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# TinyMT32 Pseudo Random Number Generator (PRNG) draft-ietf-tsvwg-tinymt32-01

#### Abstract

This document describes the TinyMT32 Pseudo Random Number Generator (PRNG) that produces 32-bit pseudo-random unsigned integers and aims at having a simple-to-use and deterministic solution. This PRNG is a small-sized variant of Mersenne Twister (MT) PRNG, also designed by M. Saito and M. Matsumoto. The main advantage of TinyMT32 over MT is the use of a small internal state, compatible with most target platforms including embedded devices, while keeping a reasonably good randomness.

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#### 1. Introduction

This document specifies the TinyMT32 PRNG, as a specialization of the reference implementation version 1.1 (2015/04/24) by Mutsuo Saito and Makoto Matsumoto, from Hiroshima University:

- o Official web site: <<u>http://www.math.sci.hiroshima-u.ac.jp/~m-</u> mat/MT/TINYMT/>
- o Official github site and reference implementation: <<u>https://github.com/MersenneTwister-Lab/TinyMT</u>>

This specialisation aims at having a simple-to-use and deterministic PRNG, as explained below.

TinyMT is a new small-sized variant of Mersenne Twister (MT) introduced by Mutsuo Saito and Makoto Matsumoto in 2011. This document focusses on the TinyMT32 variant (rather than TinyMT64) of the PRNG, which outputs 32-bit unsigned integers.

The purpose of TinyMT is not to replace Mersenne Twister: TinyMT has a far shorter period than MT. The merit of TinyMT is in its small size of the internal state of 127 bits, far smaller than 19937 bits of MT. According to statistical tests (BigCrush in TestU01 <a href="http://simul.iro.umontreal.ca/testu01/tu01.html">http://simul.iro.umontreal.ca/testu01/tu01.html</a> and AdaptiveCrush

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<http://www.math.sci.hiroshima-u.ac.jp/~m-mat/MT/ADAPTIVE/>) the
quality of the outputs of TinyMT seems pretty good, taking the small
size of the internal state into consideration. From this point of
view, TinyMT32 represents a major improvement with respect to the
Park-Miler Linear Congruential PRNG (e.g., as specified in
[RFC5170]).

The TinyMT32 PRNG initialization depends, among other things, on a parameter set -- namely (mat1, mat2, tmat) -- that needs to be well chosen (pre-calculated values are available in the official web site). In order to facilitate the use of this PRNG, and unlike the implementation version 1.1 (2015/04/24) by Mutsuo Saito and Makoto Matsumoto, this specification requires the use of a specific parameter set (see <a href="Section 3.1">Section 3.1</a>). The implementation version 1.1 (2015/04/24) also proposes two initialisation functions that differ on the approach to seed the PRNG. A second difference is the removal of the tinymt32\_init\_by\_array() function to keep only the simple initialisation through a single seed value (see <a href="Section 3.2">Section 3.2</a>).

Finally, the determinism of this PRNG, for a given seed, has been carefully checked (see <u>Section 3.3</u>). Indeed, this determinism can be a key requirement as it the case with [<u>RLC-ID</u>] that normatively depends on this specification.

#### 2. Definitions

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in <a href="https://example.com/BCP14">BCP 14 [RFC2119]</a> [RFC8174] when, and only when, they appear in all capitals, as shown here.

#### 3. TinyMT32 PRNG Specification

### 3.1. TinyMT32 Source Code

The TinyMT32 PRNG requires to be initialized with a parameter set that needs to be well chosen. In this specification, for the sake of simplicity, the following parameter set MUST be used:

```
o mat1 = 0x8f7011ee = 2406486510
o mat2 = 0xfc78ff1f = 4235788063
o tmat = 0x3793fdff = 932445695
```

This parameter set is the first entry of the precalculated parameter sets in file tinymt32dc/tinymt32dc.0.1048576.txt, by Kenji Rikitake, and available at <a href="https://github.com/jj1bdx/tinymtdc-longbatch/">https://github.com/jj1bdx/tinymtdc-longbatch/</a>. This is also the parameter set used in [KR12].

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The TinyMT32 PRNG reference implementation is reproduced in Figure 1, with the following differences with respect to the original source code:

- o the original copyright and licence have been removed, in accordance with <u>BCP 78</u> and the IETF Trust's Legal Provisions Relating to IETF Documents (<a href="http://trustee.ietf.org/license-info">http://trustee.ietf.org/license-info</a>);
- o the source code initially spread over the tinymt32.h and tinymt32.c files has been merged;
- o the unused parts of the original source code have been removed. This is the case of the tinymt32\_init\_by\_array() alternative initialisation function;
- o the unused constants TINYMT32\_MEXP and TINYMT32\_MUL have been removed;
- o the appropriate parameter set has been added to the initialization function;
- o the function order has been changed;
- o certain internal variables have been renamed for compactness purposes;
- o the const qualifier has been added to the constant definitions.

```
<CODE BEGINS>
/**
 * Tiny Mersenne Twister only 127 bit internal state.
 * Derived from the reference implementation version 1.1 (2015/04/24)
 * by Mutsuo Saito (Hiroshima University) and Makoto Matsumoto
 * (Hiroshima University).
#include <stdint.h>
/**
 * tinymt32 internal state vector and parameters
typedef struct {
   uint32_t status[4];
   uint32_t mat1;
   uint32_t mat2;
   uint32_t tmat;
} tinymt32_t;
static void tinymt32_next_state (tinymt32_t * s);
static uint32_t tinymt32_temper (tinymt32_t * s);
 * Parameter set to use for this IETF specification. Don't change.
 * This parameter set is the first entry of the precalculated
 * parameter sets in file tinymt32dc/tinymt32dc.0.1048576.txt, by
 * Kenji Rikitake, available at:
```

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```
https://github.com/jj1bdx/tinymtdc-longbatch/
 * It is also the parameter set used:
     Rikitake, K., "TinyMT Pseudo Random Number Generator for
     Erlang", ACM 11th SIGPLAN Erlang Workshop (Erlang'12),
     September, 2012.
const uint32_t TINYMT32_MAT1_PARAM = UINT32_C(0x8f7011ee);
const uint32_t TINYMT32_MAT2_PARAM = UINT32_C(0xfc78ff1f);
const uint32_t TINYMT32_TMAT_PARAM = UINT32_C(0x3793fdff);
 * This function initializes the internal state array with a
 * 32-bit unsigned integer seed.
 * @param s pointer to tinymt internal state.
 * @param seed a 32-bit unsigned integer used as a seed.
 */
void tinymt32_init (tinymt32_t * s, uint32_t seed)
   const uint32_t MIN_LOOP = 8;
   const uint32_t PRE_LOOP = 8;
   s->status[0] = seed;
   s->status[1] = s->mat1 = TINYMT32_MAT1_PARAM;
   s->status[2] = s->mat2 = TINYMT32_MAT2_PARAM;
   s->status[3] = s->tmat = TINYMT32_TMAT_PARAM;
   for (int i = 1; i < MIN_LOOP; i++) {
       s->status[i \& 3] \land = i + UINT32_C(1812433253)
           * (s->status[(i - 1) & 3]
              (s->status[(i-1) & 3] >> 30));
   }
    * NB: the parameter set of this specification warrants
    * that none of the possible 2^^32 seeds leads to an
    * all-zero 127-bit internal state. Therefore, the
     * period_certification() function of the original
     * TinyMT32 source code has been safely removed. If
     * another parameter set is used, this function will
     * have to be re-introduced here.
    * /
   for (int i = 0; i < PRE_LOOP; i++) {
       tinymt32_next_state(s);
   }
}
 * This function outputs a 32-bit unsigned integer from
 * the internal state.
 * @param s pointer to tinymt internal state.
 * @return
             32-bit unsigned integer r (0 <= r < 2^32).
```

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```
*/
uint32_t tinymt32_generate_uint32 (tinymt32_t * s)
{
    tinymt32_next_state(s);
    return tinymt32_temper(s);
}
 * Internal tinymt32 constants and functions.
 * Users should not call these functions directly.
const uint32_t TINYMT32_SH0 = 1;
const uint32_t TINYMT32_SH1 = 10;
const uint32_t TINYMT32_SH8 = 8;
const uint32_t TINYMT32_MASK = UINT32_C(0x7ffffffff);
/**
 * This function changes the internal state of tinymt32.
 * @param s
               pointer to tinymt internal state.
static void tinymt32_next_state (tinymt32_t * s)
{
    uint32_t x;
    uint32_t y;
    y = s->status[3];
    x = (s->status[0] \& TINYMT32_MASK)
        ^ s->status[1]
        ^ s->status[2];
    x \wedge = (x \ll TINYMT32\_SH0);
    y \wedge = (y \gg TINYMT32\_SH0) \wedge x;
    s->status[0] = s->status[1];
    s->status[1] = s->status[2];
    s->status[2] = x \land (y << TINYMT32_SH1);
    s->status[3] = y;
     * The if (y & 1) {...} block below replaces:
           s->status[1] ^= -((int32_t)(y \& 1)) \& s->mat1;
           s->status[2] ^= -((int32_t)(y \& 1)) \& s->mat2;
     * The adopted code is equivalent to the original code
     * but does not depend on the representation of negative
     * integers by 2's complements. It is therefore more
     * portable, but includes an if-branch which may slow
     * down the generation speed.
     */
    if (y & 1) {
         s->status[1] ^= s->mat1;
         s->status[2] ^= s->mat2;
```

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```
}
}
/**
 * This function outputs a 32-bit unsigned integer from
 * the internal state.
 * @param s pointer to tinymt internal state.
 * @return
               32-bit unsigned pseudo-random number.
 */
static uint32_t tinymt32_temper (tinymt32_t * s)
   uint32_t t0, t1;
    t0 = s->status[3];
    t1 = s->status[0] + (s->status[2] >> TINYMT32_SH8);
    t0 = -((int32_t)(t1 \& 1)) \& s->tmat;
    return t0;
}
<CODE ENDS>
```

Figure 1: TinyMT32 Reference Implementation

## 3.2. TinyMT32 Usage

This PRNG MUST first be initialized with the following function:

```
void tinymt32_init (tinymt32_t * s, uint32_t seed);
```

It takes as input a 32-bit unsigned integer used as a seed (note that value 0 is authorized by TinyMT32). This function also takes as input a pointer to an instance of a tinymt32\_t structure that needs to be allocated by the caller but left uninitialized. This structure will then updated by the various TinyMT32 functions in order to keep the internal state of the PRNG. The use of this structure authorizes several instances of this PRNG to be used in parallel, each of them having its own instance of the structure.

Then, each time a new 32-bit pseudo-random unsigned integer between 0 and  $2^32 - 1$  inclusive is needed, the following function is used:

```
uint32_t tinymt32_generate_uint32 (tinymt32_t * s);
```

Of course, the tinymt32\_t structure must be left unchanged by the caller between successive calls to this function.

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## 3.3. Specific Implementation Validation and Deterministic Behavior

PRNG determinism, for a given seed, can be a requirement (e.g., with [RLC-ID]). Consequently, any implementation of the TinyMT32 PRNG in line with this specification MUST comply with the following criteria. Using a seed value of 1, the first 50 values returned by tinymt32\_generate\_uint32(s) as 32-bit unsigned integers MUST be equal to values provided in Figure 2. Note that these values come from the tinymt/check32.out.txt file provided by the PRNG authors to validate implementations of TinyMT32, as part of the MersenneTwister-Lab/TinyMT Github repository.

 2545341989
 981918433
 3715302833
 2387538352
 3591001365

 3820442102
 2114400566
 2196103051
 2783359912
 764534509

 643179475
 1822416315
 881558334
 4207026366
 3690273640

 3240535687
 2921447122
 3984931427
 4092394160
 44209675

 2188315343
 2908663843
 1834519336
 3774670961
 3019990707

 4065554902
 1239765502
 4035716197
 3412127188
 552822483

 161364450
 353727785
 140085994
 149132008
 2547770827

 4064042525
 4078297538
 2057335507
 622384752
 2041665899

 2193913817
 1080849512
 33160901
 662956935
 642999063

 3384709977
 1723175122
 3866752252
 521822317
 2292524454

Figure 2: First 50 decimal values returned by tinymt32\_generate\_uint32(s) as 32-bit unsigned integers, with a seed value of 1.

In particular, the deterministic behavior of the Figure 1 source code has been checked across several platforms: high-end laptops running 64-bits Mac OSX and Linux/Ubuntu; a board featuring a 32-bits ARM Cortex-A15 and running 32-bit Linux/Ubuntu; several embedded cards featuring either an ARM Cortex-M0+, a Cortex-M3 or a Cortex-M4 32-bit microcontroller, all of them running RIOT [Baccelli18]; two low-end embedded cards featuring either a 16-bit microcontroller (TI MSP430) or a 8-bit microcontroller (Arduino ATMEGA2560), both of them running RIOT.

This specification only outputs 32-bit unsigned pseudo-random numbers and does not try to map this output to a smaller integer range (e.g., between 10 and 49 inclusive). If a specific use-case needs such a mapping, it will have to provide its own function. In that case, if PRNG determinism is also required, the use of floating point (single or double precision) to perform this mapping should probably be avoided, these calculations leading potentially to different rounding errors across different target platforms. Great care should also be put on not introducing biases in the randomness of the mapped output (it may be the case with some mapping algorithms) incompatible with

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the use-case requirements. The details of how to perform such a mapping are out-of-scope of this document.

### 4. Security Considerations

The authors do not believe the present specification generates specific security risks per se.

### 5. IANA Considerations

This document does not require any IANA action.

## 6. Acknowledgments

The authors would like to thank Belkacem Teibi with whom we explored TinyMT32 specificities when looking to an alternative to the Park-Miler Linear Congruential PRNG. The authors would like to thank Greg Skinner, the three TSVWG chairs, Wesley Eddy, our shepherd, David Black and Gorry Fairhurst, as well as Spencer Dawkins and Mirja Kuhlewind. Last but not least, the authors are really grateful to the IESG members, in particular Benjamin Kaduk, Eric Rescorla, and Adam Roach for their highly valuable feedbacks that greatly contributed to improve this specification.

## 7. References

## 7.1. Normative References

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Requirement Levels", BCP 14, RFC 2119,
DOI 10.17487/RFC2119, March 1997,
<a href="https://www.rfc-editor.org/info/rfc2119">https://www.rfc-editor.org/info/rfc2119</a>.

[RFC8174] Leiba, B., "Ambiguity of Uppercase vs Lowercase in RFC 2119 Key Words", BCP 14, RFC 8174, DOI 10.17487/RFC8174, May 2017, <a href="https://www.rfc-editor.org/info/rfc8174">https://www.rfc-editor.org/info/rfc8174</a>>.

## 7.2. Informative References

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Baccelli, E., Gundogan, C., Hahm, O., Kietzmann, P., Lenders, M., Petersen, H., Schleiser, K., Schmidt, T., and M. Wahlisch, "RIOT: An Open Source Operating System for Low-End Embedded Devices in the IoT", IEEE Internet of Things Journal (Volume 5, Issue 6), DOI: 10.1109/JIOT.2018.2815038, December 2018.

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- [RLC-ID] Roca, V. and B. Teibi, "Sliding Window Random Linear Code (RLC) Forward Erasure Correction (FEC) Scheme for FECFRAME", Work in Progress, Transport Area Working Group (TSVWG) <a href="mailto:draft-ietf-tsvwg-rlc-fec-scheme">draft-ietf-tsvwg-rlc-fec-scheme</a> (Work in Progress), February 2019, <a href="mailto:https://tools.ietf.org/html/draft-ietf-tsvwg-rlc-fec-scheme">https://tools.ietf.org/html/draft-ietf-tsvwg-rlc-fec-scheme</a>.

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