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**The memory-hard Argon2 password hash and proof-of-work function  
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Abstract

This document describes the Argon2 memory-hard function for password hashing and proof-of-work applications. We provide an implementer-oriented description with test vectors. The purpose is to simplify adoption of Argon2 for Internet protocols. This document is a product of the Crypto Forum Research Group (CFRG) in the IRTF.

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**1. Introduction**

This document describes the Argon2 [[ARGON2ESP](#)] memory-hard function for password hashing and proof-of-work applications. We provide an implementer oriented description with test vectors. The purpose is to simplify adoption of Argon2 for Internet protocols. This document corresponds to version 1.3 of the Argon2 hash function.

Argon2 summarizes the state of the art in the design of memory-hard functions [[HARD](#)]. It is a streamlined and simple design. It aims at the highest memory filling rate and effective use of multiple computing units, while still providing defense against tradeoff attacks. Argon2 is optimized for the x86 architecture and exploits



the cache and memory organization of the recent Intel and AMD processors. Argon2 has one primary variant: Argon2id, and two supplementary variants: Argon2d and Argon2i. Argon2d uses data-dependent memory access, which makes it suitable for cryptocurrencies and proof-of-work applications with no threats from side-channel timing attacks. Argon2i uses data-independent memory access, which is preferred for password hashing and password-based key derivation. Argon2id works as Argon2i for the first half of the first iteration over the memory, and as Argon2d for the rest, thus providing both side-channel attack protection and brute-force cost savings due to time-memory tradeoffs. Argon2i makes more passes over the memory to protect from tradeoff attacks [[AB15](#)].

Argon2 can be viewed as a mode of operation over a fixed-input-length compression function  $G$  and a variable-input-length hash function  $H$ . Even though Argon2 can be potentially used with arbitrary function  $H$ , as long as it provides outputs up to 64 bytes, in this document it MUST be BLAKE2b [[BLAKE2](#)].

For further background and discussion, see the Argon2 paper [[ARGON2](#)].

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [RFC 2119](#) [[RFC2119](#)].

This document represents the consensus of the Crypto Forum Research Group (CFRG).

## 2. Notation and Conventions

$x^y$  --- integer  $x$  multiplied by itself integer  $y$  times

$a*b$  --- multiplication of integer  $a$  and integer  $b$

$c-d$  --- subtraction of integer  $c$  with integer  $d$

$E_f$  --- variable  $E$  with subscript index  $f$

$g / h$  --- integer  $g$  divided by integer  $h$ . The result is rational number

$I(j)$  --- function  $I$  evaluated on integer parameter  $j$

$K || L$  --- string  $K$  concatenated with string  $L$

$a \text{ XOR } b$  --- bitwise exclusive-or between bitstrings  $a$  and  $b$



`a mod b` --- remainder of integer `a` modulo integer `b`, always in range `[0, b-1]`

`a >>> n` --- rotation of 64-bit string `a` to the right by `n` bits

`trunc(a)` --- the 64-bit value, truncated to the 32 least significant bits

`floor(a)` --- the largest integer not bigger than `a`

`ceil(a)` --- the smallest integer not smaller than `a`

`extract(a, i)` --- the `i`-th set of 32-bits from bitstring `a`, starting from 0-th

`|A|` --- the number of elements in set `A`

`LE32(a)` --- 32-bit integer `a` converted to bytestring in little endian. Example: 123456 (decimal) is 40 E2 01 00.

`LE64(a)` --- 64-bit integer `a` converted to bytestring in little endian. Example: 123456 (decimal) is 40 E2 01 00 00 00 00 00.

`int32(s)` --- 32-bit string `s` is converted to non-negative integer in little endian.

`int64(s)` --- 64-bit string `s` is converted to non-negative integer in little endian.

`length(P)` --- the bytelength of string `P` expressed as 32-bit integer

### **3. Argon2 Algorithm**

#### **3.1. Argon2 Inputs and Outputs**

Argon2 has the following input parameters:

- o Message string `P`, which is a password for password hashing applications. MUST have length from 0 to  $2^{(32)} - 1$  bytes.
- o Nonce `S`, which is a salt for password hashing applications. MUST have length not greater than  $2^{(32)}-1$  bytes. 16 bytes is RECOMMENDED for password hashing. Salt SHOULD be unique for each password.
- o Degree of parallelism `p` determines how many independent (but synchronizing) computational chains (lanes) can be run. It MUST be an integer value from 1 to  $2^{(24)}-1$ .



- o Tag length  $T$  MUST be an integer number of bytes from 4 to  $2^{(32)}-1$ .
- o Memory size  $m$  MUST be an integer number of kibibytes from  $8^*p$  to  $2^{(32)}-1$ . The actual number of blocks is  $m'$ , which is  $m$  rounded down to the nearest multiple of  $4^*p$ .
- o Number of iterations  $t$  (used to tune the running time independently of the memory size) MUST be an integer number from 1 to  $2^{(32)}-1$ .
- o Version number  $v$  MUST be one byte  $0x13$ .
- o Secret value  $K$  is OPTIONAL. If used, it MUST have length not greater than  $2^{(32)}-1$  bytes.
- o Associated data  $X$  is OPTIONAL. If used, it MUST have length not greater than  $2^{(32)}-1$  bytes.
- o Type  $y$  of Argon2: MUST be 0 for Argon2d, 1 for Argon2i, 2 for Argon2id.

The Argon2 output, or "tag" is a string  $T$  bytes long.

### **3.2. Argon2 Operation**

Argon2 uses an internal compression function  $G$  with two 1024-byte inputs and a 1024-byte output, and an internal hash function  $H^x()$  with  $x$  being its output length in bytes. Here  $H^x()$  applied to string  $A$  is the BLAKE2b [[BLAKE2](#)] function, which takes  $(d, |dd|, kk=0, nn=x)$  as parameters where  $d$  is  $A$  padded to a multiple of 128 bytes and partitioned into 128-byte blocks. The compression function  $G$  is based on its internal permutation. A variable-length hash function  $H'$  built upon  $H$  is also used.  $G$  is described in [Section 3.5](#) and  $H'$  is described in [Section 3.3](#).

The Argon2 operation is as follows.

1. Establish  $H_0$  as the 64-byte value as shown below.

$$\begin{aligned}
 H_0 = & H^{(64)}(\text{LE32}(p) \parallel \text{LE32}(T) \parallel \text{LE32}(m) \parallel \text{LE32}(t) \parallel \\
 & \text{LE32}(v) \parallel \text{LE32}(y) \parallel \text{LE32}(\text{length}(P)) \parallel P \parallel \\
 & \text{LE32}(\text{length}(S)) \parallel S \parallel \text{LE32}(\text{length}(K)) \parallel K \parallel \\
 & \text{LE32}(\text{length}(X)) \parallel X)
 \end{aligned}$$

$H_0$  generation





2. Allocate the memory as  $m'$  1024-byte blocks where  $m'$  is derived as:

$$m' = 4 * p * \text{floor}(m / 4p)$$

#### Memory allocation

For  $p$  lanes, the memory is organized in a matrix  $B[i][j]$  of blocks with  $p$  rows (lanes) and  $q = m' / p$  columns.

3. Compute  $B[i][0]$  for all  $i$  ranging from (and including) 0 to (not including)  $p$ .

$$B[i][0] = H^{(128)}(H_0 \parallel \text{LE32}(0) \parallel \text{LE32}(i))$$

#### Lane starting blocks

4. Compute  $B[i][1]$  for all  $i$  ranging from (and including) 0 to (not including)  $p$ .

$$B[i][1] = H^{(128)}(H_0 \parallel \text{LE32}(1) \parallel \text{LE32}(i))$$

#### Second lane blocks

5. Compute  $B[i][j]$  for all  $i$  ranging from (and including) 0 to (not including)  $p$ , and for all  $j$  ranging from (and including) 2 to (not including)  $q$ . The block indices  $l$  and  $z$  are determined for each  $i, j$  differently for Argon2d, Argon2i, and Argon2id (Section [Section 3.4](#)).

$$B[i][j] = G(B[i][j-1], B[l][z])$$

#### Further block generation

6. If the number of iterations  $t$  is larger than 1, we repeat the steps however replacing the computations with the following expression:

$$\begin{aligned} B[i][0] &= G(B[i][q-1], B[l][z]) \\ B[i][j] &= G(B[i][j-1], B[l][z]) \end{aligned}$$

#### Further passes

7. After  $t$  steps have been iterated, the final block  $C$  is computed as the XOR of the last column:



$$C = B[0][q-1] \text{ XOR } B[1][q-1] \text{ XOR } \dots \text{ XOR } B[p-1][q-1]$$

Final block

8. The output tag is computed as  $H'^{\wedge T}(C)$ .

**3.3. Variable-length hash function  $H'$**

Let  $V_i$  be a 64-byte block, and  $W_i$  be its first 32 bytes. Then we define:

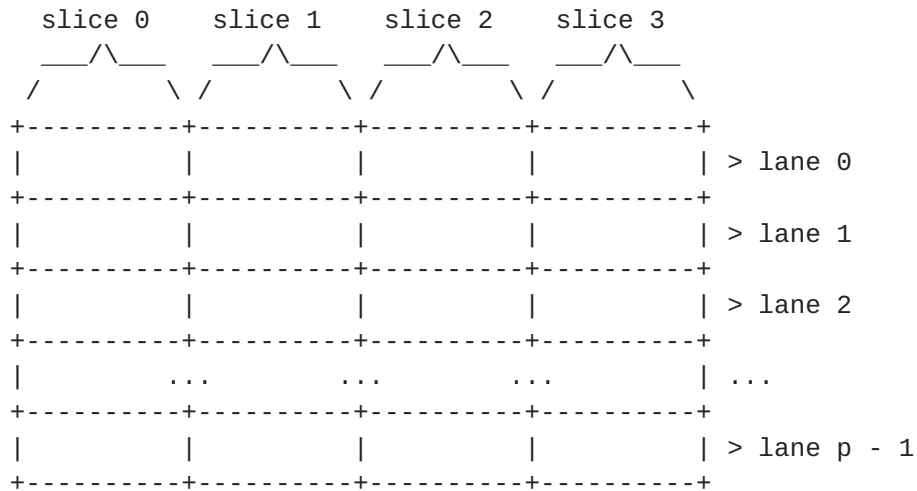
```

if T <= 64
    H'^{\wedge T}(A) = H^{\wedge T}(LE32(T)||A)
else
    r = ceil(T/32)-2
    V_1 = H^{\wedge(64)}(LE32(T)||A)
    V_2 = H^{\wedge(64)}(V_1)
    ...
    V_r = H^{\wedge(64)}(V_{r-1})
    V_{r+1} = H^{\wedge(T-32*r)}(V_r)
    H'^{\wedge T}(X) = W_1 || W_2 || ... || W_r || V_{r+1}
    
```

Tag computation

**3.4. Indexing**

To enable parallel block computation, we further partition the memory matrix into  $S = 4$  vertical slices. The intersection of a slice and a lane is a segment of length  $q/S$ . Segments of the same slice can be computed in parallel and do not reference blocks from each other. All other blocks can be referenced.



Single-pass Argon2 with p lanes and 4 slices



### **3.4.1. Getting the 32-bit values J\_1 and J\_2**

#### **3.4.1.1. Argon2d**

J\_1 is given by the first 32 bits of block B[i][j-1], while J\_2 is given by the next 32-bits of block B[i][j-1]:

```
J_1 = int32(extract(B[i][j-1], 1))
J_2 = int32(extract(B[i][j-1], 2))
```

Deriving J1,J2 in Argon2d

#### **3.4.1.2. Argon2i**

Each application of the 2-round compression function G in the counter mode gives 128 64-bit values X, which are viewed as X1||X2 and converted to J\_1=int32(X1) and J\_2=int32(X2). The first input to G is the all zero block and the second input to G is constructed as follows:

```
( LE64(r) || LE64(l) || LE64(s) || LE64(m') ||
  LE64(t) || LE64(y) || LE64(i) || ZERO ), where
```

```
r -- the pass number
l -- the lane number
s -- the slice number
m' -- the total number of memory blocks
t -- the total number of passes
y -- the Argon2 type (0 for Argon2d,
                    1 for Argon2i, 2 for Argon2id)
i -- the counter (starts from 1 in each segment)
ZERO -- the 968-byte zero string.
```

Input to compute J1,J2 in Argon2i

The values r, l, s, m', t, x, i are represented as 8 bytes in little-endian.

#### **3.4.1.3. Argon2id**

If the pass number is 0 and the slice number is 0 or 1, then compute J\_1 and J\_2 as for Argon2i, else compute J\_1 and J\_2 as for Argon2d.

### **3.4.2. Mapping J\_1 and J\_2 to reference block index**

The value of  $l = J_2 \bmod p$  gives the index of the lane from which the block will be taken. For the first pass ( $r=0$ ) and the first slice ( $s=0$ ) the block is taken from the current lane.



The set  $W$  contains the indices that can be referenced according to the following rules:

1. If  $l$  is the current lane, then  $W$  includes the indices of all blocks in the last  $S - 1 = 3$  segments computed and finished, as well as the blocks computed in the current segment in the current pass excluding  $B[i][j-1]$ .
2. If  $l$  is not the current lane, then  $W$  includes the indices of all blocks in the last  $S - 1 = 3$  segments computed and finished in lane  $l$ . If  $B[i][j]$  is the first block of a segment, then the very last index from  $W$  is excluded.

We are going to take a block from  $W$  with a non-uniform distribution over  $[0, |W|)$  using the mapping

$$J_1 \rightarrow |W|(1 - J_1^2 / 2^{64})$$

Computing  $J_1$

To avoid floating point computation, the following approximation is used:

$$\begin{aligned} x &= J_1^2 / 2^{32} \\ y &= (|W| * x) / 2^{32} \\ z &= |W| - 1 - y \end{aligned}$$

Computing  $J_1$ , part 2

The value of  $z$  gives the reference block index in  $W$ .

### **3.5. Compression function $G$**

Compression function  $G$  is built upon the BLAKE2b round function  $P$ .  $P$  operates on the 128-byte input, which can be viewed as 8 16-byte registers:

$$P(A_0, A_1, \dots, A_7) = (B_0, B_1, \dots, B_7)$$

Blake round function  $P$

Compression function  $G(X, Y)$  operates on two 1024-byte blocks  $X$  and  $Y$ . It first computes  $R = X \text{ XOR } Y$ . Then  $R$  is viewed as a  $8 \times 8$  matrix of 16-byte registers  $R_0, R_1, \dots, R_{63}$ . Then  $P$  is first applied to each row, and then to each column to get  $Z$ :





```

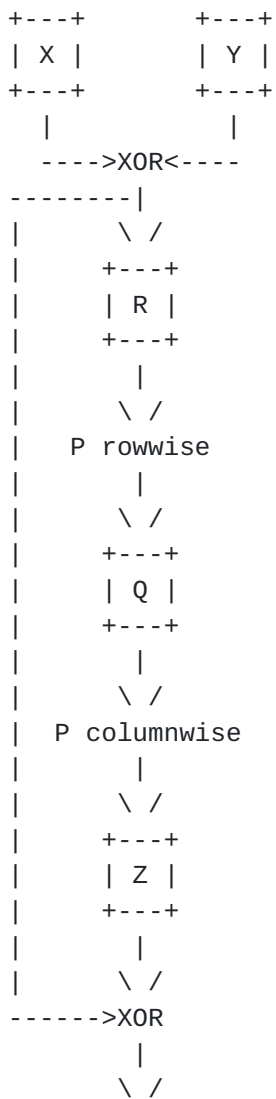
(Q_0, Q_1, Q_2, ... , Q_7) <- P( R_0, R_1, R_2, ... , R_7)
(Q_8, Q_9, Q_10, ... , Q_15) <- P( R_8, R_9, R_10, ... , R_15)
...
(Q_56, Q_57, Q_58, ... , Q_63) <- P(R_56, R_57, R_58, ... , R_63)
(Z_0, Z_8, Z_16, ... , Z_56) <- P( Q_0, Q_8, Q_16, ... , Q_56)
(Z_1, Z_9, Z_17, ... , Z_57) <- P( Q_1, Q_9, Q_17, ... , Q_57)
...
(Z_7, Z_15, Z_23, ... , Z_63) <- P( Q_7, Q_15, Q_23, ... , Q_63)

```

Core of compression function G

Finally, G outputs Z XOR R:

G: (X, Y) -> R -> Q -> Z -> Z XOR R



Argon2 compression function G.



### 3.6. Permutation P

Permutation P is based on the round function of BLAKE2b. The 8 16-byte inputs  $S_0, S_1, \dots, S_7$  are viewed as a 4x4 matrix of 64-bit words, where  $S_i = (v_{\{2*i+1\}} || v_{\{2*i\}})$ :

```
v_0  v_1  v_2  v_3
v_4  v_5  v_6  v_7
v_8  v_9 v_10 v_11
v_12 v_13 v_14 v_15
```

Matrix element labeling

It works as follows:

```
GB(v_0, v_4, v_8, v_12)
GB(v_1, v_5, v_9, v_13)
GB(v_2, v_6, v_10, v_14)
GB(v_3, v_7, v_11, v_15)

GB(v_0, v_5, v_10, v_15)
GB(v_1, v_6, v_11, v_12)
GB(v_2, v_7, v_8, v_13)
GB(v_3, v_4, v_9, v_14)
```

Feeding matrix elements to GB

GB(a, b, c, d) is defined as follows:

```
a = (a + b + 2 * trunc(a) * trunc(b)) mod 2^(64)
d = (d XOR a) >>> 32
c = (c + d + 2 * trunc(c) * trunc(d)) mod 2^(64)
b = (b XOR c) >>> 24

a = (a + b + 2 * trunc(a) * trunc(b)) mod 2^(64)
d = (d XOR a) >>> 16
c = (c + d + 2 * trunc(c) * trunc(d)) mod 2^(64)
b = (b XOR c) >>> 63
```

Details of GB

The modular additions in GB are combined with 64-bit multiplications. Multiplications are the only difference to the original BLAKE2b design. This choice is done to increase the circuit depth and thus the running time of ASIC implementations, while having roughly the same running time on CPUs thanks to parallelism and pipelining.



#### **4. Parameter Choice**

Argon2d is optimized for settings where the adversary does not get regular access to system memory or CPU, i.e. he can not run side-channel attacks based on the timing information, nor he can recover the password much faster using garbage collection. These settings are more typical for backend servers and cryptocurrency minings. For practice we suggest the following settings:

- o Cryptocurrency mining, that takes 0.1 seconds on a 2 Ghz CPU using 1 core -- Argon2d with 2 lanes and 250 MB of RAM.

Argon2id is optimized for more realistic settings, where the adversary possibly can access the same machine, use its CPU or mount cold-boot attacks. We suggest the following settings:

- o Backend server authentication, that takes 0.5 seconds on a 2 GHz CPU using 4 cores -- Argon2id with 8 lanes and 4 GiB of RAM.
- o Key derivation for hard-drive encryption, that takes 3 seconds on a 2 GHz CPU using 2 cores - Argon2id with 4 lanes and 6 GiB of RAM.
- o Frontend server authentication, that takes 0.5 seconds on a 2 GHz CPU using 2 cores - Argon2id with 4 lanes and 1 GiB of RAM.

We recommend the following procedure to select the type and the parameters for practical use of Argon2.

1. Select the type  $y$ . If you do not know the difference between them or you consider side-channel attacks as viable threat, choose Argon2id.
2. Figure out the maximum number  $h$  of threads that can be initiated by each call to Argon2.
3. Figure out the maximum amount  $m$  of memory that each call can afford.
4. Figure out the maximum amount  $x$  of time (in seconds) that each call can afford.
5. Select the salt length. 128 bits is sufficient for all applications, but can be reduced to 64 bits in the case of space constraints.



- 6. Select the tag length. 128 bits is sufficient for most applications, including key derivation. If longer keys are needed, select longer tags.
- 7. If side-channel attacks are a viable threat, or if you're uncertain, enable the memory wiping option in the library call.
- 8. Run the scheme of type y, memory m and h lanes and threads, using different number of passes t. Figure out the maximum t such that the running time does not exceed x. If it exceeds x even for t = 1, reduce m accordingly.
- 9. Hash all the passwords with the just determined values m, h, and t.

**5. Test Vectors**

This section contains test vectors for Argon2.

**5.1. Argon2d Test Vectors**

We provide test vectors with complete outputs (tags). For the convenience of developers, we also provide some interim variables, concretely, first and last memory blocks of each pass.

```

=====
Argon2d version number 19
=====
Memory: 32 KiB
Iterations: 3
Parallelism: 4 lanes
Tag length: 32 bytes
Password[32]: 01 01 01 01 01 01 01 01
              01 01 01 01 01 01 01 01
              01 01 01 01 01 01 01 01
              01 01 01 01 01 01 01 01
Salt[16]: 02 02 02 02 02 02 02 02 02 02 02 02 02 02 02 02
Secret[8]: 03 03 03 03 03 03 03 03
Associated data[12]: 04 04 04 04 04 04 04 04 04 04 04 04
Pre-hashing digest: b8 81 97 91 a0 35 96 60
                   bb 77 09 c8 5f a4 8f 04
                   d5 d8 2c 05 c5 f2 15 cc
                   db 88 54 91 71 7c f7 57
                   08 2c 28 b9 51 be 38 14
                   10 b5 fc 2e b7 27 40 33
                   b9 fd c7 ae 67 2b ca ac
                   5d 17 90 97 a4 af 31 09

```





After pass 0:

```

Block 0000 [ 0]: db2fea6b2c6f5c8a
Block 0000 [ 1]: 719413be00f82634
Block 0000 [ 2]: a1e3f6dd42aa25cc
Block 0000 [ 3]: 3ea8efd4d55ac0d1
...
Block 0031 [124]: 28d17914aea9734c
Block 0031 [125]: 6a4622176522e398
Block 0031 [126]: 951aa08aeecb2c05
Block 0031 [127]: 6a6c49d2cb75d5b6

```

After pass 1:

```

Block 0000 [ 0]: d3801200410f8c0d
Block 0000 [ 1]: 0bf9e8a6e442ba6d
Block 0000 [ 2]: e2ca92fe9c541fcc
Block 0000 [ 3]: 6269fe6db177a388
...
Block 0031 [124]: 9eacfcfbdb3ce0fc
Block 0031 [125]: 07dedaeb0aee71ac
Block 0031 [126]: 074435fad91548f4
Block 0031 [127]: 2dbfff23f31b5883

```

After pass 2:

```

Block 0000 [ 0]: 5f047b575c5ff4d2
Block 0000 [ 1]: f06985dbf11c91a8
Block 0000 [ 2]: 89efb2759f9a8964
Block 0000 [ 3]: 7486a73f62f9b142
...
Block 0031 [124]: 57cfb9d20479da49
Block 0031 [125]: 4099654bc6607f69
Block 0031 [126]: f142a1126075a5c8
Block 0031 [127]: c341b3ca45c10da5
Tag: 51 2b 39 1b 6f 11 62 97
     53 71 d3 09 19 73 42 94
     f8 68 e3 be 39 84 f3 c1
     a1 3a 4d b9 fa be 4a cb

```

**5.2. Argon2i Test Vectors**

```

=====
Argon2i version number 19
=====

Memory: 32 KiB
Iterations: 3
Parallelism: 4 lanes
Tag length: 32 bytes
Password[32]: 01 01 01 01 01 01 01 01
              01 01 01 01 01 01 01 01

```



```

01 01 01 01 01 01 01 01
01 01 01 01 01 01 01 01
Salt[16]: 02 02 02 02 02 02 02 02 02 02 02 02 02 02 02 02
Secret[8]: 03 03 03 03 03 03 03 03
Associated data[12]: 04 04 04 04 04 04 04 04 04 04 04 04
Pre-hashing digest: c4 60 65 81 52 76 a0 b3
                    e7 31 73 1c 90 2f 1f d8
                    0c f7 76 90 7f bb 7b 6a
                    5c a7 2e 7b 56 01 1f ee
                    ca 44 6c 86 dd 75 b9 46
                    9a 5e 68 79 de c4 b7 2d
                    08 63 fb 93 9b 98 2e 5f
                    39 7c c7 d1 64 fd da a9

```

After pass 0:

```

Block 0000 [ 0]: f8f9e84545db08f6
Block 0000 [ 1]: 9b073a5c87aa2d97
Block 0000 [ 2]: d1e868d75ca8d8e4
Block 0000 [ 3]: 349634174e1aebcc
...
Block 0031 [124]: 975f596583745e30
Block 0031 [125]: e349bdd7edeb3092
Block 0031 [126]: b751a689b7a83659
Block 0031 [127]: c570f2ab2a86cf00

```

After pass 1:

```

Block 0000 [ 0]: b2e4ddfcf76dc85a
Block 0000 [ 1]: 4ffd0626c89a2327
Block 0000 [ 2]: 4af1440fff212980
Block 0000 [ 3]: 1e77299c7408505b
...
Block 0031 [124]: e4274fd675d1e1d6
Block 0031 [125]: 903fffb7c4a14c98
Block 0031 [126]: 7e5db55def471966
Block 0031 [127]: 421b3c6e9555b79d

```

After pass 2:

```

Block 0000 [ 0]: af2a8bd8482c2f11
Block 0000 [ 1]: 785442294fa55e6d
Block 0000 [ 2]: 9256a768529a7f96
Block 0000 [ 3]: 25a1c1f5bb953766
...
Block 0031 [124]: 68cf72fccc7112b9
Block 0031 [125]: 91e8c6f8bb0ad70d
Block 0031 [126]: 4f59c8bd65cbb765
Block 0031 [127]: 71e436f035f30ed0
Tag: c8 14 d9 d1 dc 7f 37 aa
    13 f0 d7 7f 24 94 bd a1

```



c8 de 6b 01 6d d3 88 d2  
99 52 a4 c4 67 2b 6c e8

**5.3. Argon2id Test Vectors**

```

=====
Argon2id version number 19
=====
Memory: 32 KiB, Iterations: 3,
Parallelism: 4 lanes, Tag length: 32 bytes
Password[32]: 01 01 01 01 01 01 01 01 01 01 01 01 01 01 01 01
01 01 01 01 01 01 01 01 01 01 01 01 01 01 01 01
Salt[16]: 02 02 02 02 02 02 02 02 02 02 02 02 02 02 02 02
Secret[8]: 03 03 03 03 03 03 03 03
Associated data[12]: 04 04 04 04 04 04 04 04 04 04 04 04
Pre-hashing digest: 28 89 de 48 7e b4 2a e5 00 c0 00 7e d9 25 2f
10 69 ea de c4 0d 57 65 b4 85 de 6d c2 43 7a 67 b8 54 6a 2f 0a
cc 1a 08 82 db 8f cf 74 71 4b 47 2e 94 df 42 1a 5d a1 11 2f fa
11 43 43 70 a1 e9 97

```

```

After pass 0:
Block 0000 [ 0]: 6b2e09f10671bd43
Block 0000 [ 1]: f69f5c27918a21be
Block 0000 [ 2]: dea7810ea41290e1
Block 0000 [ 3]: 6787f7171870f893
...
Block 0031 [124]: 377fa81666dc7f2b
Block 0031 [125]: 50e586398a9c39c8
Block 0031 [126]: 6f732732a550924a
Block 0031 [127]: 81f88b28683ea8e5

```

```

After pass 1:
Block 0000 [ 0]: 3653ec9d01583df9
Block 0000 [ 1]: 69ef53a72d1e1fd3
Block 0000 [ 2]: 35635631744ab54f
Block 0000 [ 3]: 599512e96a37ab6e
...
Block 0031 [124]: 4d4b435cea35caa6
Block 0031 [125]: c582210d99ad1359
Block 0031 [126]: d087971b36fd6d77
Block 0031 [127]: a55222a93754c692

```

```

After pass 2:
Block 0000 [ 0]: 942363968ce597a4
Block 0000 [ 1]: a22448c0bdad5760
Block 0000 [ 2]: a5f80662b6fa8748
Block 0000 [ 3]: a0f9b9ce392f719f
...

```



Block 0031 [124]: d723359b485f509b  
Block 0031 [125]: cb78824f42375111  
Block 0031 [126]: 35bc8cc6e83b1875  
Block 0031 [127]: 0b012846a40f346a  
Tag: 0d 64 0d f5 8d 78 76 6c 08 c0 37 a3 4a 8b 53 c9 d0  
1e f0 45 2d 75 b6 5e b5 25 20 e9 6b 01 e6 59

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## **7. IANA Considerations**

None.

## **8. Security Considerations**

### **8.1. Security as hash function and KDF**

The collision and preimage resistance levels of Argon2 are equivalent to those of the underlying BLAKE2b hash function. To produce a collision,  $2^{256}$  inputs are needed. To find a preimage,  $2^{512}$  inputs must be tried.

The KDF security is determined by the key length and the size of the internal state of hash function  $H'$ . To distinguish the output of keyed Argon2 from random, minimum of  $(2^{128}, 2^{\text{length}(K)})$  calls to BLAKE2b are needed.

### **8.2. Security against time-space tradeoff attacks**

Time-space tradeoffs allow computing a memory-hard function storing fewer memory blocks at the cost of more calls to the internal compression function. The advantage of tradeoff attacks is measured in the reduction factor to the time-area product, where memory and extra compression function cores contribute to the area, and time is increased to accommodate the recomputation of missed blocks. A high reduction factor may potentially speed up preimage search.

The best known attacks on the 1-pass and 2-pass Argon2i is the low-storage attack described in [CBS16], which reduces the time-area product (using the peak memory value) by the factor of 5. The best attack on 3-pass and more Argon2i is [AB16] with reduction factor being a function of memory size and the number of passes. For 1





gibibyte of memory: 3 for 3 passes, 2.5 for 4 passes, 2 for 6 passes. The reduction factor grows by about 0.5 with every doubling the memory size. To completely prevent time-space tradeoffs from [AB16], the number of passes MUST exceed binary logarithm of memory minus 26. Asymptotically, the best attack on 1-pass Argon2i is given in [BZ17] with maximal advantage of the adversary upper bounded by  $O(m^{0.233})$  where  $m$  is the number of blocks. This attack is also asymptotically optimal as [BZ17] also prove the upper bound on any attack of  $O(m^{0.25})$ .

The best tradeoff attack on  $t$ -pass Argon2d is the ranking tradeoff attack, which reduces the time-area product by the factor of 1.33.

The best attack on Argon2id can be obtained by complementing the best attack on the 1-pass Argon2i with the best attack on a multi-pass Argon2d. Thus the best tradeoff attack on 1-pass Argon2id is the combined low-storage attack (for the first half of the memory) and the ranking attack (for the second half), which bring together the factor of about 2.1. The best tradeoff attack on  $t$ -pass Argon2id is the ranking tradeoff attack, which reduces the time-area product by the factor of 1.33.

### **8.3. Security for time-bounded defenders**

A bottleneck in a system employing the password-hashing function is often the function latency rather than memory costs. A rational defender would then maximize the bruteforce costs for the attacker equipped with a list of hashes, salts, and timing information, for fixed computing time on the defender's machine. The attack cost estimates from [AB16] imply that for Argon2i, 3 passes is almost optimal for the most of reasonable memory sizes, and that for Argon2d and Argon2id, 1 pass maximizes the attack costs for the constant defender time.

### **8.4. Recommendations**

The Argon2id variant with  $t=1$  and maximum available memory is RECOMMENDED as a default setting for all environments. This setting is secure against side-channel attacks and maximizes adversarial costs on dedicated bruteforce hardware.

## **9. References**

### **9.1. Normative References**



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