The scrypt Password-Based Key Derivation Function
draft-josefsson-scrypt-kdf-03

Abstract

This document specifies the password-based key derivation function scrypt. The function derives one or more secret keys from a secret string. It is based on memory-hard functions which offer added protection against attacks using custom hardware. The document also provides an ASN.1 schema.

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1. Introduction

Password-based key derivation functions are used in cryptography for deriving one or more secret keys from a secret value. Over the years, several password-based key derivation functions have been used, including the original DES-based UNIX Crypt-function, FreeBSD MD5 crypt, PKCS#5 PBKDF2 [RFC2898] (typically used with SHA-1), GNU SHA-256/512 crypt, Windows NT LAN Manager (NTLM) hash, and the Blowfish-based bcrypt. These algorithms are based on similar techniques that employ a cryptographic primitive, salting and/or iteration. The iteration count is used to slow down the computation.

Providing that the number of iterations used is increased as computer systems get faster, this allows legitimate users to spend a constant amount of time on key derivation without losing ground to an attackers' ever-increasing computing power - as long as attackers are limited to the same software implementations as legitimate users. However, as Bernstein pointed out in the context of integer factorization, while parallelized hardware implementations may not change the number of operations performed compared to software implementations, this does not prevent them from dramatically
changing the asymptotic cost, since in many contexts - including the embarrassingly parallel task of performing a brute-force search for a passphrase - dollar-seconds are the most appropriate units for measuring the cost of a computation. As semiconductor technology develops, circuits do not merely become faster; they also become smaller, allowing for a larger amount of parallelism at the same cost. Consequently, existing key derivation algorithms, even when the iteration count is increased so that the time taken to verify a password remains constant, the cost of finding a password by using a brute force attack implemented in hardware drops each year.

The scrypt function aims to reduce the advantage which attackers can gain by using custom-designed parallel circuits for breaking password-based key derivation functions.

For further background, see the original scrypt paper [SCRYP].

The rest of this document is divided into sections that each describe algorithms needed for the final "scrypt" algorithm.

2. The Salsa20/8 Core Function

Salsa20/8 Core is a round-reduced variant of the Salsa20 Core. It is a hash function from 64-octet strings to 64-octet strings. Note that Salsa20/8 Core is not a cryptographic hash function since it is not collision-resistant. See section 8 of [SALSA20SPEC] for its specification, and [SALSA20CORE] for more information.

3. The scryptBlockMix Algorithm

The scryptBlockMix algorithm is the same as the BlockMix algorithm described in [SCRYP] but with Salsa20/8 Core used as the hash function H. Below, Salsa(T) corresponds to the Salsa20/8 Core function applied to the octet vector T.
Algorithm scryptBlockMix

Parameters:

   r       Block size parameter.

Input:

   B[0], ..., B[2 * r - 1]
     Input vector of 2 * r 64-octet blocks.

Output:

   B'[0], ..., B'[2 * r - 1]
     Output vector of 2 * r 64-octet blocks.

Steps:

1. X = B[2 * r - 1]

2. for i = 0 to 2 * r - 1 do
   T = X xor B[i]
   X = Salsa (T)
   Y[i] = X
end for

3. B' = (Y[0], Y[2], ..., Y[2 * r - 2],
        Y[1], Y[3], ..., Y[2 * r - 1])

4. **The scryptROMix Algorithm**

   The scryptROMix algorithm is the same as the ROMix algorithm described in [SCRYPT] but with scryptBlockMix used as the hash function H and the Integerify function explained inline.
Algorithm scryptROMix

Input:
- \( r \) Block size parameter.
- \( B \) Input octet vector of length 128 * \( r \) octets.
- \( N \) CPU/Memory cost parameter, must be larger than 1, a power of 2 and less than \( 2^{(128 \times r / 8)} \).

Output:
- \( B' \) Output octet vector of length 128 * \( r \) octets.

Steps:

1. \( X = B \)

2. for \( i = 0 \) to \( N - 1 \) do
   - \( V[i] = X \)
   - \( X = \text{scryptBlockMix} (X) \)
   end for

3. for \( i = 0 \) to \( N - 1 \) do
   - \( j = \text{Integerify} (X) \mod N \)
   - where \( \text{Integerify} (B[0] \ldots B[2 \times r - 1]) \) is defined as the result of interpreting \( B[2 \times r - 1] \) as a little-endian integer.
   - \( T = X \oplus V[j] \)
   - \( X = \text{scryptBlockMix} (T) \)
   end for

4. \( B' = X \)

5. **The scrypt Algorithm**

The PBKDF2-HMAC-SHA-256 function used below denote the PBKDF2 algorithm [RFC2898] used with HMAC-SHA-256 [RFC6234] as the PRF. The HMAC-SHA-256 function generates 32 octet outputs.
Algorithm scrypt

Input:

- $P$  Passphrase, an octet string.
- $S$  Salt, an octet string.
- $N$  CPU/Memory cost parameter, must be larger than 1, a power of 2 and less than $2^{(128 \cdot r / 8)}$.
- $r$  Block size parameter.
- $p$  Parallelization parameter, a positive integer less than or equal to $((2^{32}-1) \cdot hLen) / MFLen$ where $hLen$ is 32 and $MFLen$ is $128 \cdot r$.
- $dkLen$  Intended output length in octets of the derived key; a positive integer less than or equal to $(2^{32} - 1) \cdot hLen$ where $hLen$ is 32.

Output:

- $DK$  Derived key, of length $dkLen$ octets.

Steps:

1. $B[0] \parallel B[1] \parallel \ldots \parallel B[p - 1] = \text{PBKDF2-HMAC-SHA256} (P, S, 1, p \cdot 128 \cdot r)$

2. for $i = 0$ to $p - 1$
   
   $B[i] = \text{scryptROMix} (r, B[i], N)$
   
end for

3. $DK = \text{PBKDF2-HMAC-SHA256} (P, B[0] \parallel B[1] \parallel \ldots \parallel B[p - 1], 1, dkLen)$

6. ASN.1 Syntax

This section defines ASN.1 syntax for the scrypt key derivation function. This is intended to operate on the same abstraction level as PKCS#5's PBKDF2. The OID id-scrypt below can be used where id-PBKDF2 is used, with scrypt-params corresponding to PBKDF2-params. The intended application of these definitions includes PKCS #8 and other syntax for key management.

The object identifier id-scrypt identifies the scrypt key derivation function.

$id$-scrypt OBJECT IDENTIFIER ::= {1 3 6 1 4 1 11591 4 11}

The parameters field associated with this OID in an AlgorithmIdentifier shall have type scrypt-params:
scrypt-params ::= SEQUENCE {
    salt OCTET STRING,
    costParameter INTEGER (1..MAX),
    blockSize INTEGER (1..MAX),
    parallelizationParameter INTEGER (1..MAX),
    keyLength INTEGER (1..MAX) OPTIONAL }

The fields of type scrypt-params have the following meanings:

- salt specifies the salt value. It shall be an octet string.
- costParameter specifies the CPU/Memory cost parameter N.
- blockSize specifies the block size parameter r.
- parallelizationParameter specifies the parallelization parameter.
- keyLength, an optional field, is the length in octets of the derived key. The maximum key length allowed depends on the implementation; it is expected that implementation profiles may further constrain the bounds. This field only provides convenience; the key length is not cryptographically protected.

To be usable in PKCS#8 [RFC5208] and Asymmetric Key Packages [RFC5958] the following extension of the PBES2-KDFs type is needed.

PBES2-KDFs ALGORITHM-IDENTIFIER ::= 
    { {scrypt-params IDENTIFIED BY id-scrypt}, ... }

6.1.  ASN.1 Module

For reference purposes, the ASN.1 syntax is presented as an ASN.1 module here.
-- scrypt ASN.1 Module

scrypt-0 {1 3 6 1 4 1 11591 4 10}

DEFINITIONS ::= BEGIN

id-scrypt OBJECT IDENTIFIER ::= {1 3 6 1 4 1 11591 4 11}

scrypt-params ::= SEQUENCE {
    salt OCTET STRING,
    costParameter INTEGER (1..MAX),
    blockSize INTEGER (1..MAX),
    parallelizationParameter INTEGER (1..MAX),
    keyLength INTEGER (1..MAX) OPTIONAL
}

PBES2-KDFs ALGORITHM-IDENTIFIER ::= {
    {scrypt-params IDENTIFIED BY id-scrypt}, ...
}

END

7. Test Vectors for Salsa20/8 Core

Below is a sequence of octets to illustrate input and output values for the Salsa20/8 Core. The octets are hex encoded and whitespace is inserted for readability. The value corresponds to the first input and output pair generated by the first scrypt test vector below.

INPUT:
7e 87 9a 21 4f 3e c9 86 7c a9 40 e6 41 71 8f 26
ba ee 55 5b 8c 61 c1 b5 0d f8 46 11 6d cd 3b 1d
ee 24 f3 19 df 9b 3d 85 14 12 1e 4b 5a c5 aa 32
76 02 1d 29 09 c7 48 29 ed eb c6 8d b8 b8 c2 5e

OUTPUT:
a4 1f 85 9c 66 08 cc 99 3b 81 ca cb 02 0c ef 05
04 4b 21 81 a2 fd 33 7d fd 7b 1c 63 96 68 2f 29
b4 39 31 68 e3 c9 e6 bc fe 6b c5 b7 a0 6d 96 ba
e4 24 cc 10 2c 91 74 5c 24 ad 67 3d c7 61 8f 81

8. Test Vectors for scryptBlockMix

Below is a sequence of octets to illustrate input and output values for scryptBlockMix. The test vector uses an r value of 1. The octets are hex encoded and whitespace is inserted for readability. The value corresponds to the first input and output pair generated by the first scrypt test vector below.
INPUT
B[0] = f7 ce 0b 65 3d 2d 72 a4 10 8c f5 ab e9 12 ff dd 77 76 16 db bb 27 a7 0e 82 04 f3 ae 2d 0f 6f ad 89 f6 8f 48 11 d1 e8 7b cc 3b d7 40 0a 9f fd 29 09 4f 01 84 63 95 74 f3 9a e5 a1 31 52 17 bc d7

B[1] = 89 49 91 44 72 13 bb 22 6c 25 b5 4d a8 63 70 fb cd 98 43 80 37 46 66 bb 8f fc b5 bf 40 c2 54 b0 67 d2 7c 51 ce 4a d5 fe d8 29 c9 0b 50 5a 57 1b 7f 4d 1c ad 6a 52 3c da 77 0e 67 bc ea af 7e 89

OUTPUT
B'[0] = a4 1f 85 9c 66 08 cc 99 3b 81 ca cb 02 0c ef 05 04 4b 21 81 a2 fd 33 7d fd 7b 1c 63 96 68 2f 29 b4 39 31 68 e3 c9 e6 bc fe 6b c5 b7 a0 6d 96 ba e4 24 cc 10 2c 91 74 5c 24 ad 67 3d c7 61 8f 81

B'[1] = 20 ed c9 75 32 38 81 a8 05 40 f6 4c 16 2d cd 3c 21 07 7c fe 5f 8d 5f e2 b1 a4 16 8f 95 36 78 b7 7d 3b 3d 80 3b 60 e4 ab 92 09 96 e5 9b 4d 53 b6 5d 2a 22 58 77 d5 ed f5 84 2c b9 f1 4e ef e4 25

9. Test Vectors for scryptROMix

Below is a sequence of octets to illustrate input and output values for scryptROMix. The test vector uses an r value of 1 and an N value of 16. The octets are hex encoded and whitespace is inserted for readability. The value corresponds to the first input and output pair generated by the first scrypt test vector below.
INPUT:
B = f7 ce 0b 65 3d 2d 72 a4 10 8c f5 ab e9 12 ff dd
   77 76 16 db bb 27 a7 0e 82 04 f3 ae 2d 0f 6f ad
   89 f6 8f 48 11 d1 e8 7b cc 3b d7 40 0a 9f fd 29
   09 4f 01 84 63 95 74 f3 9a e5 a1 31 52 17 bc d7
   89 49 91 44 72 13 bb 22 6c 25 b5 4d 83 70 fb
   cd 98 43 80 37 46 66 bb 8f fc b5 bf 40 c2 54 b0
   67 d2 7c 51 ce 4a d5 fe d8 29 c9 0b 50 5a 57 1b
   7f 4d 1c ad 6a 52 3c da 77 0e 67 bc ea af 7e 89

OUTPUT:
B = 79 cc c1 93 62 9d eb ca 04 7f 0b 70 6b 4f 6b 65
   2c e3 dd 4a 96 26 e3 55 fa fc 61 98 e6 ea 2b 46
   d5 84 13 67 3b 99 b0 29 d6 65 c3 57 60 1f b4 26
   a0 b2 f4 bb a2 00 ee 9f 0a 43 d1 9b 57 1a 9c 71
   ef 11 42 e6 5d 5a 26 6f dd ca 83 2c e5 9f aa 7c
   ac 0b 9c f1 be 2b ff ca 30 0d 01 ee 38 76 19 c4
   ae 12 fd 44 3f f2 03 a0 e4 e1 c4 7e c3 14 86 1f
   4e 90 87 cb 33 39 6a 68 73 e8 f9 d2 53 9a 4b 8e

10. Test Vectors for PBKDF2 with HMAC-SHA-256

Below is a sequence of octets illus...PBKDF2-HMAC-SHA-256. The octets are hex encoded and whitespace is inserted for readability. The test vectors below can be used to verify the PBKDF2-HMAC-SHA-256 [RFC2898] function. The password and salt strings are passed as sequences of ASCII [RFC0020] octets.

PBKDF2-HMAC-SHA-256 (P="passwd", S="salt",
   c=1, dkLen=64) =
   55 ac 04 6e 56 e3 08 9f ec 16 91 c2 25 44 b6 05
   f9 41 85 21 6d de 04 65 e6 8b 9d 57 c2 0d ac bc
   49 ca 9c cc f1 79 b6 45 99 16 64 b3 9d 77 ef 31
   7c 71 b8 45 b1 e3 0b d5 09 11 20 41 d3 a1 97 83

PBKDF2-HMAC-SHA-256 (P="Password", S="NaCl",
   c=80000, dkLen=64) =
   4d dc d8 f6 0b 98 be 21 83 0c ee 5e f2 27 01 f9
   64 1a 44 18 d0 4c 04 14 ae ff 08 87 6b 34 ab 56
   a1 d4 25 a1 22 58 33 54 9a db 84 1b 51 c9 b3 17
   6a 27 2b de bb a1 d0 78 47 8f 62 b3 97 f3 3c 8d

11. Test Vectors for scrypt

For reference purposes, we provide the following test vectors for scrypt, where the password and salt strings are passed as sequences of ASCII [RFC0020] octets.
The parameters to the scrypt function below are, in order, the password \( P \) (octet string), the salt \( S \) (octet string), the CPU/Memory cost parameter \( N \), the block size parameter \( r \), and the parallelization parameter \( p \), and the output size \( dkLen \). The output is hex encoded and whitespace is inserted for readability.

\[
\text{scrypt (} P = "" , S = "" , \\
N = 16 , \ r = 1 , \ p = 1 , \ dklen = 64) = \\
77 \ \text{d6} \ \text{57} \ \text{62} \ \text{38} \ \text{65} \ \text{7b} \ \text{20} \ \text{3b} \ \text{19} \ \text{ca} \ \text{42} \ \text{c1} \ \text{8a} \ \text{04} \ \text{97} \\
f1 \ \text{6b} \ \text{48} \ \text{44} \ \text{e3} \ \text{07} \ \text{4a} \ \text{e6} \ \text{df} \ \text{fa} \ \text{3f} \ \text{ed} \ \text{e2} \ \text{14} \ \text{42} \\
f0 \ \text{d0} \ \text{06} \ \text{9d} \ \text{ed} \ \text{09} \ \text{48} \ \text{f8} \ \text{32} \ \text{6a} \ \text{75} \ \text{3a} \ \text{0f} \ \text{c8} \ \text{1f} \ \text{17} \\
e8 \ \text{d3} \ \text{e0} \ \text{fb} \ \text{2e} \ \text{0d} \ \text{36} \ \text{28} \ \text{cf} \ \text{35} \ \text{e2} \ \text{0c} \ \text{38} \ \text{d1} \ \text{89} \ \text{06}
\]

\[
\text{scrypt (} P = \text{"password"} , S = \text{"NaCl"} , \\
N = 1024 , \ r = 8 , \ p = 16 , \ dkLen = 64) = \\
f\text{d} \ \text{ba} \ \text{be} \ \text{1c} \ \text{9d} \ \text{34} \ \text{72} \ \text{00} \ \text{78} \ \text{56} \ \text{e7} \ \text{19} \ \text{0d} \ \text{01} \ \text{e9} \ \text{fe} \\
7c \ \text{6a} \ \text{d7} \ \text{cb} \ \text{c8} \ \text{23} \ \text{78} \ \text{30} \ \text{e7} \ \text{73} \ \text{76} \ \text{63} \ \text{4b} \ \text{37} \ \text{31} \ \text{62} \\
2e \ \text{af} \ \text{30} \ \text{d9} \ \text{2e} \ \text{22} \ \text{a3} \ \text{88} \ \text{6f} \ \text{f1} \ \text{09} \ \text{27} \ \text{9d} \ \text{98} \ \text{30} \ \text{da} \\
c7 \ \text{27} \ \text{af} \ \text{b9} \ \text{4a} \ \text{83} \ \text{ee} \ \text{6d} \ \text{83} \ \text{60} \ \text{cb} \ \text{df} \ \text{a2} \ \text{cc} \ \text{06} \ \text{40}
\]

\[
\text{scrypt (} P = \text{"pleaseletmein"} , S = \text{"SodiumChloride"} , \\
N = 16384 , \ r = 8 , \ p = 1 , \ dkLen = 64) = \\
70 \ \text{23} \ \text{bd} \ \text{cb} \ \text{3a} \ \text{fd} \ \text{73} \ \text{48} \ \text{46} \ \text{1c} \ \text{06} \ \text{cd} \ \text{81} \ \text{fd} \ \text{38} \ \text{eb} \\
f0 \ \text{a8} \ \text{fb} \ \text{ba} \ \text{90} \ \text{4f} \ \text{8e} \ \text{3e} \ \text{a9} \ \text{b5} \ \text{43} \ \text{f6} \ \text{54} \ \text{5d} \ \text{a1} \ \text{f2} \\
d5 \ \text{43} \ \text{29} \ \text{55} \ \text{61} \ \text{3f} \ \text{0f} \ \text{cf} \ \text{62} \ \text{d4} \ \text{97} \ \text{05} \ \text{24} \ \text{2a} \ \text{9a} \ \text{f9} \\
e6 \ \text{1e} \ \text{85} \ \text{dc} \ \text{0d} \ \text{65} \ \text{1e} \ \text{40} \ \text{df} \ \text{cf} \ \text{01} \ \text{7b} \ \text{45} \ \text{57} \ \text{58} \ \text{87}
\]

\[
\text{scrypt (} P = \text{"pleaseletmein"} , S = \text{"SodiumChloride"} , \\
N = 1048576 , \ r = 8 , \ p = 1 , \ dkLen = 64) = \\
21 \ \text{01} \ \text{cb} \ \text{9b} \ \text{6a} \ \text{51} \ \text{1a} \ \text{ae} \ \text{ad} \ \text{db} \ \text{be} \ \text{09} \ \text{cf} \ \text{70} \ \text{f8} \ \text{81} \\
e5 \ \text{56} \ \text{8d} \ \text{57} \ \text{4a} \ \text{2f} \ \text{fd} \ \text{4d} \ \text{ab} \ \text{e5} \ \text{ee} \ \text{98} \ \text{20} \ \text{ad} \ \text{aa} \ \text{47} \\
8e \ \text{56} \ \text{fd} \ \text{8f} \ \text{4b} \ \text{a5} \ \text{d0} \ \text{9f} \ \text{fa} \ \text{1c} \ \text{6d} \ \text{92} \ \text{7c} \ \text{40} \ \text{f4} \ \text{c3} \\
37 \ \text{30} \ \text{40} \ \text{49} \ \text{e8} \ \text{a9} \ \text{52} \ \text{fb} \ \text{cb} \ \text{f4} \ \text{5c} \ \text{6f} \ \text{a7} \ \text{7a} \ \text{41} \ \text{a4}
\]

### 12. Test Vectors for PKCS#8

PKCS#8 [RFC5208] and Asymmetric Key Packages [RFC5958] encode encrypted private-keys. Using PBES2 with scrypt as the KDF, the following illustrates an example of a PKCS#8 encoded private-key. The password is "Rabbit" (without the quotes) with \( N = 1048576 \), \( r = 8 \) and \( p = 1 \). The salt is "Mouse" and the encryption algorithm used is aes256-CBC. The derived key is: E2 77 EA 2C AC B2 3E DA-FC 03 9D 22 9B 79 DC 13 EC ED B6 01 D9 9B 18 2A-9F ED BA 1E 2B FB 4F 58.
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14. Acknowledgements

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15. IANA Considerations

None.

16. Security Considerations

This document specifies a cryptographic algorithm. The reader must follow cryptographic research of published attacks. ROMix has been proven sequential memory-hard under the Random Oracle model for the hash function. The security of scrypt relies on the assumption that BlockMix with Salsa20/8 Core does not exhibit any "shortcuts" which would allow it to be iterated more easily than a random oracle. For other claims about the security properties see [SCRYPT].

Passwords and other sensitive data, such as intermediate values, may continue to be stored in memory, core dumps, swap areas, etc, for a long time after the implementation has processed them. This makes attacks on the implementation easier. Implementation should consider storing sensitive data in protected memory areas. How to achieve this is system dependent.
By nature and depending on parameters, running the scrypt algorithm may require large amounts of memory. Systems should protect against a denial of service attack resulting from attackers presenting unreasonably large parameters.

17. References

17.1. Normative References


17.2. Informative References


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