic}} = 1.054 * \frac{4 / \sqrt[3]{\text{RTT}}}{4 / \sqrt[3]{p}}$$

Figure 8

Figure 8 is then used in the next subsection to show the scalability of CUBIC.

## 5.2. Using Spare Capacity

CUBIC uses a more aggressive window increase function than Reno for fast and long-distance networks.

The following table shows that to achieve the 10 Gbps rate, Reno TCP requires a packet loss rate of 2.0e-10, while CUBIC TCP requires a packet loss rate of 2.9e-8.

Throughput (Mbps)	Average W	Reno P	HSTCP P	CUBIC P
1	8.3	2.0e-2	2.0e-2	2.0e-2



	10		83.3		2.0e-4		3.9e-4		2.9e-4	
+-----+		+-----+		+-----+		+-----+		+-----+		+
	100		833.3		2.0e-6		2.5e-5		1.4e-5	
+-----+		+-----+		+-----+		+-----+		+-----+		+
	1000		8333.3		2.0e-8		1.5e-6		6.3e-7	
+-----+		+-----+		+-----+		+-----+		+-----+		+
	10000		83333.3		2.0e-10		1.0e-7		2.9e-8	
+-----+		+-----+		+-----+		+-----+		+-----+		+

Table 3: Required packet loss rate for Reno TCP, HSTCP, and CUBIC to achieve a certain throughput

Table 3 describes the required packet loss rate for Reno TCP, HSTCP, and CUBIC to achieve a certain throughput. We use 1500-byte packets and an `_RTT_` of 0.1 seconds.

Our test results in [HLRX07] indicate that CUBIC uses the spare bandwidth left unused by existing Reno TCP flows in the same bottleneck link without taking away much bandwidth from the existing flows.

### 5.3. Difficult Environments

CUBIC is designed to remedy the poor performance of Reno in fast and long-distance networks.

### 5.4. Investigating a Range of Environments

CUBIC has been extensively studied using simulations, testbed emulations, Internet experiments, and Internet measurements, covering a wide range of network environments [HLRX07] [H16] [CEHRX09] [HR11] [BSCLU13] [LBEWK16]. They have convincingly demonstrated that CUBIC delivers substantial benefits over classical Reno congestion control [RFC5681].

Same as Reno, CUBIC is a loss-based congestion control algorithm. Because CUBIC is designed to be more aggressive (due to a faster window increase function and bigger multiplicative decrease factor) than Reno in fast and long-distance networks, it can fill large drop-tail buffers more quickly than Reno and increases the risk of a standing queue [RFC8511]. In this case, proper queue sizing and management [RFC7567] could be used to mitigate the risk to some extent and reduce the packet queuing delay. Also, in large-BDP

networks after a congestion event, CUBIC, due its cubic window increase function, recovers quickly to the highest link utilization point. This means that link utilization is less sensitive to an active queue management (AQM) target that is lower than the amplitude of the whole sawtooth.

Similar to Reno, the performance of CUBIC as a loss-based congestion control algorithm suffers in networks where a packet loss is not a good indication of bandwidth utilization, such as wireless or mobile networks [[LIU16](#)].

#### [5.5.](#) Protection against Congestion Collapse

With regard to the potential of causing congestion collapse, CUBIC behaves like Reno, since CUBIC modifies only the window adjustment algorithm of Reno. Thus, it does not modify the ACK clocking and timeout behaviors of Reno.

CUBIC also satisfies the "full backoff" requirement as described in [[RFC5033](#)]. After reducing the sending rate to one packet per RTT in response to congestion events due to ECN-Echo ACKs, CUBIC then exponentially increases the transmission timer for each packet retransmission while congestion persists.

#### [5.6.](#) Fairness within the Alternative Congestion Control Algorithm

CUBIC ensures convergence of competing CUBIC flows with the same RTT in the same bottleneck links to an equal throughput. When competing flows have different RTT values, their throughput ratio is linearly proportional to the inverse of their RTT ratios. This is true independently of the level of statistical multiplexing on the link. The convergence time depends on the network environments (e.g., bandwidth, RTT) and the level of statistical multiplexing, as mentioned in [Section 3.4](#).

#### [5.7.](#) Performance with Misbehaving Nodes and Outside Attackers

This is not considered in the current CUBIC design.

#### [5.8.](#) Behavior for Application-Limited Flows

A flow is application-limited if it is currently sending less than what is allowed by the congestion window. This can happen if the flow is limited by either the sender application or the receiver application (via the receiver advertised window) and thus sends less data than what is allowed by the sender's congestion window.

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CUBIC does not increase its congestion window if a flow is application-limited. [Section 4.2](#) requires that `_t_` in Figure 1 does not include application-limited periods, such as idle periods, otherwise `W_cubic(_t_)` might be very high after restarting from these periods.

### [5.9.](#) Responses to Sudden or Transient Events

If there is a sudden increase in capacity, e.g., due to variable radio capacity, a routing change, or a mobility event, CUBIC is designed to utilize the newly available capacity faster than Reno.

On the other hand, if there is a sudden decrease in capacity, CUBIC reduces more slowly than Reno. This remains true whether or not CUBIC is in Reno-friendly mode and whether or not fast convergence is enabled.

### [5.10.](#) Incremental Deployment

CUBIC requires only changes to the congestion control at the sender, and it does not require any changes at receivers. That is, a CUBIC sender works correctly with Reno receivers. In addition, CUBIC does not require any changes to routers and does not require any assistance from routers.

## [6.](#) Security Considerations

CUBIC makes no changes to the underlying security of TCP. More information about TCP security concerns can be found in [\[RFC5681\]](#).

## [7.](#) IANA Considerations

This document does not require any IANA actions.

## [8.](#) References

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## Appendix A. Acknowledgments

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## Appendix B. Evolution of CUBIC

### B.1. Since [draft-ietf-tcpm-rfc8312bis-06](#)

- \* [RFC7661](#) is safe even when cwnd grows beyond rwnd (#143 (<https://github.com/NTAP/rfc8312bis/issues/143>))

### B.2. Since [draft-ietf-tcpm-rfc8312bis-05](#)

- \* Clarify meaning of "application-limited" in [Section 5.8](#) (#137 (<https://github.com/NTAP/rfc8312bis/issues/137>))
- \* Create new subsections for spurious timeouts and spurious loss via ACK (#90 (<https://github.com/NTAP/rfc8312bis/issues/90>))
- \* Brief discussion of convergence in [Section 5.6](#) (#96 (<https://github.com/NTAP/rfc8312bis/issues/96>))
- \* Add more test results to [Section 5](#) and update some references (#91 (<https://github.com/NTAP/rfc8312bis/issues/91>))
- \* Change wording around setting ssthresh (#131 (<https://github.com/NTAP/rfc8312bis/issues/131>))

### B.3. Since [draft-ietf-tcpm-rfc8312bis-04](#)

- \* Fix incorrect math (#106 (<https://github.com/NTAP/rfc8312bis/issues/106>))
- \* Update [RFC5681](#) (#99 (<https://github.com/NTAP/rfc8312bis/issues/99>))

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- \* Rephrase text around algorithmic alternatives, add HyStart++ (#85 (<https://github.com/NTAP/rfc8312bis/issues/85>), #86 (<https://github.com/NTAP/rfc8312bis/issues/86>), #90 (<https://github.com/NTAP/rfc8312bis/issues/90>))
- \* Clarify what we mean by "new ACK" and use it in the text in more places. (#101 (<https://github.com/NTAP/rfc8312bis/issues/101>))
- \* Rewrite the Responses to Sudden or Transient Events section (#98 (<https://github.com/NTAP/rfc8312bis/issues/98>))
- \* Remove confusing text about `_cwnd_start_` in [Section 4.2](#) (#100 (<https://github.com/NTAP/rfc8312bis/issues/100>))
- \* Change terminology from "AIMD" to "Reno" (#108 (<https://github.com/NTAP/rfc8312bis/issues/108>))
- \* Moved MUST NOT from app-limited section to main cubic AI section (#97 (<https://github.com/NTAP/rfc8312bis/issues/97>))
- \* Clarify cwnd decrease during multiplicative decrease (#102 (<https://github.com/NTAP/rfc8312bis/issues/102>))
- \* Clarify text around queuing and slow adaptation of CUBIC in wireless environments (#94 (<https://github.com/NTAP/rfc8312bis/issues/94>))
- \* Set lower bound of cwnd to 1 MSS and use retransmit timer thereafter (#83 (<https://github.com/NTAP/rfc8312bis/issues/83>))
- \* Use FlightSize instead of cwnd to update ssthresh (#114 (<https://github.com/NTAP/rfc8312bis/issues/114>))

#### [B.4.](#) Since [draft-ietf-tcpm-rfc8312bis-03](#)

- \* Remove reference from abstract (#82 (<https://github.com/NTAP/rfc8312bis/pull/82>))

#### [B.5.](#) Since [draft-ietf-tcpm-rfc8312bis-02](#)

- \* Description of packet loss rate `_p_` (#65 (<https://github.com/NTAP/rfc8312bis/issues/65>))

- \* Clarification of TCP Friendly Equation for ABC and Delayed ACK (#66 (<https://github.com/NTAP/rfc8312bis/issues/66>))
- \* add applicability to QUIC and SCTP (#61 (<https://github.com/NTAP/rfc8312bis/issues/61>))

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- \* clarity on setting `alpha__aimd_` to 1 (#68 (<https://github.com/NTAP/rfc8312bis/issues/68>))
- \* introduce `alpha__cubic_` (#64 (<https://github.com/NTAP/rfc8312bis/issues/64>))
- \* clarify `_cwnd_` growth in convex region (#69 (<https://github.com/NTAP/rfc8312bis/issues/69>))
- \* add guidance for using bytes and mention that segments count is decimal (#67 (<https://github.com/NTAP/rfc8312bis/issues/67>))
- \* add loss events detected by RACK and QUIC loss detection (#62 (<https://github.com/NTAP/rfc8312bis/issues/62>))

#### B.6. Since [draft-ietf-tcpm-rfc8312bis-01](#)

- \* address Michael Scharf's editorial suggestions. (#59 (<https://github.com/NTAP/rfc8312bis/issues/59>))
- \* add "Note to the RFC Editor" about removing underscores

#### B.7. Since [draft-ietf-tcpm-rfc8312bis-00](#)

- \* use updated `xml2rfc` with better text rendering of subscripts

#### B.8. Since [draft-eggert-tcpm-rfc8312bis-03](#)

- \* fix spelling nits
- \* rename to [draft-ietf](#)
- \* define `_W_max_` more clearly

#### B.9. Since [draft-eggert-tcpm-rfc8312bis-02](#)

- \* add definition for `segments_acked` and `alpha__aimd_`. (#47 (<https://github.com/NTAP/rfc8312bis/issues/47>))
- \* fix a mistake in `_W_max_` calculation in the fast convergence section. (#51 (<https://github.com/NTAP/rfc8312bis/issues/51>))
- \* clarity on setting `_ssthresh_` and `_cwnd_start_` during multiplicative decrease. (#53 (<https://github.com/NTAP/rfc8312bis/issues/53>))

B.10. Since [draft-eggert-tcpm-rfc8312bis-01](#)

- \* rename TCP-Friendly to AIMD-Friendly and rename Standard TCP to AIMD TCP to avoid confusion as CUBIC has been widely used on the Internet. (#38 (<https://github.com/NTAP/rfc8312bis/issues/38>))
- \* change introductory text to reflect the significant broader deployment of CUBIC on the Internet. (#39 (<https://github.com/NTAP/rfc8312bis/issues/39>))
- \* rephrase introduction to avoid referring to variables that have not been defined yet.

B.11. Since [draft-eggert-tcpm-rfc8312bis-00](#)

- \* acknowledge former co-authors (#15 (<https://github.com/NTAP/rfc8312bis/issues/15>))
- \* prevent `_cwnd_` from becoming less than two (#7 (<https://github.com/NTAP/rfc8312bis/issues/7>))
- \* add list of variables and constants (#5 (<https://github.com/NTAP/rfc8312bis/issues/5>), #6 (<https://github.com/NTAP/rfc8312bis/issues/6>))
- \* update `_K_'s` definition and add bounds for CUBIC `_target_ _cwnd_ [SXEZ19]` (#1 (<https://github.com/NTAP/rfc8312bis/issues/1>), #14 (<https://github.com/NTAP/rfc8312bis/issues/14>))
- \* update `_W_est_` to use AIMD approach (#20 (<https://github.com/NTAP/rfc8312bis/issues/20>))

- \* set `alpha__aimd_` to 1 once `_W_est_` reaches `_W_max_` (#2 (<https://github.com/NTAP/rfc8312bis/issues/2>))
- \* add Vidhi as co-author (#17 (<https://github.com/NTAP/rfc8312bis/issues/17>))
- \* note for Fast Recovery during `_cwnd_` decrease due to congestion event (#11 (<https://github.com/NTAP/rfc8312bis/issues/11>))
- \* add section for spurious congestion events (#23 (<https://github.com/NTAP/rfc8312bis/issues/23>))
- \* initialize `_W_est_` after timeout and remove variable `_W_(last_max)_` (#28 (<https://github.com/NTAP/rfc8312bis/issues/28>))

[B.12.](#) Since [RFC8312](#)

- \* converted to Markdown and xml2rfc v3
- \* updated references (as part of the conversion)
- \* updated author information
- \* various formatting changes
- \* move to Standards Track

[B.13.](#) Since the Original Paper

CUBIC has gone through a few changes since the initial release [[HRX08](#)] of its algorithm and implementation. Below we highlight the differences between its original paper and [[RFC8312](#)].

- \* The original paper [[HRX08](#)] includes the pseudocode of CUBIC implementation using Linux's pluggable congestion control framework, which excludes system-specific optimizations. The simplified pseudocode might be a good source to start with and understand CUBIC.

- \* [HRX08] also includes experimental results showing its performance and fairness.
- \* The definition of `beta__cubic_` constant was changed in [RFC8312]. For example, `beta__cubic_` in the original paper was the window decrease constant while [RFC8312] changed it to CUBIC multiplication decrease factor. With this change, the current congestion window size after a congestion event in [RFC8312] was `beta__cubic_ * _W_max_` while it was `(1-beta__cubic_) * _W_max_` in the original paper.
- \* Its pseudocode used `_W_(last_max)_` while [RFC8312] used `_W_max_`.
- \* Its AIMD-friendly window was `_W_tcp_` while [RFC8312] used `_W_est_`.

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