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Hash-Based Signatures
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Abstract

This note describes a digital signature system based on cryptographic hash functions, following the seminal work in this area of Lamport, Diffie, Winternitz, and Merkle, as adapted by Leighton and Micali in 1995. It specifies a one-time signature scheme and a general signature scheme. These systems provide asymmetric authentication without using large integer mathematics and can achieve a high security level. They are suitable for compact implementations, are relatively simple to implement, and naturally resist side-channel attacks. Unlike most other signature systems, hash-based signatures would still be secure even if it proves feasible for an attacker to build a quantum computer.

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[1.](#) Introduction

One-time signature systems, and general purpose signature systems built out of one-time signature systems, have been known since 1979 [[Merkle79](#)], were well studied in the 1990s [[USPT05432852](#)], and have benefited from renewed attention in the last decade. The characteristics of these signature systems are small private and public keys and fast signature generation and verification, but large signatures and moderately slow key generation (in comparison with RSA and ECDSA). Private keys can be made very small by appropriate key generation, for example, as described in [Appendix A](#). In recent years there has been interest in these systems because of their post-quantum security and their suitability for compact verifier implementations.

This note describes the Leighton and Micali adaptation [[USPT05432852](#)] of the original Lamport-Diffie-Winternitz-Merkle one-time signature system [[Merkle79](#)] [[C:Merkle87](#)][[C:Merkle89a](#)][[C:Merkle89b](#)] and general signature system [[Merkle79](#)] with enough specificity to ensure interoperability between implementations.

A signature system provides asymmetric message authentication. The key generation algorithm produces a public/private key pair. A message is signed by a private key, producing a signature, and a message/signature pair can be verified by a public key. A One-Time Signature (OTS) system can be used to sign one message securely, but will become insecure if more than one is signed with the same public/private key pair. An N-time signature system can be used to sign N or fewer messages securely. A Merkle tree signature scheme is an N-time signature system that uses an OTS system as a component.

In this note we describe the Leighton-Micali Signature (LMS) system, which is a variant of the Merkle scheme, and a Hierarchical Signature System (HSS) built on top of it that can efficiently scale to larger numbers of signatures. We denote the one-time signature scheme incorporated in LMS as LM-OTS. This note is structured as follows. Notation is introduced in [Section 3](#). The LM-OTS signature system is described in [Section 4](#), and the LMS and HSS N-time signature systems are described in [Section 5](#) and [Section 6](#), respectively. Sufficient detail is provided to ensure interoperability. The public formats are described in [Section 7](#). The rationale for design decisions are given in [Section 8](#). The changes made to this document over previous versions is listed in [Section 9](#). The IANA registry for these signature systems is described in [Section 10](#). Intellectual Property issues are discussed in [Section 11](#). Security considerations are presented in [Section 12](#).

[1.1](#). Conventions Used In This Document

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [[RFC2119](#)].

[2](#). Interface

The LMS signing algorithm is stateful; it modifies and updates the private key as a side effect of generating a signature. Once a particular value of the private key is used to sign one message, it MUST NOT be used to sign another.

The key generation algorithm takes as input an indication of the parameters for the signature system. If it is successful, it returns both a private key and a public key. Otherwise, it returns an indication of failure.

The signing algorithm takes as input the message to be signed and the current value of the private key. If successful, it returns a signature and the next value of the private key, if there is such a value. After the private key of an N-time signature system has signed N messages, the signing algorithm returns the signature and an indication that there is no next value of the private key that can be used for signing. If unsuccessful, it returns an indication of failure.

The verification algorithm takes as input the public key, a message, and a signature, and returns an indication of whether or not the signature and message pair are valid.

A message/signature pair are valid if the signature was returned by the signing algorithm upon input of the message and the private key corresponding to the public key; otherwise, the signature and message pair are not valid with probability very close to one.

[3.](#) Notation

[3.1.](#) Data Types

Bytes and byte strings are the fundamental data types. A single byte is denoted as a pair of hexadecimal digits with a leading "0x". A byte string is an ordered sequence of zero or more bytes and is denoted as an ordered sequence of hexadecimal characters with a leading "0x". For example, 0xe534f0 is a byte string with a length of three. An array of byte strings is an ordered set, indexed starting at zero, in which all strings have the same length.

Unsigned integers are converted into byte strings by representing them in network byte order. To make the number of bytes in the representation explicit, we define the functions `u8str(X)`, `u16str(X)`, and `u32str(X)`, which take a non-negative integer `X` as input and return one, two, and four byte strings, respectively. We also make

use of the function `strTou32(S)`, which takes a four byte string `S` as input and returns a non-negative integer; the identity `u32str(strTou32(S)) = S` holds for any four-byte string `S`.

[3.1.1.](#) Operators

When `a` and `b` are real numbers, mathematical operators are defined as follows:

`^` : `a ^ b` denotes the result of `a` raised to the power of `b`

`*` : `a * b` denotes the product of `a` multiplied by `b`

`/` : `a / b` denotes the quotient of `a` divided by `b`

`%` : `a % b` denotes the remainder of the integer division of `a` by `b`

`+` : `a + b` denotes the sum of `a` and `b`

`-` : `a - b` denotes the difference of `a` and `b`

The standard order of operations is used when evaluating arithmetic expressions.

When `B` is a byte and `i` is an integer, then `B >> i` denotes the logical right-shift operation by `i` positions. Similarly, `B << i` denotes the logical left-shift operation.

If `S` and `T` are byte strings, then `S || T` denotes the concatenation of `S` and `T`. If `S` and `T` are equal length byte strings, then `S AND T` denotes the bitwise logical and operation.

The i^{th} element in an array `A` is denoted as `A[i]`.

[3.1.2.](#) Functions

If `r` is a non-negative real number, then we define the following functions:

`ceil(r)` : returns the smallest integer larger than `r`

`floor(r)` : returns the largest integer smaller than `r`

`lg(r)` : returns the base-2 logarithm of `r`

[3.1.3.](#) Strings of `w`-bit elements

If `S` is a byte string, then `byte(S, i)` denotes its i^{th} byte, where `byte(S, 0)` is the leftmost byte. In addition, `bytes(S, i, j)` denotes the range of bytes from the i^{th} to the j^{th} byte, inclusive. For example, if `S = 0x02040608`, then `byte(S, 0)` is `0x02` and `bytes(S, 1, 2)` is `0x0406`.

A byte string can be considered to be a string of `w`-bit unsigned integers; the correspondence is defined by the function `coef(S, i, w)` as follows:

If `S` is a string, `i` is a positive integer, and `w` is a member of the set `{ 1, 2, 4, 8 }`, then `coef(S, i, w)` is the i^{th} , `w`-bit value, if `S` is interpreted as a sequence of `w`-bit values. That is,

$$\text{coef}(S, i, w) = (2^w - 1) \text{ AND } \\ (\text{byte}(S, \text{floor}(i * w / 8)) \gg \\ (8 - (w * (i \% (8 / w)) + w)))$$

For example, if `S` is the string `0x1234`, then `coef(S, 7, 1)` is 0 and `coef(S, 0, 4)` is 1.

`S` (represented as bits)

```
+---+---+---+---+---+---+---+---+---+---+---+---+---+---+---+
| 0| 0| 0| 1| 0| 0| 1| 0| 0| 0| 1| 1| 0| 1| 0| 0|
+---+---+---+---+---+---+---+---+---+---+---+---+---+---+---
```

$$\begin{array}{c} \wedge \\ | \\ \text{coef}(S, 7, 1) \end{array}$$

S (represented as four-bit values)

+-----+	+-----+	+-----+	+-----+
	1		2
	3		4
+-----+	+-----+	+-----+	+-----+

$$\begin{array}{c} \wedge \\ | \\ \text{coef}(S, 0, 4) \end{array}$$

The return value of `coef` is an unsigned integer. If *i* is larger than the number of *w*-bit values in *S*, then `coef(S, i, w)` is undefined, and an attempt to compute that value should raise an error.

3.2. Security string

To improve security against attacks that amortize their effort against multiple invocations of the hash function, Leighton and Micali introduce a "security string" that is distinct for each invocation of that function. Whenever this process computes a hash, the string being hashed will start with a string formed from the below fields. These fields will appear in fixed locations in the value we compute the hash of, and so we list where in the hash these fields would be present. These fields are:

I - a 16 byte identifier for the LMS public/private key pair. It MUST be chosen uniformly at random, or via a pseudorandom process, at the time that a key pair is generated, in order to minimize the probability that any specific value of *I* be used for a large number of different LMS private keys. This is always bytes 0-15 of the hash.

r - in the LMS N-time signature scheme, the node number *r* associated with a particular node of a hash tree is used as an input to the hash used to compute that node. This value is represented as a 32-bit (four byte) unsigned integer in network

byte order. Either *r* or *q* (depending on the domain separation

parameter) will be bytes 16-19 of the hash.

q - in the LMS N-time signature scheme, each LM-OTS signature is associated with the leaf of a hash tree, and q is set to the leaf number. This ensures that a distinct value of q is used for each distinct LM-OTS public/private key pair. This value is represented as a 32-bit (four byte) unsigned integer in network byte order. Either r or q (depending on the domain separation parameter) will be bytes 16-19 of the hash.

D - a domain separation parameter, which is a two byte identifier that takes on different values in the different contexts in which the hash function is invoked. D occurs in bytes 20, 21 of the hash, and takes on the following values:

D_PBLC = 0x8080 when computing the hash of all of the iterates in the LM-OTS algorithm

D_MSG = 0x8181 when computing the hash of the message in the LM-OTS algorithms

D_LEAF = 0x8282 when computing the hash of the leaf of an LMS tree

D_INTR = 0x8383 when computing the hash of an interior node of an LMS tree

i = a value between 0 and 264; this is used in the LM-OTS scheme, when either computing the iterations of the Winternitz chain, or when using the suggested LM-OTS private key generation process. The value is also the index of the LM-OTS private key element upon which H is being applied. It is represented as a 16-bit (two byte) unsigned integer in network byte order.

j - in the LM-OTS scheme, j is the iteration number used when the private key element is being iteratively hashed. It is represented as an 8-bit (one byte) unsigned integer and is present if D is a value between 0 and 264. If present, it occurs at byte 22 of the hash.

C - an n-byte randomizer that is included with the message whenever it is being hashed to improve security. C MUST be chosen uniformly at random, or via a pseudorandom process. It is present if D=D_MSG, and it occurs at bytes 22 to 21+n of the hash.

[3.3.](#) Typecodes

A typecode is an unsigned integer that is associated with a particular data format. The format of the LM-OTS, LMS, and HSS signatures and public keys all begin with a typecode that indicates the precise details used in that format. These typecodes are represented as four-byte unsigned integers in network byte order; equivalently, they are XDR enumerations (see [Section 7](#)).

[4.](#) LM-OTS One-Time Signatures

This section defines LM-OTS signatures. The signature is used to validate the authenticity of a message by associating a secret private key with a shared public key. These are one-time signatures; each private key **MUST** be used at most one time to sign any given message.

As part of the signing process, a digest of the original message is computed using the cryptographic hash function H (see [Section 4.1](#)), and the resulting digest is signed.

In order to facilitate its use in an N-time signature system, the LM-OTS key generation, signing, and verification algorithms all take as input a diversification parameter q (which is used as part of the security string, as listed in [Section 3.2](#)). When the LM-OTS signature system is used outside of an N-time signature system, this value **SHOULD** be set to the all-zero value.

[4.1.](#) Parameters

The signature system uses the parameters n and w , which are both positive integers. The algorithm description also makes use of the internal parameters p and ls , which are dependent on n and w . These parameters are summarized as follows:

n : the number of bytes of the output of the hash function

w : the width (in bits) of the Winternitz coefficients; it is a member of the set $\{ 1, 2, 4, 8 \}$

p : the number of n -byte string elements that make up the LM-OTS signature

ls : the number of left-shift bits used in the checksum function Ck_{sm} (defined in [Section 4.5](#)).

H : a second-preimage-resistant cryptographic hash function that accepts byte strings of any length, and returns an n-byte string.

For more background on the cryptographic security requirements on H, see the [Section 12](#).

The value of n is determined by the hash function selected for use as part of the LM-OTS algorithm; the choice of this value has a strong effect on the security of the system. The parameter w determines the length of the Winternitz chains computed as a part of the OTS signature (which involve $2^w - 1$ invocations of the hash function); it has little effect on security. Increasing w will shorten the signature, but at a cost of a larger computation to generate and verify a signature. The values of p and ls are dependent on the choices of the parameters n and w, as described in [Appendix B](#). A table illustrating various combinations of n, w, p, and ls is provided in Table 1.

[4.2](#). Parameter Sets

To fully describe a LM-OTS signature method, the parameters n and w, as well as the function H, MUST be specified. This section defines several LM-OTS methods, each of which is identified by a name. The values for p and ls are provided as a convenience; the formal method of computing them is given in [Appendix B](#).

The value of w describes a space/time trade-off; increasing the value of w will cause the signature to shrink (by decreasing the value of p) while increasing the amount of time needed to perform operations with it (generate the public key, generate and verify the signature); in general, the LM-OTS signature is $n \times p$ bytes long, and public key generation will take $p \times (2^w - 1) + 1$ hash computations (and signature generation and verification will take about half that on average).

Name	H	n	w	p	ls
LMOTS_SHA256_N32_W1	SHA256	32	1	265	7
LMOTS_SHA256_N32_W2	SHA256	32	2	133	6
LMOTS_SHA256_N32_W4	SHA256	32	4	67	4

	LMOTS_SHA256_N32_W8		SHA256		32	
					8	
					34	
					0	
+	-----	+	-----	+	-----	+

Table 1

Here SHA256 denotes the NIST standard hash function [[FIPS180](#)].

[4.3.](#) Private Key

The format of the LM-OTS private key is an internal matter to the implementation, and this document does not attempt to define it. One possibility is that the private key may consist of a typecode indicating the particular LM-OTS algorithm, an array `x[]` containing `p` `n`-byte strings, and the 16 byte string `I` and the 4 byte string `q`. This private key **MUST** be used to sign (at most) one message. The following algorithm shows pseudocode for generating a private key.

Algorithm 0: Generating a Private Key

1. retrieve the value `q` from the type, and the value `I` the 16 byte identifier of the LMS public/private keypair that this LM-OTS private key will be used with
2. set `type` to the typecode of the algorithm
3. set `n` and `p` according to the typecode and Table 1
4. compute the array `x` as follows:


```
for ( i = 0; i < p; i = i + 1 ) {
    set x[i] to a uniformly random n-byte string
}
```
5. return `u32str(type) || I || u32str(q) || x[0] || x[1] || ... || x[p-1]`

An implementation **MAY** use a pseudorandom method to compute `x[i]`, as suggested in [[Merkle79](#)], page 46. The details of the pseudorandom method do not affect interoperability, but the cryptographic strength **MUST** match that of the LM-OTS algorithm. [Appendix A](#) provides an example of a pseudorandom method for computing the LM-OTS private

key.

[4.4.](#) Public Key

The LM-OTS public key is generated from the private key by iteratively applying the function H to each individual element of x , for $2^w - 1$ iterations, then hashing all of the resulting values.

The public key is generated from the private key using the following algorithm, or any equivalent process.

Algorithm 1: Generating a One Time Signature Public Key From a Private Key

1. set type to the typecode of the algorithm
2. set the integers n , p , and w according to the typecode and Table 1
3. determine x , I and q from the private key
4. compute the string K as follows:

```
for ( i = 0; i < p; i = i + 1 ) {
    tmp = x[i]
    for ( j = 0; j < 2^w - 1; j = j + 1 ) {
        tmp = H(I || u32str(q) || u16str(i) || u8str(j) || tmp)
    }
    y[i] = tmp
}
K = H(I || u32str(q) || u16str(D_PBLIC) || y[0] || ... || y[p-1])
```
5. return $u32str(type) || I || u32str(q) || K$

The public key is the value returned by Algorithm 1.

[4.5.](#) Checksum

A checksum is used to ensure that any forgery attempt that manipulates the elements of an existing signature will be detected. The security property that it provides is detailed in [Section 12](#). The checksum function Cksm is defined as follows, where S denotes the n -byte string that is input to that function, and the value sum is a 16-bit unsigned integer:

Algorithm 2: Checksum Calculation

```

sum = 0
for ( i = 0; i < (n*8/w); i = i + 1 ) {
    sum = sum + (2^w - 1) - coef(S, i, w)
}
return (sum << ls)

```

Because of the left-shift operation, the rightmost bits of the result of Cksm will often be zeros. Due to the value of p , these bits will not be used during signature generation or verification.

[4.6.](#) Signature Generation

The LM-OTS signature of a message is generated by first prepending the LM key identifier I , the LM leaf identifier q , the value D_MSG and the randomizer C to the message, then computing the hash, and then concatenating the checksum of the hash to the hash itself, then considering the resulting value as a sequence of w -bit values, and using each of the w -bit values to determine the number of times to apply the function H to the corresponding element of the private key. The outputs of the function H are concatenated together and returned as the signature. The pseudocode for this procedure is shown below.

Algorithm 3: Generating a One Time Signature From a Private Key and a Message

1. set type to the typecode of the algorithm
2. set n , p , and w according to the typecode and Table 1

3. determine x , I and q from the private key
4. set C to a uniformly random n -byte string
5. compute the array y as follows:


```

      Q = H(I || u32str(q) || u16str(D_MESG) || C || message)
      for ( i = 0; i < p; i = i + 1 ) {
        a = coef(Q || Cksm(Q), i, w)
        tmp = x[i]
        for ( j = 0; j < a; j = j + 1 ) {
          tmp = H(I || u32str(q) || u16str(i) || u8str(j) || tmp)
        }
        y[i] = tmp
      }
      
```
6. return $u32str(type) || C || y[0] || \dots || y[p-1]$

Note that this algorithm results in a signature whose elements are intermediate values of the elements computed by the public key algorithm in [Section 4.4](#).

The signature is the string returned by Algorithm 3. [Section 7](#) specifies the typecode and more formally defines the encoding and decoding of the string.

[4.7](#). Signature Verification

In order to verify a message with its signature (an array of n -byte strings, denoted as y), the receiver must "complete" the chain of iterations of H using the w -bit coefficients of the string resulting from the concatenation of the message hash and its checksum. This computation should result in a value that matches the provided public key.

Algorithm 4a: Verifying a Signature and Message Using a Public Key

1. if the public key is not at least four bytes long, return INVALID
2. parse pubkey, I, q, and K from the public key as follows:
 - a. pubkey = strtou32(first 4 bytes of public key)
 - b. if the public key is not exactly 24 + n bytes long, return INVALID
 - c. I = next 16 bytes of public key
 - d. q = strtou32(next 4 bytes of public key)
 - e. K = next n bytes of public key
3. compute the public key candidate Kc from the signature, message, and the identifiers I and q obtained from the public key, using Algorithm 4b. If Algorithm 4b returns INVALID, then return INVALID.
4. if Kc is equal to K, return VALID; otherwise, return INVALID

Algorithm 4b: Computing a Public Key Candidate Kc from a Signature, Message, Signature Typecode Type , and identifiers I, q

1. if the signature is not at least four bytes long, return INVALID

2. parse sigtype, C, and y from the signature as follows:
 - a. sigtype = strTou32(first 4 bytes of signature)
 - b. if sigtype is not equal to pubtype, return INVALID
 - c. set n and p according to the pubtype and Table 1; if the signature is not exactly $4 + n * (p+1)$ bytes long, return INVALID
 - d. C = next n bytes of signature
 - e. y[0] = next n bytes of signature
 y[1] = next n bytes of signature
 ...
 y[p-1] = next n bytes of signature
3. compute the string Kc as follows


```

Q = H(I || u32str(q) || u16str(D_MESG) || C || message)
for ( i = 0; i < p; i = i + 1 ) {
  a = coef(Q || Cksm(Q), i, w)
  tmp = y[i]
  for ( j = a; j < 2^w - 1; j = j + 1 ) {
    tmp = H(I || u32str(q) || u16str(i) || u8str(j) || tmp)
  }
  z[i] = tmp
}
Kc = H(I || u32str(q) || u16str(D_PBLC) || z[0] || z[1] || ... || z[p-1])

```
4. return Kc

5. Leighton Micali Signatures

The Leighton Micali Signature (LMS) method can sign a potentially large but fixed number of messages. An LMS system uses two cryptographic components: a one-time signature method and a hash function. Each LMS public/private key pair is associated with a perfect binary tree, each node of which contains an m-byte value, where m is the output length of the hash function. Each leaf of the tree contains the value of the public key of an LM-OTS public/private key pair. The value contained by the root of the tree is the LMS public key. Each interior node is computed by applying the hash function to the concatenation of the values of its children nodes.

Each node of the tree is associated with a node number, an unsigned integer that is denoted as `node_num` in the algorithms below, which is computed as follows. The root node has node number 1; for each node with node number $N < 2^h$, its left child has node number $2*N$, while its right child has node number $2*N+1$. The result of this is that each node within the tree will have a unique node number, and the leaves will have node numbers 2^h , $(2^h)+1$, $(2^h)+2$, ..., $(2^h)+(2^h)-1$. In general, the j^{th} node at level L has node number $2^L + j$. The node number can conveniently be computed when it is needed in the LMS algorithms, as described in those algorithms.

5.1. Parameters

An LMS system has the following parameters:

h : the height (number of levels - 1) in the tree, and

m : the number of bytes associated with each node.

H : a second-preimage-resistant cryptographic hash function that accepts byte strings of any length, and returns an m -byte string. H SHOULD be the same as in [Section 4.1](#), but MAY be different.

There are 2^h leaves in the tree. The hash function used within the LMS system SHOULD be the same as the hash function used within the LM-OTS system used to generate the leaves.

Name	H	m	h
LMS_SHA256_M32_H5	SHA256	32	5
LMS_SHA256_M32_H10	SHA256	32	10
LMS_SHA256_M32_H15	SHA256	32	15
LMS_SHA256_M32_H20	SHA256	32	20
LMS_SHA256_M32_H25	SHA256	32	25

Table 2

5.2. LMS Private Key

The format of the LMS private key is an internal matter to the implementation, and this document does not attempt to define it. One

possibility is that it may consist of an array `OTS_PRIV[]` of 2^h LM-

OTS private keys, and the leaf number q of the next LM-OTS private key that has not yet been used. The q^{th} element of `OTS_PRIV[]` is generated using Algorithm 0 with the identifiers I, q . The leaf number q is initialized to zero when the LMS private key is created. The process is as follows:

Algorithm 5: Computing an LMS Private Key.

1. determine h and m from the typecode and Table 2.
2. compute the array `OTS_PRIV[]` as follows:
for ($q = 0; q < 2^h; q = q + 1$) {
 `OTS_PRIV[q]` = LM-OTS private key with identifiers I, q
}
3. $q = 0$

An LMS private key MAY be generated pseudorandomly from a secret value, in which case the secret value MUST be at least m bytes long, be uniformly random, and MUST NOT be used for any other purpose than the generation of the LMS private key. The details of how this process is done do not affect interoperability; that is, the public key verification operation is independent of these details.

[Appendix A](#) provides an example of a pseudorandom method for computing an LMS private key.

The signature generation logic uses q as the next leaf to use, hence step 3 starts it off at the left-most one.

[5.3.](#) LMS Public Key

An LMS public key is defined as follows, where we denote the public key final hash value (namely, the K value computed in algorithm 1) associated with the i^{th} LM-OTS private key as `OTS_PUB_HASH[i]`, with i ranging from 0 to $(2^h)-1$. Each instance of an LMS public/private key pair is associated with a balanced binary tree, and the nodes of that tree are indexed from 1 to $2^{(h+1)}-1$. Each node is associated with an m -byte string, and the string for the r^{th} node is denoted as `T[r]` and is defined as

$$T[r] = \begin{cases} H(I || u32str(r) || u16str(D_LEAF) || OTS_PUB_HASH[r-2^h]) & \text{if } r \geq 2^h, \\ H(I || u32str(r) || u16str(D_INTR) || T[2*r] || T[2*r+1]) & \text{otherwise.} \end{cases}$$

The LMS public key is the string `u32str(type) || u32str(otstype) || I || T[1]`. [Section 7](#) specifies the format of the type variable. The value `otstype` is the parameter set for the LM-OTS public/private keypairs used. The value `I` is the private key identifier, and is the value used for all computations for the same LMS tree. The value

`T[1]` can be computed via recursive application of the above equation, or by any equivalent method. An iterative procedure is outlined in [Appendix C](#).

[5.4](#). LMS Signature

An LMS signature consists of

- the number `q` of the leaf associated with the LM-OTS signature, as a four-byte unsigned integer in network byte order,

- an LM-OTS signature, and

- a typecode indicating the particular LMS algorithm,

- an array of `h` `m`-byte values that is associated with the path through the tree from the leaf associated with the LM-OTS signature to the root.

Symbolically, the signature can be represented as `u32str(q) || ots_signature || u32str(type) || path[0] || path[1] || ... || path[h-1]`. [Section 7](#) specifies the typecode and more formally defines the format. The array of values contains the siblings of the nodes on the path from the leaf to the root but does not contain the nodes on the path themselves. The array for a tree with height `h` will have `h` values. The first value is the sibling of the leaf, the next value is the sibling of the parent of the leaf, and so on up the path to the root.

[5.4.1](#). LMS Signature Generation

To compute the LMS signature of a message with an LMS private key, the signer first computes the LM-OTS signature of the message using

the leaf number of the next unused LM-OTS private key. The leaf number q in the signature is set to the leaf number of the LMS private key that was used in the signature. Before releasing the signature, the leaf number q in the LMS private key MUST be incremented, to prevent the LM-OTS private key from being used again. If the LMS private key is maintained in nonvolatile memory, then the implementation MUST ensure that the incremented value has been stored before releasing the signature. The issue this tries to prevent is a scenario where a) we generate a signature, using one LM-OTS private key, and release it to the application, b) before we update the nonvolatile memory, we crash, and c) we reboot, and generate a second signature using the same LM-OTS private key; with two different signatures using the same LM-OTS private key, someone could potentially generate a forged signature of a third message.

The array of node values in the signature MAY be computed in any way. There are many potential time/storage tradeoffs that can be applied. The fastest alternative is to store all of the nodes of the tree and set the array in the signature by copying them; pseudocode to do so appears in [Appendix D](#). The least storage intensive alternative is to recompute all of the nodes for each signature. Note that the details of this procedure are not important for interoperability; it is not necessary to know any of these details in order to perform the signature verification operation. The internal nodes of the tree need not be kept secret, and thus a node-caching scheme that stores only internal nodes can sidestep the need for strong protections.

Several useful time/storage tradeoffs are described in the 'Small-Memory LM Schemes' section of [\[USPTO5432852\]](#).

[5.5](#). LMS Signature Verification

An LMS signature is verified by first using the LM-OTS signature verification algorithm (Algorithm 4b) to compute the LM-OTS public key from the LM-OTS signature and the message. The value of that public key is then assigned to the associated leaf of the LMS tree, then the root of the tree is computed from the leaf value and the array `path[]` as described in Algorithm 6 below. If the root value matches the public key, then the signature is valid; otherwise, the signature fails.

Algorithm 6: LMS Signature Verification

1. if the public key is not at least eight bytes long, return INVALID
2. parse pubkey, I, and T[1] from the public key as follows:
 - a. pubkey = strTou32(first 4 bytes of public key)
 - b. ots_typecode = strTou32(next 4 bytes of public key)
 - c. set m according to pubkey, based on Table 2
 - d. if the public key is not exactly 24 + m bytes long, return INVALID
 - e. I = next 16 bytes of the public key
 - f. T[1] = next m bytes of the public key

3. compute the LMS Public Key Candidate T_c from the signature, message, identifier, pubkey and ots_typecode using Algorithm 6b.
4. if T_c is equal to $T[1]$, return VALID; otherwise, return INVALID

Algorithm 6b: Computing an LMS Public Key Candidate from a Signature, Message, Identifier, and algorithm typecode

1. if the signature is not at least eight bytes long, return INVALID
2. parse sigtype, q, ots_signature, and path from the signature as follows:
 - a. $q = \text{strTou32}(\text{first 4 bytes of signature})$
 - b. $\text{otssigtype} = \text{strTou32}(\text{next 4 bytes of signature})$
 - c. if otssigtype is not the OTS typecode from the public key, return INVALID
 - d. set n, p according to otssigtype and Table 1; if the signature is not at least $12 + n * (p + 1)$ bytes long, return INVALID
 - e. $\text{ots_signature} = \text{bytes } 8 \text{ through } 8 + n * (p + 1) - 1 \text{ of signature}$
 - f. $\text{sigtype} = \text{strTou32}(4 \text{ bytes of signature at location } 8 + n * (p + 1))$
 - f. if sigtype is not the LM typecode from the public key, return INVALID

- g. set m, h according to sigtype and Table 2
- h. if $q \geq 2^h$ or the signature is not exactly $12 + n * (p + 1) + m * h$ bytes long, return INVALID
- i. set path as follows:
 - path[0] = next m bytes of signature
 - path[1] = next m bytes of signature
 - ...
 - path[h-1] = next m bytes of signature
3. K_c = candidate public key computed by applying Algorithm 4b to the signature ots_signature, the message, and the

identifiers I , q

4. compute the candidate LMS root value T_c as follows:

```
node_num = 2^h + q
tmp = H(I || u32str(node_num) || u16str(D_LEAF) || Kc)
i = 0
while (node_num > 1) {
  if (node_num is odd):
    tmp = H(I || u32str(node_num/2) || u16str(D_INTR) || path[i] || tmp)
  else:
    tmp = H(I || u32str(node_num/2) || u16str(D_INTR) || tmp || path[i])
  node_num = node_num/2
  i = i + 1
}
Tc = tmp
```

5. return T_c

6. Hierarchical signatures

In scenarios where it is necessary to minimize the time taken by the public key generation process, a Hierarchical N-time Signature System (HSS) can be used. Leighton and Micali describe a scheme in which an LMS public key is used to sign a second LMS public key, which is then distributed along with the signatures generated with the second public key [[USPT05432852](#)]. This hierarchical scheme, which we describe in this section, uses an LMS scheme as a component. HSS, in essence, utilizes a tree of LMS trees, in which the HSS public key contains the public key of the LMS tree at the root, and an HSS signature is associated with a path from the root of the HSS tree to one of its leaves. Compared to LMS, HSS has a much reduced public key generation time, as only the root tree needs to be generated prior to the distribution of the HSS public key.

Each level of the hierarchy is associated with a distinct LMS public key, private key, signature, and identifier. The number of levels is

denoted L , and is between one and eight, inclusive. The following notation is used, where i is an integer between 0 and $L-1$ inclusive, and the root of the hierarchy is level 0:

$prv[i]$ is the LMS private key of the i^{th} level,

pub[i] is the LMS public key of the i^{th} level (which includes the identifier I as well as the key value K),

sig[i] is the LMS signature of the i^{th} level,

In this section, we say that an N-time private key is exhausted when it has generated N signatures, and thus it can no longer be used for signing.

HSS allows $L=1$, in which case the HSS public key and signature formats are essentially the LMS public key and signature formats, prepended by a fixed field. Since HSS with $L=1$ has very little overhead compared to LMS, all implementations MUST support HSS in order to maximize interoperability.

[6.1.](#) Key Generation

When an HSS key pair is generated, the key pair for each level MUST have its own identifier I.

To generate an HSS private and public key pair, new LMS private and public keys are generated for prv[i] and pub[i] for $i=0, \dots, L-1$. These key pairs, and their identifiers, MUST be generated independently.

The public key of the HSS scheme consists of the number of levels L, followed by pub[0], the public key of the top level.

The HSS private key consists of prv[0], \dots , prv[L-1]. The values pub[0] and prv[0] do not change, though the values of pub[i] and prv[i] are dynamic for $i > 0$, and are changed by the signature generation algorithm.

[6.2.](#) Signature Generation

To sign a message using the private key prv, the following steps are performed:

If prv[L-1] is exhausted, then determine the smallest integer d such that all of the private keys prv[d], prv[d+1], \dots , prv[L-1] are exhausted. If d is equal to zero, then the HSS key pair is exhausted, and it MUST NOT generate any more signatures.

Otherwise, the key pairs for levels d through $L-1$ must be regenerated during the signature generation process, as follows. For i from d to $L-1$, a new LMS public and private key pair with a new identifier is generated, $\text{pub}[i]$ and $\text{prv}[i]$ are set to those values, then the public key $\text{pub}[i]$ is signed with $\text{prv}[i-1]$, and $\text{sig}[i-1]$ is set to the resulting value.

The message is signed with $\text{prv}[L-1]$, and the value $\text{sig}[L-1]$ is set to that result.

The value of the HSS signature is set as follows. We let signed_pub_key denote an array of octet strings, where $\text{signed_pub_key}[i] = \text{sig}[i] \parallel \text{pub}[i+1]$, for i between 0 and $\text{Nspk}-1$, inclusive, where $\text{Nspk} = L-1$ denotes the number of signed public keys. Then the HSS signature is $\text{u32str}(\text{Nspk}) \parallel \text{signed_pub_key}[0] \parallel \dots \parallel \text{signed_pub_key}[\text{Nspk}-1] \parallel \text{sig}[\text{Nspk}]$.

Note that the number of signed_pub_key elements in the signature is indicated by the value Nspk that appears in the initial four bytes of the signature.

In the specific case of $L=1$, the format of an HSS signature is

$\text{u32str}(0) \parallel \text{sig}[0]$

In the general case, the format of an HSS signature is

$\text{u32str}(\text{Nspk}) \parallel \text{signed_pub_key}[0] \parallel \dots \parallel \text{signed_pub_key}[\text{Nspk}-1] \parallel \text{sig}[\text{Nspk}]$

which is equivalent to

$\text{u32str}(\text{Nspk}) \parallel \text{sig}[0] \parallel \text{pub}[1] \parallel \dots \parallel \text{sig}[\text{Nspk}-1] \parallel \text{pub}[\text{Nspk}] \parallel \text{sig}[\text{Nspk}]$

[6.3.](#) Signature Verification

To verify a signature sig and message using the public key pub , the following steps are performed:

The signature *S* is parsed into its components as follows:

```
Nspk = strTou32(first four bytes of S)
if Nspk+1 is not equal to the number of levels L in pub:
    return INVALID
for (i = 0; i < Nspk; i = i + 1) {
    siglist[i] = next LMS signature parsed from S
    publist[i] = next LMS public key parsed from S
}
siglist[Nspk] = next LMS signature parsed from S

key = pub
for (i = 0; i < Nspk; i = i + 1) {
    sig = siglist[i]
    msg = publist[i]
    if (lms_verify(msg, key, sig) != VALID):
        return INVALID
    key = msg
return lms_verify(message, key, siglist[Nspk])
```

Since the length of an LMS signature cannot be known without parsing it, the HSS signature verification algorithm makes use of an LMS signature parsing routine that takes as input a string consisting of an LMS signature with an arbitrary string appended to it, and returns both the LMS signature and the appended string. The latter is passed on for further processing.

7. Formats

The signature and public key formats are formally defined using the External Data Representation (XDR) [[RFC4506](#)] in order to provide an unambiguous, machine readable definition. For clarity, we also include a private key format as well, though consistency is not needed for interoperability and an implementation MAY use any private key format. Though XDR is used, these formats are simple and easy to parse without any special tools. An illustration of the layout of data in these objects is provided below. The definitions are as follows:

```
/* one-time signatures */
```

```
enum ots_algorithm_type {
    lmots_reserved      = 0,
    lmots_sha256_n32_w1 = 1,
    lmots_sha256_n32_w2 = 2,
    lmots_sha256_n32_w4 = 3,
```

```
    lmots_sha256_n32_w8 = 4
};

typedef opaque bytestring32[32];

struct lmots_signature_n32_p265 {
    bytestring32 C;
    bytestring32 y[265];
};

struct lmots_signature_n32_p133 {
    bytestring32 C;
    bytestring32 y[133];
};

struct lmots_signature_n32_p67 {
    bytestring32 C;
    bytestring32 y[67];
};

struct lmots_signature_n32_p34 {
    bytestring32 C;
    bytestring32 y[34];
};

union ots_signature switch (ots_algorithm_type type) {
    case lmots_sha256_n32_w1:
        lmots_signature_n32_p265 sig_n32_p265;
    case lmots_sha256_n32_w2:
        lmots_signature_n32_p133 sig_n32_p133;
    case lmots_sha256_n32_w4:
        lmots_signature_n32_p67 sig_n32_p67;
    case lmots_sha256_n32_w8:
        lmots_signature_n32_p34 sig_n32_p34;
    default:
```

```

    void;    /* error condition */
};

/* hash based signatures (hbs) */

enum hbs_algorithm_type {
    hbs_reserved      = 0,
    lms_sha256_n32_h5  = 5,
    lms_sha256_n32_h10 = 6,
    lms_sha256_n32_h15 = 7,
    lms_sha256_n32_h20 = 8,
    lms_sha256_n32_h25 = 9,

```

```

};

/* leighton micali signatures (lms) */

union lms_path switch (hbs_algorithm_type type) {
    case lms_sha256_n32_h5:
        bytestring32 path_n32_h5[5];
    case lms_sha256_n32_h10:
        bytestring32 path_n32_h10[10];
    case lms_sha256_n32_h15:
        bytestring32 path_n32_h15[15];
    case lms_sha256_n32_h20:
        bytestring32 path_n32_h20[20];
    case lms_sha256_n32_h25:
        bytestring32 path_n32_h25[25];
    default:
        void;    /* error condition */
};

struct lms_signature {
    unsigned int q;
    ots_signature lmots_sig;
    lms_path nodes;
};

struct lms_key_n32 {
    ots_algorithm_type ots_alg_type;
    opaque I[16];

```

```

    opaque K[32];
};

union hbs_public_key switch (hbs_algorithm_type type) {
    case lms_sha256_n32_h5:
    case lms_sha256_n32_h10:
    case lms_sha256_n32_h15:
    case lms_sha256_n32_h20:
    case lms_sha256_n32_h25:
        lms_key_n32 z_n32;
    default:
        void;      /* error condition */
};

/* hierarchical signature system (hss) */

struct hss_public_key {
    unsigned int L;
    hbs_public_key pub;
};

```

```

struct signed_public_key {
    hbs_signature sig;
    hbs_public_key pub;
}

struct hss_signature {
    signed_public_key signed_keys<7>;
    hbs_signature sig_of_message;
};

```

Many of the objects start with a typecode. A verifier MUST check each of these typecodes, and a verification operation on a signature with an unknown type, or a type that does not correspond to the type within the public key MUST return INVALID. The expected length of a variable-length object can be determined from its typecode, and if an object has a different length, then any signature computed from the object is INVALID.

[8.](#) Rationale

The goal of this note is to describe the LM-OTS, LMS and HSS

algorithms following the original references and present the modern security analysis of those algorithms. Other signature methods are out of scope and may be interesting follow-on work.

We adopt the techniques described by Leighton and Micali to mitigate attacks that amortize their work over multiple invocations of the hash function.

The values taken by the identifier I across different LMS public/private key pairs are chosen randomly in order to improve security. The analysis of this method in [Fluhrer17] shows that we do not need uniqueness to ensure security; we do need to ensure that we don't have a large number of private keys that use the same I value. By randomly selecting 16 byte I values, the chance that, out of 2^{64} private keys, 4 or more of them will use the same I value is negligible (that is, has probability less than 2^{-128}).

The reason this size was selected was to optimize the Winternitz hash chain operation. With the current settings, the value being hashed is exactly 55 bytes long (for a 32 byte hash function), which SHA-256 can hash in a single hash compression operation. Other hash functions may be used in future specifications; all the ones that we will be likely to support (SHA-512/256 and the various SHA-3 hashes) would work well with a 16 byte I value.

The signature and public key formats are designed so that they are relatively easy to parse. Each format starts with a 32-bit

enumeration value that indicates the details of the signature algorithm and provides all of the information that is needed in order to parse the format.

The Checksum [Section 4.5](#) is calculated using a non-negative integer "sum", whose width was chosen to be an integer number of w -bit fields such that it is capable of holding the difference of the total possible number of applications of the function H as defined in the signing algorithm of [Section 4.6](#) and the total actual number. In the case that the number of times H is applied is 0, the sum is $(2^w - 1) * (8 * n / w)$. Thus for the purposes of this document, which describes signature methods based on $H = \text{SHA256}$ ($n = 32$ bytes) and $w = \{ 1, 2, 4, 8 \}$, the sum variable is a 16-bit non-negative integer for all combinations of n and w . The calculation uses the parameter ls

defined in [Section 4.1](#) and calculated in [Appendix B](#), which indicates the number of bits used in the left-shift operation.

9. History

This is the eighth version of this draft. It has the following changes from previous versions:

Version 08

Added additional test vector with private key

Added appendix with discussion of parameter set trade-offs

Miscellaneous clarifications and typo corrections.

Version 07

Corrected the LMS public key format specification in [section 5.3](#); the format listed in [section 7](#) was correct.

Corrected the LMS public key generation algorithm in [appendix C](#). The hashes listed in [section 5.3](#) were correct.

Corrected the HSS signature verification algorithm in [section 6.3](#).

Miscellaneous clarifications and typo corrections.

Version 06

Modified the order of the values that were hashed to make it easier to prove security.

Decreased the size of the I LMS public key identifier to 16 bytes.

Version 05

Clarified the L=1 specific case.

Extended the parameter sets to include an H=25 option

A large number of corrections and clarifications

Added a comparison to XMSS and SPHINCS, and citations to those algorithms and to the recent Security Standardization Research 2016 publications on the security of LMS and on the state management in hash-based signatures.

Version 04

Specified that, in the HSS method, the I value was computed from the I value of the parent LM tree. Previous versions had the I value extracted from the public key (which meant that all LM trees of a particular level and public key used the same I value)

Changed the length of the I field based on the parameter set. As noted in the Rationale section, this allows an implementation to compute SHA256 n=32 based parameter sets significantly faster.

Modified the XDR of an HSS signature not to use an array of LM signatures; LM signatures are variable length, and XDR doesn't support arrays of variable length structures.

Changed the LMS registry to be in a consistent order with the LM-OTS parameter sets. Also, added LMS parameter sets with height 15 trees

Previous versions

In Algorithms 3 and 4, the message was moved from the initial position of the input to the function H to the final position, in the computation of the intermediate variable Q. This was done to improve security by preventing an attacker that can find a collision in H from taking advantage of that fact via the forward chaining property of Merkle-Damgard.

The Hierarchical Signature Scheme was generalized slightly so that it can use more than two levels.

Several points of confusion were corrected; these had resulted from incomplete or inconsistent changes from the Merkle approach of the earlier draft to the Leighton-Micali approach.

This section is to be removed by the RFC editor upon publication.

10. IANA Considerations

The Internet Assigned Numbers Authority (IANA) is requested to create two registries: one for OTS signatures, which includes all of the LM-OTS signatures as defined in [Section 3](#), and one for Leighton-Micali Signatures, as defined in [Section 4](#). Additions to these registries require that a specification be documented in an RFC or another permanent and readily available reference in sufficient detail that interoperability between independent implementations is possible. Each entry in the registry contains the following elements:

- a short name, such as "LMS_SHA256_M32_H10",

- a positive number, and

- a reference to a specification that completely defines the signature method test cases that can be used to verify the correctness of an implementation.

Requests to add an entry to the registry MUST include the name and the reference. The number is assigned by IANA. Submitters SHOULD have their requests reviewed by the IRTF Crypto Forum Research Group (CFRG) at cfrg@ietf.org. Interested applicants that are unfamiliar with IANA processes should visit <http://www.iana.org>.

The numbers between 0xDDDDDDDD (decimal 3,722,304,989) and 0xFFFFFFFF (decimal 4,294,967,295) inclusive, will not be assigned by IANA, and are reserved for private use; no attempt will be made to prevent multiple sites from using the same value in different (and incompatible) ways [[RFC2434](#)].

The LM-OTS registry is as follows.

Name	Reference	Numeric Identifier
LMOTS_SHA256_N32_W1	Section 4	0x00000001
LMOTS_SHA256_N32_W2	Section 4	0x00000002
LMOTS_SHA256_N32_W4	Section 4	0x00000003
LMOTS_SHA256_N32_W8	Section 4	0x00000004

Table 3

The LMS registry is as follows.

Name	Reference	Numeric Identifier
LMS_SHA256_M32_H5	Section 5	0x00000005
LMS_SHA256_M32_H10	Section 5	0x00000006
LMS_SHA256_M32_H15	Section 5	0x00000007
LMS_SHA256_M32_H20	Section 5	0x00000008
LMS_SHA256_M32_H25	Section 5	0x00000009

Table 4

An IANA registration of a signature system does not constitute an endorsement of that system or its security.

[11.](#) Intellectual Property

This draft is based on U.S. patent 5,432,852, which issued over twenty years ago and is thus expired.

[11.1.](#) Disclaimer

This document is not intended as legal advice. Readers are advised to consult with their own legal advisers if they would like a legal interpretation of their rights.

The IETF policies and processes regarding intellectual property and patents are outlined in [[RFC3979](#)] and [[RFC4879](#)] and at <https://datatracker.ietf.org/ipr/about>.

[12.](#) Security Considerations

The hash function H MUST have second preimage resistance: it must be computationally infeasible for an attacker that is given one message M to be able to find a second message M' such that $H(M) = H(M')$.

The security goal of a signature system is to prevent forgeries. A

successful forgery occurs when an attacker who does not know the private key associated with a public key can find a message and signature that are valid with that public key (that is, the Signature Verification algorithm applied to that signature and message and public key will return VALID). Such an attacker, in the strongest

case, may have the ability to forge valid signatures for an arbitrary number of other messages.

LMS is provably secure in the random oracle model, where the hash compression function is considered the random oracle, as shown by [\[Fluhrer17\]](#). Corollary 1 of that paper states:

If we have no more than 2^{64} randomly chosen LMS private keys, allow the attacker access to a signing oracle and a SHA-256 hash compression oracle, and allow a maximum of 2^{120} hash compression computations, then the probability of an attacker being able to generate a single forgery against any of those LMS keys is less than 2^{-129} .

The format of the inputs to the hash function H have the property that each invocation of that function has an input that is repeated by a small bounded number of other inputs (due to potential repeats of the I value), and in particular, will vary somewhere in the first 23 bytes of the value being hashed. This property is important for a proof of security in the random oracle model. The formats used during key generation and signing are

```
I || u32str(q) || u16str(i) || u8str(j) || tmp
I || u32str(q) || u16str(D_PBLC) || y[0] || ... || y[p-1]
I || u32str(q) || u16str(D_MESG) || C || message
I || u32str(r) || u16str(D_LEAF) || OTS_PUB_HASH[r-2^h]
I || u32str(r) || u16str(D_INTR) || T[2*r] || T[2*r+1]
I || u32str(q) || u16str(j) || u8str(0xff) || SEED
```

Each hash type listed is distinct; at locations 20, 21 of each hash, there exists either a fixed value D_PBLC , D_MESG , D_LEAF , D_INTR , or a 16 bit value (i or j). These fixed values are distinct from each other, and large (over 32768), while the 16 bit values are small (currently no more than 265; possibly being slightly larger if larger hash functions are supported; hence the hash invocations with i/j will not collide any of the D_PBLC , D_MESG , D_LEAF , D_INTR hashes.

The only other collision possibility is the Winternitz chain hash colliding with the recommended pseudorandom key generation process; here, at location 22, the Winternitz chain function has the value $u8str(j)$, where j is a value between 0 and 254, while location 22 of the recommended pseudorandom key generation process has value 255.

For the Winternitz chaining function, D_PBLC , and D_MSG , the value of $I \parallel u32str(q)$ is distinct for each LMS leaf (or equivalently, for each q value). For the Winternitz chaining function, the value of $u16str(i) \parallel u8str(j)$ is distinct for each invocation of H for a given leaf. For D_PBLC and D_MSG , the input format is used only once for each value of q , and thus distinctness is assured. The

formats for D_INTR and D_LEAF are used exactly once for each value of r , which ensures their distinctness. For the recommended pseudorandom key generation process, for a given value of I , q and j are distinct for each invocation of H .

The value of I is chosen uniformly at random from the set of all 128 bit strings. If 2^{64} public keys are generated (and hence 2^{64} random I values), there is a nontrivial probability of a duplicate (which would imply duplicate prefixes. However, there will be an extremely high probability there will not be a four-way collision (that is, any I value used for four distinct LMS keys; probability $< 2^{-132}$), and hence the number of repeats for any specific prefix will be limited to 3. This can be shown (in [\[Fluhrer17\]](#)) to have only a limited effect on the security of the system.

[12.1](#). Stateful signature algorithm

The LMS signature system, like all N-time signature systems, requires that the signer maintain state across different invocations of the signing algorithm, to ensure that none of the component one-time signature systems are used more than once. This section calls out some important practical considerations around this statefulness.

In a typical computing environment, a private key will be stored in non-volatile media such as on a hard drive. Before it is used to sign a message, it will be read into an application's Random Access Memory (RAM). After a signature is generated, the value of the private key will need to be updated by writing the new value of the private key into non-volatile storage. It is essential for security

that the application ensure that this value is actually written into that storage, yet there may be one or more memory caches between it and the application. Memory caching is commonly done in the file system, and in a physical memory unit on the hard disk that is dedicated to that purpose. To ensure that the updated value is written to physical media, the application may need to take several special steps. In a POSIX environment, for instance, the `O_SYNC` flag (for the `open()` system call) will cause invocations of the `write()` system call to block the calling process until the data has been to the underlying hardware. However, if that hardware has its own memory cache, it must be separately dealt with using an operating system or device specific tool such as `hdparm` to flush the on-drive cache, or turn off write caching for that drive. Because these details vary across different operating systems and devices, this note does not attempt to provide complete guidance; instead, we call the implementer's attention to these issues.

When hierarchical signatures are used, an easy way to minimize the private key synchronization issues is to have the private key for the

second level resident in RAM only, and never write that value into non-volatile memory. A new second level public/private key pair will be generated whenever the application (re)starts; thus, failures such as a power outage or application crash are automatically accommodated. Implementations SHOULD use this approach wherever possible.

[12.2.](#) Security of LM-OTS Checksum

To show the security of LM-OTS checksum, we consider the signature y of a message with a private key x and let $h = H(\text{message})$ and $c = \text{Cksm}(H(\text{message}))$ (see [Section 4.6](#)). To attempt a forgery, an attacker may try to change the values of h and c . Let h' and c' denote the values used in the forgery attempt. If for some integer j in the range 0 to u , where $u = \text{ceil}(8 \cdot n/w)$ is the size of the range that the checksum value can cover), inclusive,

$$a' = \text{coef}(h', j, w),$$

$$a = \text{coef}(h, j, w), \text{ and}$$

$$a' > a$$

then the attacker can compute $F^{a'}(x[j])$ from $F^a(x[j]) = y[j]$ by iteratively applying function F to the j^{th} term of the signature an additional $(a' - a)$ times. However, as a result of the increased number of hashing iterations, the checksum value c' will decrease from its original value of c . Thus a valid signature's checksum will have, for some number k in the range u to $(p-1)$, inclusive,

$$\begin{aligned} b' &= \text{coef}(c', k, w), \\ b &= \text{coef}(c, k, w), \text{ and} \\ b' &< b \end{aligned}$$

Due to the one-way property of F , the attacker cannot easily compute $F^{b'}(x[k])$ from $F^b(x[k]) = y[k]$.

[13.](#) Comparison with other work

The eXtended Merkle Signature Scheme (XMSS) [[XMSS](#)] is similar to HSS in several ways. Both are stateful hash based signature schemes, and both use a hierarchical approach, with a Merkle tree at each level of the hierarchy. XMSS signatures are slightly shorter than HSS signatures, for equivalent security and an equal number of signatures.

HSS has several advantages over XMSS. HSS operations are roughly four times faster than the comparable XMSS ones, when SHA256 is used as the underlying hash. This occurs because the hash operation done as a part of the Winternitz iterations dominates performance, and XMSS performs four compression function invocations (two for the PRF, two for the F function) where HSS need only perform one. Additionally, HSS is somewhat simpler, and it allows a single-level tree in a simple way (as described in [Section 6.2](#)).

[14.](#) Acknowledgements

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Law, and Kevin Igoe, who pointed out the security benefits of the approach of Leighton and Micali [[USPT05432852](#)] and Jonathan Katz, who gave us security guidance, and Bruno Couillard and Jim Goodman for an especially thorough review.

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[Appendix A.](#) Pseudorandom Key Generation

An implementation MAY use the following pseudorandom process for generating an LMS private key.

SEED is an m-byte value that is generated uniformly at random at the start of the process,

I is LMS key pair identifier,

q denotes the LMS leaf number of an LM-OTS private key,

x_q denotes the x array of private elements in the LM-OTS private key with leaf number q,

j is an index of the private key element, and

H is the hash function used in LM-OTS.

The elements of the LM-OTS private keys are computed as:

$$x_q[j] = H(I \parallel u32str(q) \parallel u16str(j) \parallel u8str(0xff) \parallel SEED).$$

This process stretches the m-byte random value SEED into a (much larger) set of pseudorandom values, using a unique counter in each invocation of H. The format of the inputs to H are chosen so that they are distinct from all other uses of H in LMS and LM-OTS. A careful reader will note that this is similar to the hash we perform when iterating through the Winternitz chain; however in that chain, the iteration index will vary between 0 and 254 maximum (for W=8), while the corresponding value in this formula is 255. This algorithm is included in the proof of security in [[Fluhrer17](#)] and hence this method is safe when used within the LMS system; however any other cryptographical secure method of generating private keys would also be safe.

[Appendix B](#). LM-OTS Parameter Options

The LM-OTS one time signature method uses several internal parameters, which are a function of the selected parameter set. These internal parameters set:

p - This is the number of independent Winternitz chains used in the signature; it will be the number of w -bit digits needed to hold the n -bit hash (u in the below equations), along with the number of digits needed to hold the checksum (v in the below equations)

ls - This is the size of the shift needed to move the checksum so that it appears in the checksum digits

The parameters ls , and p are computed as follows:

$$\begin{aligned}u &= \text{ceil}(8*n/w) \\v &= \text{ceil}((\text{floor}(\lg((2^w - 1) * u)) + 1) / w) \\ls &= 16 - (v * w) \\p &= u + v\end{aligned}$$

Here u and v represent the number of w -bit fields required to contain the hash of the message and the checksum byte strings, respectively. And as the value of p is the number of w -bit elements of $(H(\text{message}) || \text{Cksm}(H(\text{message})))$, it is also equivalently the number of byte strings that form the private key and the number of byte strings in the signature. The value 16 in the ls computation of ls corresponds to the 16 bits value used for the sum variable in Algorithm 2 in [Section 4.5](#)

A table illustrating various combinations of n and w with the associated values of u , v , ls , and p is provided in Table 5.

Hash Length in Bytes (n)	Winternitz Parameter (w)	w-bit Elements in Hash (u)	w-bit Elements in Checksum (v)	Left Shift (ls)	Total Number of w-bit Elements (p)
32	1	256	9	7	265
32	2	128	5	6	133
32	4	64	3	4	67
32	8	32	2	0	34

Table 5

[Appendix C](#). An iterative algorithm for computing an LMS public key

The LMS public key can be computed using the following algorithm or any equivalent method. The algorithm uses a stack of hashes for data. It also makes use of a hash function with the typical init/update/final interface to hash functions; the result of the invocations `hash_init()`, `hash_update(N[1])`, `hash_update(N[2])`, ..., `hash_update(N[n])`, `v = hash_final()`, in that order, is identical to that of the invocation of `H(N[1] || N[2] || ... || N[n])`.

Generating an LMS Public Key from an LMS Private Key

```
for ( i = 0; i < 2^h; i = i + 1 ) {
    r = i + num_lmots_keys;
    temp = H(I || u32str(r) || u16str(D_LEAF) || OTS_PUB_HASH[i])
    j = i;
    while (j % 2 == 1) {
        r = (r - 1)/2;
        j = (j-1) / 2;
        left_side = pop(data stack);
        temp = H(I || u32str(r) || u16str(D_INTR) || left_side || temp)
    }
    push temp onto the data stack
}
public_key = pop(data stack)
```

Note that this pseudocode expects that all 2^h leaves of the tree have equal depth; that is, `num_lmots_keys` to be a power of 2. The maximum depth of the stack will be $h-1$ elements, that is, a total of $(h-1)*n$ bytes; for the currently defined parameter sets, this will never be more than 768 bytes of data.

[Appendix D](#). Method for deriving authentication path for a signature

The LMS signature consists of `u32str(q) || ots_signature || u32str(type) || path[0] || path[1] || ... || path[h-1]`. This appendix shows one method of constructing the `path[i]` values, assuming that the implementation has stored the `T[]` array that was used to construct the public key. Note that this is not the only possible method; other methods exist which don't assume that you have the entire `T[]` array in memory. To compute `path[i]`, you perform the following computations:

Generating an LMS Path Value

```
r = 2^h + q
temp = (r / 2^i) xor 1
return path[i] = T[temp]
```

where 'xor' is the bitwise exclusive-or operation.

[Appendix E](#). Example Implementation

Two example implementations can be found online at <http://github.com/davidmcgrew/hash-sigs/> and at <http://github.com/cisco/hash-sigs>.

[Appendix F](#). Parameter Set Recommendations

As for guidance as to the number of LMS level, and the size of each, any discussion of performance is implementation specific. In general, the sole drawback for a single LMS tree is the time it takes to generate the public key; as every LM-OTS public key needs to be generated, the time this takes can be substantial. For a two level tree, only the top level LMS tree and the initial bottom level LMS tree needs to be generated initially (before the first signature is generated); this will in general be significantly quicker.

To give a general idea on the trade-offs available, we include some measurements taken with the github.com/cisco/hash-sigs LMS implementation, taken on a 3.3 GHz Xeon processor, with threading enabled. We tried various parameter sets, all with $W=8$ (which minimizes signature size, while increasing time). These are here to give a guideline as to what's possible; for the computational time, your mileage may vary, depending on the computing resources you have. The machine I have does not have the SHA-256 extensions; you could possibly do significantly better.

ParmSet	KeyGenTime	SigSize	KeyLifetime
15	6 sec	1616	30 seconds
20	3 min	1776	16 minutes
25	1.5 hour	1936	9 hours

15/10	6 sec	3172	9 hours
15/15	6 sec	3332	12 days
20/10	3 min	3332	12 days
20/15	3 min	3492	1 year
25/10	1.5 hour	3492	1 year
25/15	1.5 hour	3652	34 years

ParmSet: this is the height of the Merkle tree(s); parameter sets listed as a single integer consists of a single Merkle tree of that height; parameter sets that consist of two trees are listed as x/y, with x being the height of the top level Merkle tree, and y being the bottom level.

KeyGenTime: the measured key generation time; that is, the time needed to generate the public private key pair.

SigSize: the size of a signature (in bytes)

KeyLifetime: the lifetime of a key, assuming we generated 1000 signatures per second. In practice, we're not likely to get anywhere close to 1000 signatures per second sustained; if you have a more appropriate figure for your scenario, this column is pretty easy to recompute.

As for signature generation or verification times, those are moderately insensitive to the above parameter settings (except for the Winternitz setting, and the number of Merkle trees for verification). Tests on the same machine (without multithreading) gave approximately 4msec to sign a short message, 2.6msec to verify; these tests used a two level ParmSet; a single level would approximately halve the verification time. All times can be significantly improved (by maybe a factor of 8) by using a parameter set with W=4; however that also about doubles the signature size.

[Appendix G](#). Test Cases

This section provides test cases that can be used to verify or debug an implementation. This data is formatted with the name of the elements on the left, and the value of the elements on the right, in hexadecimal. The concatenation of all of the values within a public key or signature produces that public key or signature, and values that do not fit within a single line are listed across successive

lines.

Test Case 1 Public Key

```
-----
HSS public key
levels      00000002
-----
LMS type    00000005          # LM_SHA256_M32_H5
LMOTS type  00000004          # LMOTS_SHA256_N32_W8
I           61a5d57d37f5e46bfb7520806b07a1b8
K           50650e3b31fe4a773ea29a07f09cf2ea
           30e579f0df58ef8e298da0434cb2b878
-----
-----
```

Test Case 1 Message

```
-----
Message    54686520706f77657273206e6f742064 |The powers not d|
           656c65676174656420746f2074686520 |elegated to the |
           556e6974656420537461746573206279 |United States by|
           2074686520436f6e737469747574696f | the Constitutio|
           6e2c206e6f722070726f686962697465 |n, nor prohibite|
           6420627920697420746f207468652053 |d by it to the S|
           74617465732c20617265207265736572 |tates, are reser|
           76656420746f20746865205374617465 |ved to the State|
-----
```


y[11]	aaf65de7620dabec29eb82a17fde35af 15ad238c73f81bdb8dec2fc0e7f93270
y[12]	1099762b37f43c4a3c20010a3d72e2f6 06be108d310e639f09ce7286800d9ef8
y[13]	a1a40281cc5a7ea98d2adc7c7400c2fe 5a101552df4e3cccfdf0cbf2ddf5dc677
y[14]	9cbbc68fee0c3efe4ec22b83a2caa3e4 8e0809a0a750b73ccdcf3c79e6580c15
y[15]	4f8a58f7f24335eec5c5eb5e0cf01dcf 4439424095fceb077f66ded5bec73b27
y[16]	c5b9f64a2a9af2f07c05e99e5cf80f00 252e39db32f6c19674f190c9fbc506d8
y[17]	26857713afd2ca6bb85cd8c107347552 f30575a5417816ab4db3f603f2df56fb
y[18]	c413e7d0acd8bdd81352b2471fc1bc4f 1ef296fea1220403466b1afe78b94f7e
y[19]	cf7cc62fb92be14f18c2192384ebceaf 8801afdf947f698ce9c6ceb696ed70e9
y[20]	e87b0144417e8d7baf25eb5f70f09f01 6fc925b4db048ab8d8cb2a661ce3b57a
y[21]	da67571f5dd546fc22cb1f97e0ebd1a6 5926b1234fd04f171cf469c76b884cf3
y[22]	115cce6f792cc84e36da58960c5f1d76 0f32c12faef477e94c92eb75625b6a37
y[23]	1efc72d60ca5e908b3a7dd69fef02491 50e3eebdfed39cbdc3ce9704882a2072
y[24]	c75e13527b7a581a556168783dc1e975 45e31865ddc46b3c957835da252bb732
y[25]	8d3ee2062445dfb85ef8c35f8e1f3371 af34023cef626e0af1e0bc017351aae2
y[26]	ab8f5c612ead0b729a1d059d02bfe18e fa971b7300e882360a93b025ff97e9e0
y[27]	eec0f3f3f13039a17f88b0cf808f4884 31606cb13f9241f40f44e537d302c64a
y[28]	4f1f4ab949b9feefadcb71ab50ef27d6 d6ca8510f150c85fb525bf25703df720
y[29]	9b6066f09c37280d59128d2f0f637c7d 7d7fad4ed1c1ea04e628d221e3d8db77
y[30]	b7c878c9411cafc5071a34a00f4cf077 38912753dfce48f07576f0d4f94f42c6
y[31]	d76f7ce973e9367095ba7e9a3649b7f4 61d9f9ac1332a4d1044c96aefee67676
y[32]	401b64457c54d65fef6500c59cdfb69a f7b6dddfcb0f086278dd8ad0686078df

```
y[33]          b0f3f79cd893d314168648499898fbc0
                ced5f95b74e8ff14d735cdea968bee74
-----
LMS type       00000005                                # LM_SHA256_M32_H5
path[0]        d8b8112f9200a5e50c4a262165bd342c
                d800b8496810bc716277435ac376728d
path[1]        129ac6eda839a6f357b5a04387c5ce97
                382a78f2a4372917eefcbf93f63bb591
path[2]        12f5dbe400bd49e4501e859f885bf073
                6e90a509b30a26bfac8c17b5991c157e
path[3]        b5971115aa39efd8d564a6b90282c316
                8af2d30ef89d51bf14654510a12b8a14
path[4]        4cca1848cf7da59cc2b3d9d0692dd2a2
                0ba3863480e25b1b85ee860c62bf5136
-----
LMS public key
LMS type       00000005                                # LM_SHA256_M32_H5
LMOTS type     00000004                                # LMOTS_SHA256_N32_W8
I              d2f14ff6346af964569f7d6cb880a1b6
K              6c5004917da6eafe4d9ef6c6407b3db0
                e5485b122d9ebe15cda93cfec582d7ab
-----
final_signature:
-----
LMS signature
q              0000000a
-----
LMOTS signature
LMOTS type     00000004                                # LMOTS_SHA256_N32_W8
C              0703c491e7558b35011ece3592eaa5da
                4d918786771233e8353bc4f62323185c
y[0]           95cae05b899e35dff71705470620998
                8ebfdf6e37960bb5c38d7657e8bffeef
y[1]           9bc042da4b4525650485c66d0ce19b31
                7587c6ba4bfffcc428e25d08931e72dfb
y[2]           6a120c5612344258b85efdb7db1db9e1
                865a73caf96557eb39ed3e3f426933ac
y[3]           9eeddb03a1d2374af7bf771855774562
                37f9de2d60113c23f846df26fa942008
y[4]           a698994c0827d90e86d43e0df7f4bfcd
                b09b86a373b98288b7094ad81a0185ac
y[5]           100e4f2c5fc38c003c1ab6fea479eb2f
                5ebe48f584d7159b8ada03586e65ad9c
y[6]           969f6aecbfe44cf356888a7b15a3ff07
                4f771760b26f9c04884ee1faa329fbf4
y[7]           e61af23aee7fa5d4d9a5dfcf43c4c26c
                e8aea2ce8a2990d7ba7b57108b47dabf
```

y[8] beadb2b25b3cacc1ac0cef346cbb90fb

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y[9] 044beee4fac2603a442bdf7e507243b7
319c9944b1586e899d431c7f91bcccc8
690dbf59b28386b2315f3d36ef2eaa3c
y[10] f30b2b51f48b71b003dfb08249484201
043f65f5a3ef6bbd61ddfee81aca9ce6
y[11] 0081262a00000480dcbc9a3da6fbef5c
1c0a55e48a0e729f9184fcb1407c3152
y[12] 9db268f6fe50032a363c9801306837fa
fabdf957fd97eafc80dbd165e435d0e2
y[13] dfd836a28b354023924b6fb7e48bc0b3
ed95eea64c2d402f4d734c8dc26f3ac5
y[14] 91825daef01eae3c38e3328d00a77dc6
57034f287ccb0f0e1c9a7cbdc828f627
y[15] 205e4737b84b58376551d44c12c3c215
c812a0970789c83de51d6ad787271963
y[16] 327f0a5fbb6b5907dec02c9a90934af5
a1c63b72c82653605d1dcce51596b3c2
y[17] b45696689f2eb382007497557692caac
4d57b5de9f5569bc2ad0137fd47fb47e
y[18] 664fcb6db4971f5b3e07aceda9ac130e
9f38182de994cff192ec0e82fd6d4cb7
y[19] f3fe00812589b7a7ce51544045643301
6b84a59bec6619a1c6c0b37dd1450ed4
y[20] f2d8b584410ceda8025f5d2d8dd0d217
6fc1cf2cc06fa8c82bed4d944e71339e
y[21] ce780fd025bd41ec34ebff9d4270a322
4e019fcb444474d482fd2dbe75efb203
y[22] 89cc10cd600abb54c47ede93e08c114e
db04117d714dc1d525e11bed8756192f
y[23] 929d15462b939ff3f52f2252da2ed64d
8fae88818b1efa2c7b08c8794fb1b214
y[24] aa233db3162833141ea4383f1a6f120b
e1db82ce3630b3429114463157a64e91
y[25] 234d475e2f79cbf05e4db6a9407d72c6
bff7d1198b5c4d6aad2831db61274993
y[26] 715a0182c7dc8089e32c8531deed4f74
31c07c02195eba2ef91efb5613c37af7
y[27] ae0c066bab69369700e1dd26eddc0d2
16c781d56e4ce47e3303fa73007ff7b9
y[28] 49ef23be2aa4dbf25206fe45c20dd888

	395b2526391a724996a44156beac8082
y[29]	12858792bf8e74cba49dee5e8812e019
	da87454bfff9e847ed83db07af3137430
y[30]	82f880a278f682c2bd0ad6887cb59f65
	2e155987d61bbf6a88d36ee93b6072e6
y[31]	656d9ccbaae3d655852e38deb3a2dcf8
	058dc9fb6f2ab3d3b3539eb77b248a66
y[32]	1091d05eb6e2f297774fe6053598457c

y[33]	c61908318de4b826f0fc86d4bb117d33	
	e865aa805009cc2918d9c2f840c4da43	
	a703ad9f5b5806163d7161696b5a0adc	

LMS type	00000005	# LM_SHA256_M32_H5
path[0]	d5c0d1bebb06048ed6fe2ef2c6cef305	
	b3ed633941ebc8b3bec9738754cddd60	
path[1]	e1920ada52f43d055b5031cee6192520	
	d6a5115514851ce7fd448d4a39fae2ab	
path[2]	2335b525f484e9b40d6a4a969394843b	
	dcf6d14c48e8015e08ab92662c05c6e9	
path[3]	f90b65a7a6201689999f32bfd368e5e3	
	ec9cb70ac7b8399003f175c40885081a	
path[4]	09ab3034911fe125631051df0408b394	
	6b0bde790911e8978ba07dd56c73e7ee	

Test Case 2 Private Key

(note: procedure in [Appendix A](#) is used)

SEED	000102030405060708090a0b0c0d0e0f
	101112131415161718191a1b1c1d1e1f
I	d08fabd4a2091ff0a8cb4ed834e74534

Test Case 2 Public Key

HSS public key	
levels	00000002

LMS type	00000006	# LM_SHA256_M32_H10
----------	----------	---------------------

```
LMOTS type 00000003 # LMOTS_SHA256_N32_W4
I d08fabd4a2091ff0a8cb4ed834e74534
K 32a58885cd9ba0431235466bff9651c6
  c92124404d45fa53cf161c28f1ad5a8e
-----
-----
```

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Test Case 2 Message

```
-----
Message 54686520656e756d65726174696f6e20 The enumeration
        696e2074686520436f6e737469747574 in the Constitut
        696f6e2c206f66206365727461696e20 ion, of certain
        7269676874732c207368616c6c206e6f rights, shall no
        7420626520636f6e7374727565642074 t be construed t
        6f2064656e79206f7220646973706172 o deny or dispar
        616765206f7468657273207265746169 age others retai
        6e6564206279207468652070656f706c ned by the peopl
        652e0a e..
-----
```

Test Case 2 Signature

HSS signature

Nspk 00000001

sig[0]:

LMS signature

q 00000003

LMOTS signature

LMOTS type 00000003

LMOTS_SHA256_N32_W4

C	3d46bee8660f8f215d3f96408a7a64cf 1c4da02b63a55f62c666ef5707a914ce
y[0]	0674e8cb7a55f0c48d484f31f3aa4af9 719a74f22cf823b94431d01c926e2a76
y[1]	bb71226d279700ec81c9e95fb11a0d10 d065279a5796e265ae17737c44eb8c59
y[2]	4508e126a9a7870bf4360820bdeb9a01 d9693779e416828e75bddd7d8c70d50a
y[3]	0ac8ba39810909d445f44cb5bb58de73 7e60cb4345302786ef2c6b14af212ca1
y[4]	9edea3bfcfe8baa6621ce88480df237 1dd37add732c9de4ea2ce0dffa53c926
y[5]	49a18d39a50788f4652987f226a1d481 68205df6ae7c58e049a25d4907edc1aa
y[6]	90da8aa5e5f7671773e941d805536021 5c6b60dd35463cf2240a9c06d694e9cb
y[7]	54e7b1e1bf494d0d1a28c0d31acc7516 1f4f485dfd3cb9578e836ec2dc722f37
y[8]	ed30872e07f2b8bd0374eb57d22c614e 09150f6c0d8774a39a6e168211035dc5
y[9]	2988ab46eaca9ec597fb18b4936e66ef 2f0df26e8d1e34da28cbb3af75231372

y[10]	0c7b345434f72d65314328bbb030d0f0 f6d5e47b28ea91008fb11b05017705a8
y[11]	be3b2adb83c60a54f9d1d1b2f476f9e3 93eb5695203d2ba6ad815e6a111ea293
y[12]	dcc21033f9453d49c8e5a6387f588b1e a4f706217c151e05f55a6eb7997be09d
y[13]	56a326a32f9cba1fbe1c07bb49fa04ce cf9df1a1b815483c75d7a27cc88ad1b1
y[14]	238e5ea986b53e087045723ce16187ed a22e33b2c70709e53251025abde89396
y[15]	45fc8c0693e97763928f00b2e3c75af3 942d8ddaee81b59a6f1f67efda0ef81d
y[16]	11873b59137f67800b35e81b01563d18 7c4a1575a1acb92d087b517a8833383f
y[17]	05d357ef4678de0c57ff9f1b2da61dfd e5d88318bcdde4d9061cc75c2de3cd47
y[18]	40dd7739ca3ef66f1930026f47d9ebaa 713b07176f76f953e1c2e7f8f271a6ca
y[19]	375dbfb83d719b1635a7d8a138919579

y[20]	44b1c29bb101913e166e11bd5f34186f a6c0a555c9026b256a6860f4866bd6d0 b5bf90627086c6149133f8282ce6c9b3
y[21]	622442443d5eca959d6c14ca8389d12c 4068b503e4e3c39b635bea245d9d05a2
y[22]	558f249c9661c0427d2e489ca5b5dde2 20a90333f4862aec793223c781997da9
y[23]	8266c12c50ea28b2c438e7a379eb106e ca0c7fd6006e9bf612f3ea0a454ba3bd
y[24]	b76e8027992e60de01e9094fddeb3349 883914fb17a9621ab929d970d101e45f
y[25]	8278c14b032bcab02bd15692d21b6c5c 204abbf077d465553bd6eda645e6c306
y[26]	5d33b10d518a61e15ed0f092c3222628 1a29c8a0f50cde0a8c66236e29c2f310
y[27]	a375cebda1dc6bb9a1a01dae6c7aba8e bedc6371a7d52aacb955f83bd6e4f84d
y[28]	2949dcc198fb77c7e5cdf6040b0f84fa f82808bf985577f0a2acf2ec7ed7c0b0
y[29]	ae8a270e951743ff23e0b2dd12e9c3c8 28fb5598a22461af94d568f29240ba28
y[30]	20c4591f71c088f96e095dd98beae456 579ebbbba36f6d9ca2613d1c26eee4d8c
y[31]	73217ac5962b5f3147b492e8831597fd 89b64aa7fde82e1974d2f6779504dc21
y[32]	435eb3109350756b9fdabe1c6f368081 bd40b27ebcb9819a75d7df8bb07bb05d
y[33]	b1bab705a4b7e37125186339464ad8fa aa4f052cc1272919fde3e025bb64aa8e

y[34]	0eb1fcbfcc25acb5f718ce4f7c2182fb 393a1814b0e942490e52d3bca817b2b2
y[35]	6e90d4c9b0cc38608a6cef5eb153af08 58acc867c9922aed43bb67d7b33acc51
y[36]	9313d28d41a5c6fe6cf3595dd5ee63f0 a4c4065a083590b275788bee7ad875a7
y[37]	f88dd73720708c6c6c0ecf1f43bbaada e6f208557fdc07bd4ed91f88ce4c0de8
y[38]	42761c70c186bfdafafc444834bd3418 be4253a71eaf41d718753ad07754ca3e
y[39]	ffd5960b0336981795721426803599ed 5b2b7516920efcbe32ada4bcf6c73bd2

y[40]	9e3fa152d9adeca36020fdeeee1b7395 21d3ea8c0da497003df1513897b0f547
y[41]	94a873670b8d93bcca2ae47e64424b74 23e1f078d9554bb5232cc6de8aae9b83
y[42]	fa5b9510beb39ccf4b4e1d9c0f19d5e1 7f58e5b8705d9a6837a7d9bf99cd1338
y[43]	7af256a8491671f1f2f22af253bcff54 b673199bdb7d05d81064ef05f80f0153
y[44]	d0be7919684b23da8d42ff3effdb7ca0 985033f389181f47659138003d712b5e
y[45]	c0a614d31cc7487f52de8664916af79c 98456b2c94a8038083db55391e347586
y[46]	2250274a1de2584fec975fb09536792c fbfcf6192856cc76eb5b13dc4709e2f7
y[47]	301ddff26ec1b23de2d188c999166c74 e1e14bbc15f457cf4e471ae13dcbdd9c
y[48]	50f4d646fc6278e8fe7eb6cb5c94100f a870187380b777ed19d7868fd8ca7ceb
y[49]	7fa7d5cc861c5bdac98e7495eb0a2cee c1924ae979f44c5390ebedddc65d6ec1
y[50]	1287d978b8df064219bc5679f7d7b264 a76ff272b2ac9f2f7cfc9fdc fb6a5142
y[51]	8240027afd9d52a79b647c90c2709e06 0ed70f87299dd798d68f4fadd3da6c51
y[52]	d839f851f98f67840b964ebe73f8cec4 1572538ec6bc131034ca2894eb736b3b
y[53]	da93d9f5f6fa6f6c0f03ce43362b8414 940355fb54d3dfdd03633ae108f3de3e
y[54]	bc85a3ff51efeea3bc2cf27e1658f178 9ee612c83d0f5fd56f7cd071930e2946
y[55]	beeecaa04dccea9f97786001475e0294 bc2852f62eb5d39bb9fbee75916efe4
y[56]	4a662ecae37ede27e9d6eadfdeb8f8b2 b2dbccbf96fa6dbaf7321fb0e701f4d4
y[57]	29c2f4dcd153a2742574126e5eaccc77 686acf6e3ee48f423766e0fc466810a9

y[58]	05ff5453ec99897b56bc55dd49b99114 2f65043f2d744eeb935ba7f4ef23cf80
y[59]	cc5a8a335d3619d781e7454826df720e ec82e06034c44699b5f0c44a8787752e
y[60]	057fa3419b5bb0e25d30981e41cb1361

```

y[61] 322dba8f69931cf42fad3f3bce6ded5b
8bfc3d20a2148861b2afc14562ddd27f
12897abf0685288dcc5c4982f8260268
y[62] 46a24bf77e383c7aacab1ab692b29ed8
c018a65f3dc2b87ff619a633c41b4fad
y[63] b1c78725c1f8f922f6009787b1964247
df0136b1bc614ab575c59a16d089917b
y[64] d4a8b6f04d95c581279a139be09fcf6e
98a470a0bceca191fce476f9370021cb
y[65] c05518a7efd35d89d8577c990a5e1996
1ba16203c959c91829ba7497cfffcb4b
y[66] 294546454fa5388a23a22e805a5ca35f
956598848bda678615fec28afd5da61a
-----
LMS type 00000006 # LM_SHA256_M32_H10
path[0] b326493313053ced3876db9d23714818
1b7173bc7d042cefb4dbe94d2e58cd21
path[1] a769db4657a103279ba8ef3a629ca84e
e836172a9c50e51f45581741cf808315
path[2] 0b491cb4ecbbabec128e7c81a46e62a6
7b57640a0a78be1cbf7dd9d419a10cd8
path[3] 686d16621a80816bfdb5bdc56211d72c
a70b81f1117d129529a7570cf79cf52a
path[4] 7028a48538ecdd3b38d3d5d62d262465
95c4fb73a525a5ed2c30524ebb1d8cc8
path[5] 2e0c19bc4977c6898ff95fd3d310b0ba
e71696cef93c6a552456bf96e9d075e3
path[6] 83bb7543c675842bafbfc7cdb88483b3
276c29d4f0a341c2d406e40d4653b7e4
path[7] d045851acf6a0a0ea9c710b805cced46
35ee8c107362f0fc8d80c14d0ac49c51
path[8] 6703d26d14752f34c1c0d2c4247581c1
8c2cf4de48e9ce949be7c888e9caebe4
path[9] a415e291fd107d21dc1f084b11582082
49f28f4f7c7e931ba7b3bd0d824a4570
-----
LMS public key
LMS type 00000005 # LM_SHA256_M32_H5
LMOTS type 00000004 # LMOTS_SHA256_N32_W8
I 215f83b7ccb9acbcd08db97b0d04dc2b
K a1cd035833e0e90059603f26e07ad2aa
d152338e7a5e5984bcd5f7bb4eba40b7
-----

```

final_signature:

LMS signature

q 00000004

LMOTS signature

LMOTS type 00000004

LMOTS_SHA256_N32_W8

C 0eb1ed54a2460d512388cad533138d24
0534e97b1e82d33bd927d201dfc24ebb
y[0] 11b3649023696f85150b189e50c00e98
850ac343a77b3638319c347d7310269d
y[1] 3b7714fa406b8c35b021d54d4fdada7b
9ce5d4ba5b06719e72aaf58c5aae7aca
y[2] 057aa0e2e74e7dcfd17a0823429db629
65b7d563c57b4cec942cc865e29c1dad
y[3] 83cac8b4d61aacc457f336e6a10b6632
3f5887bf3523dfcadee158503bfaa89d
y[4] c6bf59daa82afd2b5ebb2a9ca6572a60
67cee7c327e9039b3b6ea6aledc7fdc3
y[5] df927aade10c1c9f2d5ff446450d2a39
98d0f9f6202b5e07c3f97d2458c69d3c
y[6] 8190643978d7a7f4d64e97e3f1c4a08a
7c5bc03fd55682c017e2907eab07e5bb
y[7] 2f190143475a6043d5e6d5263471f4ee
cf6e2575fbc6ff37edfa249d6cda1a09
y[8] f797fd5a3cd53a066700f45863f04b6c
8a58cfd341241e002d0d2c0217472bf1
y[9] 8b636ae547c1771368d9f317835c9b0e
f430b3df4034f6af00d0da44f4af7800
y[10] bc7a5cf8a5abdb12dc718b559b74cab9
090e33cc58a955300981c420c4da8ffd
y[11] 67df540890a062fe40dba8b2c1c548ce
d22473219c534911d48ccaabfb71bc71
y[12] 862f4a24ebd376d288fd4e6fb06ed870
5787c5fedc813cd2697e5b1aac1ced45
y[13] 767b14ce88409eaebb601a93559aae89
3e143d1c395bc326da821d79a9ed41dc
y[14] fbe549147f71c092f4f3ac522b5cc572
90706650487bae9bb5671ecc9ccc2ce5
y[15] 1ead87ac01985268521222fb9057df7e
d41810b5ef0d4f7cc67368c90f573b1a
y[16] c2ce956c365ed38e893ce7b2fae15d36
85a3df2fa3d4cc098fa57dd60d2c9754
y[17] a8ade980ad0f93f6787075c3f680a2ba
1936a8c61d1af52ab7e21f416be09d2a
y[18] 8d64c3d3d8582968c2839902229f85ae
e297e717c094c8df4a23bb5db658dd37
y[19] 7bf0f4ff3ffd8fba5e383a48574802ed

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y[20]	545bbe7a6b4753533353d73706067640 135a7ce517279cd683039747d218647c 86e097b0daa2872d54b8f3e508598762
y[21]	9547b830d8118161b65079fe7bc59a99 e9c3c7380e3e70b7138fe5d9be255150
y[22]	2b698d09ae193972f27d40f38dea264a 0126e637d74ae4c92a6249fa103436d3
y[23]	eb0d4029ac712bfc7a5eacbdd7518d6d 4fe903a5ae65527cd65bb0d4e9925ca2
y[24]	4fd7214dc617c150544e423f450c99ce 51ac8005d33acd74f1bed3b17b7266a4
y[25]	a3bb86da7eba80b101e15cb79de9a207 852cf91249ef480619ff2af8cabca831
y[26]	25d1faa94cbb0a03a906f683b3f47a97 c871fd513e510a7a25f283b196075778
y[27]	496152a91c2bf9da76ebe089f4654877 f2d586ae7149c406e663eadeb2b5c7e8
y[28]	2429b9e8cb4834c83464f079995332e4 b3c8f5a72bb4b8c6f74b0d45dc6c1f79
y[29]	952c0b7420df525e37c15377b5f09843 19c3993921e5ccd97e097592064530d3
y[30]	3de3afad5733cbe7703c5296263f7734 2efbf5a04755b0b3c997c4328463e84c
y[31]	aa2de3ffdc297baaaacd7ae646e44b5 c0f16044df38fabd296a47b3a838a913
y[32]	982fb2e370c078edb042c84db34ce36b 46ccb76460a690cc86c302457dd1cde1
y[33]	97ec8075e82b393d542075134e2a17ee 70a5e187075d03ae3c853cff60729ba4

LMS type	00000005	# LM_SHA256_M32_H5
path[0]	4de1f6965bdabc676c5a4dc7c35f97f8 2cb0e31c68d04f1dad96314ff09e6b3d	
path[1]	e96ae300d1f68bf1bca9fc58e40323 36cd819aaf578744e50d1357a0e42867	
path[2]	04d341aa0a337b19fe4bc43c2e79964d 4f351089f2e0e41c7c43ae0d49e7f404	
path[3]	b0f75be80ea3af098c9752420a8ac0ea 2bbb1f4eeba05238aef0d8ce63f0c6e5	
path[4]	e4041d95398a6f7f3e0ee97cc1591849 d4ed236338b147abde9f51ef9fd4e1c1	

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