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Using the ECC Brainpool Curves for IKEv2 Key Exchange  
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## Abstract

This document specifies the use of the ECC Brainpool elliptic curve groups for key exchange in the Internet Key Exchange version 2 (IKEv2) protocol.

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## 1. Introduction

In [RFC 5639](#) [[RFC5639](#)], a new set of elliptic curve groups over finite prime fields for use in cryptographic applications was specified. These groups, denoted as Brainpool curves, were generated in a verifiably pseudo-random way and comply with the security requirements of relevant standards from ISO [[IS01](#)] [[IS02](#)], ANSI [[ANSI1](#)], NIST [[FIPS](#)], and SecG [[SEC2](#)].

While the ASN.1 object identifiers defined in [RFC 5639](#) allow usage of the ECC Brainpool curves in certificates and certificate revocation lists, their utilization for key exchange in IKEv2 [[RFC4306](#)] requires the definition and assignment of additional transform IDs in the respective IANA registry. Furthermore, the encoding of the key exchange payload and derivation of the shared secret are defined, because previous RFCs specified this encoding only for the curves proposed therein.

## [2.](#) IKEv2 Key Exchange using the ECC Brainpool Curves

### [2.1.](#) Diffie-Hellman Group Transform IDs

In order to use the Brainpool curves for key exchange within IKEv2, the Diffie-Hellman Group Transform IDs (Transform Type 4) listed in the following table are to be registered with IANA [[IANA-IKE2](#)]. The parameters associated with these curves are defined in [RFC 5639](#) [[RFC5639](#)].

Curve	Transform ID
brainpoolP160r1	TBD1
brainpoolP160t1	TBD2
brainpoolP192r1	TBD3
brainpoolP192t1	TBD4
brainpoolP224r1	TBD5
brainpoolP224t1	TBD6
brainpoolP256r1	TBD7
brainpoolP256t1	TBD8

brainpoolP320r1	TBD9
brainpoolP320t1	TBD10
brainpoolP384r1	TBD11
brainpoolP384t1	TBD12
brainpoolP512r1	TBD13
brainpoolP512t1	TBD14

Table 1

Test vectors for the groups defined by the Brainpool curves are provided in [Appendix A](#)

## [2.2](#). Key Exchange Payload and Shared Secret

[RFC4306](#) [[RFC4306](#)] only specifies the use of MODP groups and  $GF[2^N]$  elliptic curve groups for Diffie-Hellman key exchange with IKEv2. For Diffie-Hellman groups of elliptic curves defined over prime fields (ECP Diffie-Hellman groups), however, the format of key exchange payloads and the derivation of a shared secret has thus far not been specified generally but on a group-by-group basis. To accomodate for different bandwidth limitations, for the groups defined in this document, two different methods for encoding the key exchange payload, compressed and uncompressed, are specified.

In an ECP key exchange, the Diffie-Hellman public value passed in a KE payload consists of two components, x and y, corresponding to the coordinates of an elliptic curve point. Each component MUST be computed from the corresponding coordinate using the FieldElement-to-OctetString conversion method specified in [[SEC1](#)] and MUST have bit length as indicated in Table 2. This length is enforced by the FieldElement-to-OctetString conversion method, if necessary, by prepending the value with zeros.

+-----+-----+

Curves	Bit lengths
brainpoolP160r1 or brainpoolP160t1	160
brainpoolP192r1 or brainpoolP192t1	191
brainpoolP224r1 or brainpoolP224t1	224
brainpoolP256r1 or brainpoolP256t1	256
brainpoolP320r1 or brainpoolP320t1	320
brainpoolP384r1 or brainpoolP384t1	384
brainpoolP512r1 or brainpoolP512t1	512

Table 2

From these components, the key exchange payload MUST be computed using one of the two following encodings.

1. Uncompressed. This method equals the method specified in [RFC 5903](#) [RFC5903] for the ECP curves proposed therein. The key exchange payload is defined as the concatenation of the x and y coordinates. Using this method, the bit length of the key

exchange payload is twice the bit length of each component listed in Table 2. If a peer receives a key exchange payload for an ECC Brainpool curve having twice the bitlength indicated for that curve in Table 2, it MUST assume that the uncompressed encoding has been used.

2. Compressed. The key exchange payload is defined as x. Using this method, the bit length of the key exchange payload equals the bit length of each component listed in Table 2. If a peer receives a key exchange payload for an ECC Brainpool curve having the bitlength indicated for that curve in Table 2, it MUST assume that the compressed encoding has been used.

The Diffie-Hellman shared secret value MUST be computed from the x coordinate of the Diffie-Hellman common value using the FieldElement-

to-OctetString conversion method specified in [\[SEC1\]](#) and MUST have bit length as indicated in the Table 2. The parties MUST verify that the Diffie-Hellman common value is not the "point at infinity", i.e. that the shared secret derived contains non-zero octets.

When compressed encoding is used, computation of the Diffie-Hellman common value, and hence, of the shared secret value from the x-coordinate transmitted in the key exchange payload requires recovery of a corresponding y-coordinate. Since there are up to two possible points on the elliptic curve having a given x-coordinate, the recovered y-component is not unique. However, as explained in [\[RFC6090\]](#), any of the two y-coordinates corresponding to the x-value transmitted in the key exchange payload can be used to compute the Diffie-Hellman common value.

### [3.](#) Security Considerations

The level of security provided by the authentication method in IKEv2 and the symmetric encryption and message integrity protection in IPSEc should roughly match or exceed the level provided by the group chosen for key exchange. [RFC 5639](#) gives guidance in selection symmetric key sizes and hash functions for the ECC Brainpool curves. Furthermore, the security considerations of [\[RFC4306\]](#) apply as well.





Before this document can become an RFC, IANA is required to update the Transform Type 4 (Diffie-Hellman Group Transform) IDs in its Internet Key Exchange Version 2 (IKEv2) Parameters registry [[IANA-IKE2](#)]. In particular, numbers are to be assigned to the 14 groups specified in Table 1. Another I-D is being submitted for publication as RFC [[BP\\_IKE](#)] requesting assignment for the same groups in the corresponding registry for IKEv1; in order to keep the registries for IKEv1 and IKEv2 in accordance, it is advisable to assign the same values in both registries.

## [5.](#) Intellectual Property Rights

Although, the authors have no knowledge about any intellectual property rights which cover the general usage of the ECP groups defined herein, implementations based on these domain parameters may require use of inventions covered by patent rights. In particular, the compressed encoding method for the key exchange payload defined in [Section 2.2](#) may be covered by patents.

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## [6.](#) References

### [6.1.](#) Normative References

- [IANA-IKE2]    Internet Assigned Numbers Authority, "Internet Key Exchange Version 2 (IKEv2) Parameters",  
              <http://www.iana.org/assignments/ikev2-parameters>.
- [RFC2119]    Bradner, S., "Key words for use in RFCs to Indicate Requirement Levels", [BCP 14](#), [RFC 2119](#), March 1997.
- [RFC4306]    Kaufman, C., "Internet Key Exchange (IKEv2) Protocol", [RFC 4306](#), December 2005.
- [RFC5639]    Lochter, M. and J. Merkle, "Elliptic Curve Cryptography (ECC) Brainpool Standard Curves and Curve Generation", [RFC 5639](#), March 2010.

### [6.2.](#) Informative References

- [ANSI1]    American National Standards Institute, "Public Key Cryptography For The Financial Services Industry: The Elliptic Curve Digital Signature Algorithm (ECDSA)", ANSI X9.62, 2005.
- [FIPS]    National Institute of Standards and Technology, "Digital Signature Standard (DSS)", FIPS PUB 186-2, December 1998.
- [BP\_IKE]    Harkins, D., "Brainpool Elliptic Curves for the IKE Group Description Registry",  
              [draft-harkins-brainpool-ike-groups-00](#) (work in progress), August 2012.
- [ISO1]    International Organization for Standardization, "Information Technology - Security Techniques - Digital Signatures with Appendix - Part 3: Discrete Logarithm Based Mechanisms", ISO/IEC 14888-3, 2006.

- [IS02] International Organization for Standardization, "Information Technology - Security Techniques - Cryptographic Techniques Based on Elliptic Curves - Part 2: Digital signatures", ISO/IEC 15946-2, 2002.
- [RFC5903] Fu, D. and J. Solinas, "Elliptic Curve Groups modulo a Prime (ECP Groups) for IKE and IKEv2", [RFC 5903](#), June 2010.

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- [RFC6090] McGrew, D., Igoe, K., and M. Salter, "Fundamental Elliptic Curve Cryptography Algorithms", [RFC 6090](#), February 2011.
- [SEC1] Certicom Research, "Elliptic Curve Cryptography", Standards for Efficient Cryptography (SEC) 1, September 2000.
- [SEC2] Certicom Research, "Recommended Elliptic Curve Domain Parameters", Standards for Efficient Cryptography (SEC) 2, September 2000.

## [Appendix A](#). Test Vectors

This section provides some test vectors for example Diffie-Hellman key exchanges using each of the curves defined in [Section 2](#) . In all of the following sections the following notation is used:

$d_A$ : the secret key of party A

$x_{qA}$ : the x-coordinate of the public key of party A

$y_{qA}$ : the y-coordinate of the public key of party A

$d_B$ : the secret key of party B

$x_{qB}$ : the x-coordinate of the public key of party B

$y_{qB}$ : the y-coordinate of the public key of party B

$x_Z$ : the x-coordinate of the shared secret that results from completion of the Diffie-Hellman computation

$y_Z$ : the y-coordinate of the shared secret that results from completion of the Diffie-Hellman computation

The field elements  $x_{qA}$ ,  $y_{qA}$ ,  $x_{qB}$ ,  $y_{qB}$ ,  $x_Z$ ,  $y_Z$  are represented

as hexadecimal values using the FieldElement-to-OctetString conversion method specified in [[SEC1](#)].

#### [A.1.](#) 160 Bit Curves

Curve brainpoolP160r1

```
dA = 8BF7BC5CBE8AC8B34940C2C5652D6AE4EC9F53CE
x_qA = 651DA24C7FF64DD863F8F650E53F07B8EC943C39
y_qA = D1C68C656E44034D0DAD60A1589FD49594E7C2A4
dB = B6F7160F0DE61CCEAAC528A32BD7AD942E8017B2
x_qB = DF9F259AEA6DFA1F28B16B8FEC52044CC1DFBA35
y_qB = DF72AEA65A5E3EF69166DA161ABE00FC9C81C4D0
x_Z = D78792AC4CBE3390DDD6557060066BC25579CA97
y_Z = 3A3DAB50421585FB9DE9D87BB3BBBAFE3379A571
```

Twisted Curve brainpoolP160t1

```
dA = A1FED74247778596E0FFEA292DF215D291FB8A6A
x_qA = 1CDBF3D03C8CE04183600B99F80661129AB17B64
y_qA = 5FF702E42CFEB890329439CD9594FB26D52CDCC5
dB = A98B640213F32546F7A527EA7C75EACDADC001AB
x_qB = D7FB21ED2FD367B21B663C77ECD233FE97B7B39B
y_qB = A475B6F2BDB551A8303262814C2A5B1F3C77009C
x_Z = 87BFBDB38B161DA82C7696F80403610213419FF5
y_Z = 51D2ECA90C28ACBD7162A7700EB7FD3D60D9722B
```

## [A.2.](#) 192 Bit Curves

Curve brainpoolP192r1

dA = 4B32E699290E3F052A99C7F0CFFD1C5707898015C743FE2A

x\_qA = 31DB86048351629CFCA68541D65D909A0F1DC8E77AC440B2

y\_qA = 7FB2925E1FDC609CF2252F0469836BA4F216ADF8A812893D

dB = 6916B2A336B3305A256238EA2BAB549D9C893F47D07964B8

x\_qB = 15B795C67C5E47510116B0DE419C45835C209AE77D971536

y\_qB = 0D1ADD9881EF6115EDF5B5CEF854B42E435CD9260A5719FB

x\_Z = B946A6914877922A40F6D588D47FC7D44691C346FD384570

y\_Z = AAD4E9CBC5BB6C7C308A95F445287580A09EBC93624FB24E

Twisted Curve brainpoolP192t1

dA = BA0D8C324347CD29B6EBC40540A4EB46C293F18E799E4748

x\_qA = 29541AD06E6BC4C3CF28D7D0A505037D527A165889AF2646

y\_qA = 0222140F457C044F5F585E5943A7411BCF7B95676C938E9C

dB = 479499E64FF4F30A5F4F08B1A451A113B166A32328ED549B

x\_qB = 885FC460B907C9F7C1CF91C7C6AD3BF6343F381D06139021

y\_qB = 704257DFF34C99B623FE6DF24A2719B9D5901285519977EB

x\_Z = 1C6BE551CA60C6D24AF434915A381FBDC9EC934F4DB73257

y\_Z = 110BA8C4446A689F1A526087DF8A9A620F75286F36B07014

## [A.3.](#) 224 Bit Curves

Curve brainpoolP224r1

dA = 39F155483CEE191FBECFE9C81D8AB1A03CDA6790E7184ACE44BCA161  
x\_qA = A9C21A569759DA95E0387041184261440327AFE33141CA04B82DC92E  
y\_qA = 98A0F75FBBF61D8E58AE5511B2BCDBE8E549B31E37069A2825F590C1  
dB = 6060552303899E2140715816C45B57D9B42204FB6A5BF5BEAC10DB00  
x\_qB = 034A56C550FF88056144E6DD56070F54B0135976B5BF77827313F36B  
y\_qB = 75165AD99347DC86CAAB1CBB579E198EAF88DC35F927B358AA683681  
x\_Z = 1A4BFE705445120C8E3E026699054104510D119757B74D5FE2462C66  
y\_Z = BB6802AC01F8B7E91B1A1ACFB9830A95C079CEC48E52805DFD7D2AFE

Twisted Curve brainpoolP224t1

dA = B9324E65766C765036E8AFBD2611864C195F893B9256F40AA23B2738  
x\_qA = 3DA543100518A53531EBB3D1C14514C13EECA0A78CE92E71E2546FC1  
y\_qA = 67580D56C0C89AF632911B3F99934CA2AB154E7E6F5E47CB2980E084  
dB = C9452FA256A710BEA19DFE6C7B4A848F82C2586BB815909B0C8099D6  
x\_qB = 5DC490CFBD576B1DAC7462BE6B567CA371A108BB3CD3609F0C33C679B  
y\_qB = 8FBAB24A248B676DF9D739478ABCCD593169297F2DEC2552C3F8DA0  
x\_Z = 62F1A83BE792608C1D2Aafb229779B47D3F88B1EE2F9686E8CD8EF3C  
y\_Z = B7F4B16BE902487127A605FED0069CB451CC56E0F9186B462D8BDD04

#### [A.4.](#) 256 Bit Curves

Curve brainpoolP256r1



dA =  
81DB1EE100150FF2EA338D708271BE38300CB54241D79950F77B063039804F1D

x\_qA =  
44106E913F92BC02A1705D9953A8414DB95E1AAA49E81D9E85F929A8E3100BE5

y\_qA =  
8AB4846F11CACCB73CE49CBDD120F5A900A69FD32C272223F789EF10EB089BDC

dB =  
55E40BC41E37E3E2AD25C3C6654511FFA8474A91A0032087593852D3E7D76BD3

x\_qB =  
8D2D688C6CF93E1160AD04CC4429117DC2C41825E1E9FCA0ADDD34E6F1B39F7B

y\_qB =  
990C57520812BE512641E47034832106BC7D3E8DD0E4C7F1136D7006547CEC6A

x\_Z =  
89AFC39D41D3B327814B80940B042590F96556EC91E6AE7939BCE31F3A18BF2B

y\_Z =  
49C27868F4ECA2179BFD7D59B1E3BF34C1DBDE61AE12931648F43E59632504DE

Twisted Curve brainpoolP256t1

dA =  
67CF7C2A6537E1E135C131B06958D388B97AC6173A2E669103A6F55EFCA51726

x\_qA =  
356AEB7B004AD59A48E46373BF2D413A52987BF8FE7073729AB56920C4B2FFE1

y\_qA =  
791116DEA74A3724F84F68ED3E18F01E3B9ABD90A26E38028322066FD7A09BAF

dB =  
A74E29848D27882B6B7817694CC82EE81330AF856F243939B5F8B57CE59FD7EC

x\_qB =  
7D9FD6B1FAAF13C9C34DD8D713E9759D7A0F7E34206B8566C8D771C02871A702

y\_qB =  
45A49EDEBA249C9DBB0FE8B42CF4765650DB68C84B4BD467BE151E6D6C60F5C1

$x_Z =$

A0AF0A63DE5579343129183FF958582A19D63DDBAAA91E07536421DEAB1064AF

$y_Z =$

78162E9FB4E2E0CA1F7B30ED51685864F9AB1B59E40E0E8DA046D4E897A77DD7

#### [A.5.](#) 320 Bit Curves

Curve brainpoolP320r1

$dA =$  7CD9C454BA907F7617E262A7FD73764C4A3157C13F82279EF9F062BE5D49A  
8E390B66A4DCEDFA867

$x_{qA} =$  BC43666C00E4B943FE1C785DD8AA842A42AB54B0B49819F960F77694193  
CD3AFA71B6B3C826C7734

$y_{qA} =$  69E998892C0764468023C8E3A7B8F219A1446042BE175D4476B2FDFD85B  
22EAD2F29101A1242A578

$dB =$  B832A73DA5F671E80D87F09372544801F6812224B19A4BC1B37AA7DB0842E  
6DD3CA11DE0F802BFED

$x_{qB} =$  B1246229429354D1D687BCA48BCCD6FC733B146DAC03642A0AD4B896F5D  
8BCBD2F4BCA16776E4526

$y_{qB} =$  A41683898F9A76EF36EA2DC7B74D419E55CF3664721890D6A2B2FB8CEB7  
C113167ED137A358EE37F

$x_Z =$  730314D906B2F21DC11BE05031B028D665696BEEC7139328CDF70C718BE5  
D208659BB96743A88067

$y_Z =$  C338B5B7A3FB62EDE9BAA9C06DF9BC36D4B5F0D35EFDF79249913E6DC4DB  
6DBC7BA9B74E59C840F1

Twisted Curve brainpoolP320t1

$dA =$  61ACFDF3C9C0E50B6ED58EC6B2750725D90C94D368EFA665B8800AFF31F21  
9AF39DA188ABAD9D6BC

$x_{qA} =$  4DEABAB307DDD924E302EFABC15E4BC588FE67ECF92F03B918E5F4AE43B  
62FFDE0F115015D9AD732

$y_{qA} =$  6E312549C939A9FCCD17D454B9212A39F670D4738B175EE5755A5BAAFF6  
D94992A5EA7541250E8FA

$dB =$  CDF6A4032DA09679DDE13D74F12C0F2E838D4CBE062E65CDDDB595799EDA4C  
22D3A69A4794DD4B032

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x\_qB = B3B33997A7047C32F2FCBC76960FFD71910316177E059AE77FFDE107722  
C6B05D019A71AE7FCEA05

y\_qB = 2D97625CB68013D900C169FD1336FC27A5531F0F54461AD91E38C49584D  
8ECCDE3AE66BA4D1E7D29

x\_Z = 13FB6B5E601AB1FAD84210E087EAE185F8CDC6D54EF63CF62950D0DA3437  
4BEF4DE4998E9A87263A

y\_Z = 6A969AE380DC0B22A0112F602DE3188EE2DE14EA453A2F5D2963CAF11CA9  
AEFEE241C7038411C27C

#### [A.6.](#) 384 Bit Curves

Curve brainpoolP384r1

dA = 1E20F5E048A5886F1F157C74E91BDE2B98C8B52D58E5003D57053FC4B0BD6  
5D6F15EB5D1EE1610DF870795143627D042

x\_qA = 68B665DD91C195800650CDD363C625F4E742E8134667B767B1B47679358  
8F885AB698C852D4A6E77A252D6380FCAF068

y\_qA = 55BC91A39C9EC01DEE36017B7D673A931236D2F1F5C83942D049E3FA206  
07493E0D038FF2FD30C2AB67D15C85F7FAA59

dB = 032640BC6003C59260F7250C3DB58CE647F98E1260ACCE4ACDA3DD869F74E  
01F8BA5E0324309DB6A9831497ABAC96670

x\_qB = 4D44326F269A597A5B58BBA565DA5556ED7FD9A8A9EB76C25F46DB69D19  
DC8CE6AD18E404B15738B2086DF37E71D1EB4

y\_qB = 62D692136DE56CBE93BF5FA3188EF58BC8A3A0EC6C1E151A21038A42E91  
85329B5B275903D192F8D4E1F32FE9CC78C48

x\_Z = 0BD9D3A7EA0B3D519D09D8E48D0785FB744A6B355E6304BC51C229FBBCE2  
39BBADF6403715C35D4FB2A5444F575D4F42

y\_Z = 0DF213417EBE4D8E40A5F76F66C56470C489A3478D146DECF6DF0D94BAE9  
E598157290F8756066975F1DB34B2324B7BD

## Twisted Curve brainpoolP384t1

dA = 820B55599BA830FB45BD280FE20D32F9A114F6E2EA4F9AC1D5EBE67F7C0B1  
A0506413A4B49E372A56620454FC0735481

x\_qA = 0C1C3E48C8072055EC617DECC3B5F6EE2566CBB16E9EAB2E8D839AB6E98  
1FCF13B2EDF86E27877B1AF99D8F2280BEA76

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y\_qA = 3365AC30C33AABB342C6FC30C2E3C0AAC15E4D521633185899687742188  
F96588C03DE656BD308C1906F67B033981603

dB = 3DF90919D4970788047B1FA0FBB716546ECF2A784CDD9CA53D5101B5BCA1A  
7CCAD7A7180B4C9F9D7D2A8F24E2B5936BD

x\_qB = 4C3949372FF295B6708C4180F6CF3616CA8BDF7CC792BAB582C27EC42EE  
FF0E563F2512B592438616E45D01309A06C0C

y\_qB = 1C43A48648C857189D9F2799B06F8253DF1BA8187622EDBF5C2C4A34164  
22877E7A2056FE6165271899DDD86DEC2CBC7

x\_Z = 8549A7BC6523128176322B295F5806971F9C2B6C10A6595D252CCA4B404E  
940BDB193AE0AB664959DBE638C8BB75A55E

y\_Z = 0C9D339F9ECA04924E2B73619DB30CADAF344AAB15938D4EE4E9DC7A81A4  
66A1CDC0D4C422DC75A5333DE8F226E9707C

### [A.7.](#)    512 Bit Curves

#### Curve brainpoolP512r1

dA = 16302FF0DBBB5A8D733DAB7141C1B45ACBC8715939677F6A56850A38BD87B  
D59B09E80279609FF333EB9D4C061231FB26F92EEB04982A5F1D1764CAD5766542  
2

x\_qA = 0A420517E406AAC0ACDCE90FCD71487718D3B953EFD7FBEC5F7F27E28C6  
149999397E91E029E06457DB2D3E640668B392C2A7E737A7F0BF04436D11640FD0  
9FD

y\_qA = 72E6882E8DB28AAD36237CD25D580DB23783961C8DC52DFA2EC138AD472  
A0FCEF3887CF62B623B2A87DE5C588301EA3E5FC269B373B60724F5E82A6AD147F  
DE7

dB = 230E18E1BCC88A362FA54E4EA3902009292F7F8033624FD471B5D8ACE49D1  
2CFABBC19963DAB8E2F1EBA00BFFB29E4D72D13F2224562F405CB80503666B2542  
9

x\_qB = 9D45F66DE5D67E2E6DB6E93A59CE0BB48106097FF78A081DE781CDB31FC  
E8CCBAAEA8DD4320C4119F1E9CD437A2EAB3731FA9668AB268D871DEDA55A54731  
99F

y\_qB = 2FDC313095BCDD5FB3A91636F07A959C8E86B5636A1E930E8396049CB48  
1961D365CC11453A06C719835475B12CB52FC3C383BCE35E27EF194512B7187628  
5FA

x\_Z = A7927098655F1F9976FA50A9D566865DC530331846381C87256BAF322624  
4B76D36403C024D7BBF0AA0803EAF0405D3D24F11A9B5C0BEF679FE1454B21C4CD

1F

y\_Z = 7DB71C3DEF63212841C463E881BDCF055523BD368240E6C3143BD8DEF8B3  
B3223B95E0F53082FF5E412F4222537A43DF1C6D25729DDB51620A832BE6A26680  
A2

Twisted Curve brainpoolP512t1

dA = 7938A373E32ECDCB3A88B725531EF0A41165904FDE02879EE738FE81B3B87  
A4F5730A8EB5FBA650609D7A5979099F058500EB160D3557D69B90FB2BAFE8AA3B  
4

x\_qA = 587335843CF88ACBC4110DD3711E21238280FD9D6BCDCB5F5AC8DB599D3  
77DE168AA32276FB068A3EF05EE61021668EC7C5BB1DDB96E392F6AC5C03F4A7C6  
05A

y\_qA = 501E2C43716E3F5D6D2F5960A33ECD2BA2D812AFB76B8C158E6E25FD37F  
82EE7299E2E64BCB39C0B739A5493C99615E62AE79C8719E40DDD9B7A44D990C73  
683

dB = 5538DF5451063E1CE7351C1A750C29D38FA2348F2FA097A1DB75D24AC8F83  
D8F13ED009F02621F6A0E3796101FB1EC9F1890B66635DDCEB5EF1ED083A28CF01  
2

x\_qB = A6400A41B64FCD6E451DD3B42B0247B24596118058B4DF8E34EC3EC33B1  
9CDCF5A9B2ECA4F1DB2D58C2AFD047550996CA361FCA8497233AF8C0F406FD9FC0

CD1

y\_qB = 7B7DB683F90DE91F3814139CC83E0693FED68A302458CA7690BA66067E3  
C963EB4D073F72723E01E05B6D0484D80FBE2EE830DB1F8F0B58570E5D8342267B  
2DE

x\_Z = 540789E4BA46DD1925ED37A9FCAFC927A3FE264F924FDA130790B1429AA2  
449C6FDFF21EC506672E2E9E1DB3D69B04461FFB1736D7E7F7764BE4BDD9F8D271  
B1

y\_Z = 37C113154C495B136D495B6864EC85C31AC46C19E3131E736D1C0B42BC00  
B05452AF0AB408B244ED0B4B3ECB65634C603829C72396D8D6072DE5663935DD89  
5F

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