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Pascal Urien
Telecom ParisTech
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TLS Tripartite Diffie-Hellman Key Exchange
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Abstract

Most of privacy exchanges over the Internet rely on the TLS protocol. According to this protocol two entities the client and the server computes a master secret from which are deduced cryptographic keys used for data privacy and security. Digital transactions may deal with critical information (payments ...) that need to be recorded for traceability issues or for legal requirements. However messages are secured by the TLS protocol, so it is not possible for a third party that logs packets to perform decryption operations upon legitimate requests.

The goal of this draft is to support a Trusted Third Party (TTP) that could recover the protected information when needed. The proposed protocol uses the Tripartite Diffie-Hellman (tdh) algorithm based on bilinear pairings over elliptic curves.

Requirements Language

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [RFC 2119](#) [[RFC2119](#)].

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1 Overview

Most of privacy exchanges over the Internet rely on the TLS protocol. According to this protocol two entities the client and the server computes a master secret from which are deduced cryptographic keys used for data privacy and security.

Digital transactions may deal with critical information (payments ...) that need to be recorded for traceability issues or for legal requirements.

However messages are secured by the TLS protocol, so it is not possible to a third party that logs packets to perform decryption operations upon legitimate requests.

The idea of this proposal is to support a Trusted Third Party (TTP) that could recover the protected information when needed.

The Tripartite Diffie-Hellman (tdh) idea was initially introduced in [\[TDH\]](#).

Toady cryptography provides efficient software tools [\[PBC\]](#) computing bilinear pairing over elliptic curve. The [\[TLS-ECC\]](#) standard already supports cryptographic operations based on elliptic curves, mainly for key exchange based on ECDH (Elliptic Curve Diffie Hellman) or the ECDSA (Elliptic Curve Digital Signature Algorithm) signature.

The Weil pairing for example works with classical elliptic curves; server and client are equipped with DH public and private keys.

The classical TLS pre-master-secret is computed according to the relation

pre-master-secret = abP (or g^{ab} with multiplicative notations)

Where P is a point of an elliptic curve point (a generator) defined over a F_q field, aP and bP are respectively the server and client DH public keys, and a, b their private keys.

If the client and the server agree to use a TTP, identified by an attribute `ttp-name` and owning a DH public key cP , the pre-master-secret is computing according to the following relation:

$$\begin{aligned} S_{\text{client}} &= e(aP, cP)^b \\ S_{\text{server}} &= e(bP, cP)^a \\ S_{\text{ttp}} &= e(aP, bP)^c, \end{aligned}$$

$S = S_{\text{server}} = S_{\text{client}} = S_{\text{ttp}} = \text{shared-secret}$

S is an element of $F(q^k)$, with k integer

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pre-master-secret = $h(S)$, h a hash function producing p bits

In other words each entity (client, server, TTP) computes a shared secret S by using its private DH key and the two other public DH keys.

The master-secret is thereafter produced:

```
master_secret = PRF(pre-master-secret,
                    "master secret",
                    ClientHello.random + ServerHello.random).
```

The master secret is computed by the client and the server without a dialog with the TTP. But the TTP will be able to recover the master secret from the TLS session logs.

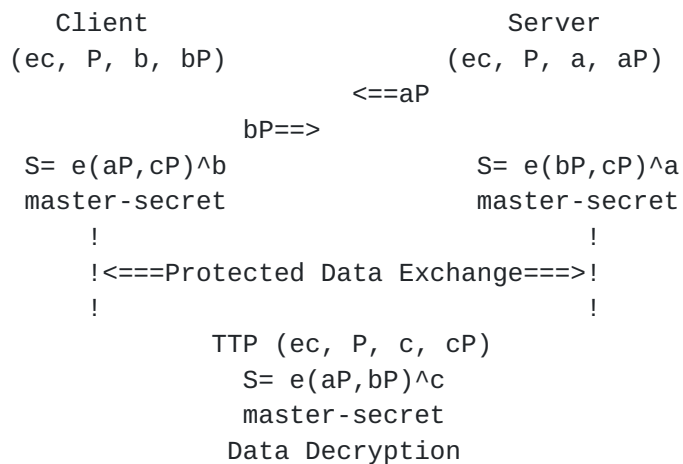


Figure 1. Illustration of TTP use in a TLS session

[2](#) About Bilinear Pairing

[2.1](#) Symmetric Bilinear Pairing

Z is the set of integer.

r is a prime integer

Let $(G1, +)$ be a cyclic group of order r , (with additive operation $+$)

Let $(G2, *)$ be a cyclic group of order r , (with multiplicative operation x).

Let e a non-degenerate bilinear map, $G1 \times G1 \rightarrow G2$

A non-degenerate bilinear pairing satisfies the following conditions:

- Bilinear:

for P, Q elements of $G1$, a, b elements of Z , $e(aP, bP) = e(P, Q)^{ab}$

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- Non-Degenerate:
 $e(P,P) \neq 1$ is a generator of G_2

The Weil pairing [ECC] has been defined for elliptic curve [ECC] over finite field of prime characteristic p (F_p)

- ECC is an elliptic curve over F_p
- G_1 is a subgroup in $ECC(F_p)$, whose order is r
- G_2 is a subgroup in $F(p^k)$, k an integer

2.2 Asymmetric Bilinear Pairing

In that case the bilinear map works with two different groups G_1 , whose order is r , and G_1' , where each element has order dividing r .

e is a non-degenerate bilinear map, $G_1 \times G_1' \rightarrow G_2$

For P elements of G_1 , Q element of G_1' , a, b elements of Z :
 $e(aP, bQ) = e(P, Q)^{ab}$

The Tate pairing [ECC] has been defined for elliptic curve [ECC] over finite field of prime characteristic p (F_p).

- ECC is an elliptic curve over F_p
- G_1 is a subgroup in $ECC(F_p)$, whose order is r
- G_1' is a subgroup in $ECC(F_{p^k})$, with k integer (k is the elliptic curve embedding degree)
- G_2 is a subgroup in $F(p^k)$

2.3 The Bilinear Diffie-Hellman (BDH) problem.

P is a generator of G_1

a, b, c are elements of Z_r^*

BDH: Knowing P, aP, bP, cP the computation of $e(P, P)^{abc}$ is 'impossible'

Furthermore the classical computational Diffie Hellman (CDH) assumption is assumed for the group G_1 .

CDH: Knowing P, aP, bP the computation of abP is 'impossible'

2.4 Practical properties

2.4.1 Symmetric Pairing

We suppose three entities A (server), B (client), C (ttp) equipped with three pairs of public and private keys, associated with a group

G1 and a generator P.

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a_P and a , are respectively the public and the private keys for A
 b_P and b , are respectively the public and the private keys for B
 c_P and c , are respectively the public and the private keys for C

A shared secret (S) may be computed by these three entities,
according to the following scenario:

- A computes $S = e^a(b_P, c_P) = e(P, P)^{abc}$
- B computes $S = e^b(a_P, c_P) = e(P, P)^{abc}$
- C computes $S = e^c(a_P, b_P) = e(P, P)^{abc}$

In other word each entity computes a shared secret key, deduced from
its private key and the two other public key.

If A is a client, B a server and C a trusted party, all security
properties such as encrypted packets exchanged between client and
server may be recovered by the trusted party.

2.4.2 Asymmetric pairing

We suppose three entities A (server), B (client), C (ttp) equipped
with pairs of public and private keys, associated with the group G_1
(generator P) and the group G_1' (generator P').

a_P , $a_{P'}$ and a , are respectively the public and the private keys for A
 b_P and b , are respectively the public and the private key for B
 c_P , $c_{P'}$ and c , are respectively the public and the private keys for C

A shared secret (S) may be computed by these three entities,
according to the following scenario

- A computes $S = e^b(b_P, c_{P'}) = e(P, P')^{abc}$
- B computes $S = e^b(a_P, c_{P'}) = e(P, P')^{abc}$
- C computes $S = e^c(a_P, b_{P'}) = e(P, P')^{abc}$

3. Bilinear pairing operations overview



Figure 2. Overview of the TLS bilinear pairing operations.

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The TLS dialog is illustrated by figure 2. A new extension is used both by client and server in order to negotiate a pairing scheme. The TTP is selected thanks attributes exchanged in the ServerKeyExchange and ClientKeyExchange messages. Elliptic curve and DH parameter are specified according to [\[TLS-ECC\]](#).

[4. Bilinear Pairing Operations details](#)

[4.1 TLS Extension](#)

A new TLS extension is defined in this specification: the pairing-scheme extension.

The general structure of TLS extensions is described in [\[TLS 1.1\]](#), and this specification adds one new item to ExtensionType.

```
enum { pairing-scheme(xx)} ExtensionType;
```

The client negotiates the pairing-scheme via the corresponding extension inserted in the client hello message

The server selects one of the proposed items and inserts it in the server hello message.

Two other extensions are imported from [\[TLS-ECC\]](#):

- elliptic-curves(10),
- ec_point-formats(11);

4.1.1 Supported Pairing Scheme

Supported Pairing Scheme

```
enum {  
    Weil-Pairing (1)  
} NamedScheme;
```

[4.2 Key Exchange](#)

A new KeyExchange Algorithm is defined: ec-bilinear-pairing

4.2.1 Trusted-Third-Party list

Each trusted third party (TTP) is identified by a name. A DH public key is implicitly deduced from its identifier.

Structure of this message:

```
opaque TTP-Name<1..2^24-1>;
```

```
struct {  
    TTP-Name ttp-name-list<0..2^24-1>;  
} TTP-List;
```

4.2.1 Server Key Exchange

The ServerKeyExchange message is extended as follows.

```
enum { ec-bilinear-pairing } KeyExchangeAlgorithm;  
  
select (KeyExchangeAlgorithm) {  
    case ec_bilinear-pairing:  
        ServerECDHParams    params;  
        Signature            signed-params;  
        TTP-List             ttp-list  
} ServerKeyExchange;
```

The attributes ServerECDHParams and Signature are imported from [TLS-ECC]

4.2.2 Client Key Exchange

The ClientKeyExchange message is extended as follows.

```
struct {  
    select (KeyExchangeAlgorithm) {  
        case ec_bilinear-pairing:  
            ClientECDiffieHellmanPublic;  
            TTP-Name: ttp-name  
        } exchange-keys;  
} ClientKeyExchange;
```

The attribute ClientECDiffieHellmanPublic is imported from [[TLS-ECC](#)].

[4.3](#) PreMasterSecret computing

aP and bP are respectively the server and the client DH public values (with additive notations)

cP is the trusted third party (ttp) public value, (with additive notations).

h is a digest function producing p bytes.

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On the server side:

$$\text{PreMasterSecret} = h(e(b_P, c_P)^a)$$

On client side:

$$\text{PreMasterSecret} = h(e(a_P, c_P)^b)$$

On the ttp side

$$\text{PreMasterSecret} = h(e(a_P, b_P)^c)$$

4.3.1 Hash function for the Weil pairing

For the Weil pairing, G_2 is a subgroup of F_q^2 , if the output of e is expressed as the tuple (a_0, a_1) with x and y elements of F_q

$h = \text{sha1}(a_0 || a_1)$, a_0 and a_1 are values of exactly q bits.

4.4 CipherSuites

To be done.

5. Example of pairings

This example has been computed with the Pairing-Based Cryptography Library [[PBC](#)] [[BL](#)].

5.1 Symmetric pairing

The elliptic curve (ECC) is chosen as:

$y^2 = x^3 + x$, with x, y elements of a Field F_q

q is a prime number, with $q \equiv 3 \pmod{4}$

G_1 is a subgroup of $ECC(F_q)$

G_2 is a subgroup of F_q^2

There are $q+1$ points on the ECC curve, i.e. $\#ECC(F_q) = q+1$

r = order of G_1 = prime factor of $q+1$.

h = cofactor = $\#ECC(F_q) / r$

$q=8780710799663312522437781984754049815806883199414208211028653399266$
 $475630880222957078625179422662221423155858769582317459277713367317481$
 $324925129998224791.$

$h=1201601226489114607938882136674053420480295440125131182291961513104$
 $7207289359704531102844802183906537786776$

$r=730750818665451621361119245571504901405976559617$

Generator P=

764213932795790385166146156484628185710738246136731223594607305863197
148904107335230752866953232919510098156557991388877251113225844051396
9390781514106884,
841053126166803064145349163706237513167951671763744795990943027230354
098248702951019958048685849729494818612964151563063433969126677448023
4634049031935396

a = 321231739573260508064943282038854866624801566274

aP =

301901600464207748384853072909292823401500311348346356764859754747703
064669197258898445749044213480292759568257999990157011471277891932048
3502179821202747,
622130912004388536645426112375868421081814378272661695953772580311048
821974186212677634483766383564352093956376894422864585155448402243584
2060112859040085

b = 591069617759232948334516538341133684003963967541

bP =

489872625336582550697622917901310968712983470168986006826993590244144
534124000070208650497397931419729729097601618783404569928023315742260
1733989063260044,
715768020641988338757762409522925702707172363082968385844449919698450
610626853008028585471746136204506517503675925750751323255279155813951
061482849469617

c = 332790059747456431829511198714114673843901104395

cP =

361673235446634950587227148388584900737947568189969047494313829915613
165227389313929815513580932571550613336307696480151992816947356553291
3077259306029100,
591927063716469042674124332635453987072498361375371305395310139261168
079986151403557597760872949800149313292665777504365718007945299529892
7247712148590792

$S = f(aP, bP)^c = f(bP, cP)^a = f(cP, aP)^b =$

411874021818983935494518378468671897765968395058497750231537284872046
634607045530820852050427874577949368791925702115715036551400857093954
2202145179250626,
792272713616191570585463230096947246676587164343554480144379956667402
825333387256294430771484207666103108581680992251414596583914923441539
9681428439428268

6. Security Considerations

To be done.

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7. IANA Considerations

To be done

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Author's Addresses

Pascal Urien
Telecom ParisTech
37/39 rue Dareau, 75014 Paris, France

Email: Pascal.Urien@telecom-paristech.fr

