

Network Working Group
Internet-Draft
Intended status: Standards Track
Expires: April 16, 2019

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October 13, 2018

Algorithm Identifiers for HSS and XMSS for Use in the Internet X.509
Public Key Infrastructure
draft-vangeest-x509-hash-sigs-01

Abstract

This document specifies algorithm identifiers and ASN.1 encoding formats for the Hierarchical Signature System (HSS), eXtended Merkle Signature Scheme (XMSS), and XMSS^{MT}, a multi-tree variant of XMSS. This specification applies to the Internet X.509 Public Key Infrastructure (PKI) when digital signatures are used to sign certificates and certificate revocation lists (CRLs).

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[1.](#) Introduction

The Hierarchical Signature System (HSS) is described in [\[I-D.mcgrewhash-signs\]](#).

The eXtended Merkle Signature Scheme (XMSS), and its multi-tree variant XMSS^{AMT}, are described in [\[RFC8391\]](#).

These signature algorithms are based on well-studied Hash Based Signature (HBS) schemes, which can withstand known attacks using quantum computers. They combine Merkle Trees with One Time Signature (OTS) schemes in order to create signature systems which can sign a large but limited number of messages per private key. The private keys are stateful; a key's state must be updated and persisted after signing to prevent reuse of OTS keys. If an OTS key is reused, cryptographic security is not guaranteed for that key.

Due to the statefulness of the private key and the limited number of signatures that can be created, these signature algorithms might not be appropriate for use in interactive protocols. While the right selection of algorithm parameters would allow a private key to sign a

virtually unbounded number of messages (e.g. 2^{60}), this is at the cost of a larger signature size and longer signing time. Since these algorithms are already known to be secure against quantum attacks, and because roots of trust are generally long-lived and can take longer to be deployed than end-entity certificates, these signature algorithms are more appropriate to be used in root and subordinate CA certificates. They are also appropriate in non-interactive contexts such as code signing.

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in [[RFC2119](#)].

[2.](#) Subject Public Key Algorithms

Certificates conforming to [[RFC5280](#)] can convey a public key for any public key algorithm. The certificate indicates the algorithm through an algorithm identifier. An algorithm identifier consists of an OID and optional parameters.

In this document, we define two new OIDs for identifying the different hash-based signature algorithms. A third OID is defined in [[I-D.ietf-lamps-cms-hash-sig](#)] and repeated here for convenience. For all of the OIDs, the parameters MUST be absent.

[2.1.](#) HSS Public Keys

The object identifier and public key algorithm identifier for HSS is defined in [[I-D.ietf-lamps-cms-hash-sig](#)]. The definitions are repeated here for reference.

The object identifier for an HSS public key is id-alg-hss-lms-hashsig:

```
id-alg-hss-lms-hashsig OBJECT IDENTIFIER ::= { iso(1)
  member-body(2) us(840) rsadsi(113549) pkcs(1) pkcs9(9)
```

```
smime(16) alg(3) 17 }
```

Note that the id-alg-hss-lms-hashsig algorithm identifier is also referred to as id-alg-mts-hashsig. This synonym is based on the terminology used in an early draft of the document that became [\[I-D.mcgrew-hash-sigs\]](#).

The HSS public key's properties are defined as follows:

```
pk-HSS-LMS-HashSig PUBLIC-KEY ::= {  
  IDENTIFIER id-alg-hss-lms-hashsig  
  KEY HSS-LMS-HashSig-PublicKey  
  PARAMS ARE absent  
  CERT-KEY-USAGE  
    { digitalSignature, nonRepudiation, keyCertSign, cRLSign } }
```

```
HSS-LMS-HashSig-PublicKey ::= OCTET STRING
```

[I-D.ietf-lamps-cms-hash-sig] contains more information on the contents and format of an HSS public key.

[2.2.](#) XMSS Public Keys

The object identifier for an XMSS public key is id-xmss:

```
id-xmss OBJECT IDENTIFIER ::= { itu-t(0)  
  identified-organization(4) etsi(0) reserved(127)  
  etsi-identified-organization(0) isara(15) algorithms(1)  
  asymmetric(1) xmss(13) 0 }
```

The XMSS public key's properties are defined as follows:

```
pk-xmss PUBLIC-KEY ::= {  
  IDENTIFIER id-xmss  
  KEY XMSS-PublicKey  
  PARAMS ARE absent  
  CERT-KEY-USAGE  
    { digitalSignature, nonRepudiation, keyCertSign, cRLSign } }
```

XMSS-PublicKey ::= OCTET STRING

The format of an XMSS public key is formally defined using XDR [RFC4506] and is defined in [Appendix B.3 of \[RFC8391\]](#). In particular, the first 4 bytes represents the big-ending encoding of the XMSS algorithm type.

[2.3.](#) XMSS^{MT} Public Keys

The object identifier for an XMSS^{MT} public key is id-xmssmt:

```
id-xmssmt OBJECT IDENTIFIER ::= { itu-t(0)
    identified-organization(4) etsi(0) reserved(127)
    etsi-identified-organization(0) isara(15) algorithms(1)
    asymmetric(1) xmssmt(14) 0 }
```

The XMSS^{MT} public key's properties are defined as follows:

```
pk-xmssmt PUBLIC-KEY ::= {
    IDENTIFIER id-xmssmt
    KEY XMSSMT-PublicKey
    PARAMS ARE absent
    CERT-KEY-USAGE
        { digitalSignature, nonRepudiation, keyCertSign, cRLSign } }
```

XMSSMT-PublicKey ::= OCTET STRING

The format of an XMSS^{MT} public key is formally defined using XDR [RFC4506] and is defined in [Appendix C.3 of \[RFC8391\]](#). In particular, the first 4 bytes represents the big-ending encoding of the XMSS^{MT} algorithm type.

[3.](#) Key Usage Bits

The intended application for the key is indicated in the keyUsage certificate extension.

If the keyUsage extension is present in an end-entity certificate that indicates id-xmss or id-xmssmt in SubjectPublicKeyInfo, then the keyUsage extension MUST contain one or both of the following values:

nonRepudiation; and
digitalSignature.

If the keyUsage extension is present in a certification authority certificate that indicates id-xmss or id-xmssmt, then the keyUsage extension MUST contain one or more of the following values:

nonRepudiation;
digitalSignature;
keyCertSign; and
cRLSign.

[I-D.ietf-lamps-cms-hash-sig] defines the key usage for id-alg-hss-lms-hashsig, which is the same as for the keys above.

[4.](#) Signature Algorithms

Certificates and CRLs conforming to [[RFC5280](#)] may be signed with any public key signature algorithm. The certificate or CRL indicates the algorithm through an algorithm identifier which appears in the signatureAlgorithm field within the Certificate or CertificateList. This algorithm identifier is an OID and has optionally associated parameters. This section identifies algorithm identifiers that MUST be used in the signatureAlgorithm field in a Certificate or CertificateList.

Signature algorithms are always used in conjunction with a one-way hash function.

This section identifies OIDs for HSS, XMSS, and XMSS^{MT}. When these algorithm identifiers appear in the algorithm field as an AlgorithmIdentifier, the encoding MUST omit the parameters field. That is, the AlgorithmIdentifier SHALL be a SEQUENCE of one component, one of the OIDs defined below.

The data to be signed (e.g., the one-way hash function output value) is directly signed by the hash-based signature algorithms without any additional formatting necessary. The signature value is a large OCTET STRING. This signature value is then ASN.1 encoded as a BIT STRING and included in the Certificate or CertificateList in the signature field.

[4.1.](#) HSS Signature Algorithm

The ASN.1 OIDs used to specify that an HSS signature was generated on a SHA-256 or SHA-512 hash of an object are, respectively:

```
hss-with-SHA256 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) hss(12) 2 }
```

```
hss-with-SHA512 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) hss(12) 1 }
```

[I-D.ietf-lamps-cms-hash-sig] contains more information on the contents and format of an HSS signature.

[4.2.](#) XMSS Signature Algorithm

The ASN.1 OIDs used to specify that an XMSS signature was generated on a SHA-256 or SHA-512 hash of an object are, respectively:

```
xmss-with-SHA256 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) xmss(13) 2 }
```

```
xmss-with-SHA512 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) xmss(13) 1 }
```

The format of an XMSS signature is is formally defined using XDR [RFC4506] and is defined in [Appendix B.2 of \[RFC8391\]](#).

[4.3.](#) XMSS^{MT} Signature Algorithm

The ASN.1 OIDs used to specify that an XMSS^{MT} signature was generated on a SHA-256 or SHA-512 hash of an object are, respectively:

```

xmssmt-with-SHA256  OBJECT IDENTIFIER ::= { itu-t(0)
    identified-organization(4) etsi(0) reserved(127)
    etsi-identified-organization(0) isara(15) algorithms(1)
    asymmetric(1) xmssmt(14) 2 }

```

```

xmssmt-with-SHA512  OBJECT IDENTIFIER ::= { itu-t(0)
    identified-organization(4) etsi(0) reserved(127)
    etsi-identified-organization(0) isara(15) algorithms(1)
    asymmetric(1) xmssmt(14) 1 }

```

The format of an XMSS^{MT} signature is formally defined using XDR [RFC4506] and is defined in [Appendix C.2 of \[RFC8391\]](#).

5. ASN.1 Module

For reference purposes, the ASN.1 syntax is presented as an ASN.1 module here.

```
-- ASN.1 Module
```

```
Hashsigns-pkix-0 -- TBD - IANA assigned module OID
```

```

DEFINITIONS EXPLICIT TAGS ::=
BEGIN

```

```

IMPORTS
    PUBLIC-KEY
    FROM AlgorithmInformation-2009
        {iso(1) identified-organization(3) dod(6) internet(1) security(5)
        mechanisms(5) pkix(7) id-mod(0)
        id-mod-algorithmInformation-02(58)}
;

```



```

-- HSS Signatures
--

-- HSS Object Identifiers

hss-with-SHA256 OBJECT IDENTIFIER ::= { itu-t(0)
    identified-organization(4) etsi(0) reserved(127)
    etsi-identified-organization(0) isara(15) algorithms(1)
    asymmetric(1) hss(12) 2 }

hss-with-SHA512 OBJECT IDENTIFIER ::= { itu-t(0)
    identified-organization(4) etsi(0) reserved(127)
    etsi-identified-organization(0) isara(15) algorithms(1)
    asymmetric(1) hss(12) 1 }

-- HSS Signature Algorithms

sa-hssWithSHA256 SIGNATURE-ALGORITHM ::= {
    IDENTIFIER hss-with-SHA256
    PARAMS ARE absent
    HASHES { mda-sha256 }
    PUBLIC-KEYS { pk-HSS-LMS-HashSig }
    SMIME-CAPS { IDENTIFIED BY hss-with-SHA256 } }

sa-hssWithSHA512 SIGNATURE-ALGORITHM ::= {
    IDENTIFIER hss-with-SHA512
    PARAMS ARE absent
    HASHES { mda-sha512 }
    PUBLIC-KEYS { pk-HSS-LMS-HashSig }
    SMIME-CAPS { IDENTIFIED BY hss-with-SHA512 } }

-- Note that pk-HSS-LMS-HashSig is defined in
-- AlgorithmInformation-2009

--

-- XMSS Keys and Signatures
--

-- XMSS Object Identifiers

id-xmss OBJECT IDENTIFIER ::= { itu-t(0)
    identified-organization(4) etsi(0) reserved(127)
    etsi-identified-organization(0) isara(15) algorithms(1)
    asymmetric(1) xmss(13) 0 }

```

```
xmss-with-SHA256 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) xmss(13) 2 }

xmss-with-SHA512 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) xmss(13) 1 }

-- XMSS Signature Algorithms and Public Key

sa-xmssWithSHA256 SIGNATURE-ALGORITHM ::= {
  IDENTIFIER xmss-with-SHA256
  PARAMS ARE absent
  HASHES { mda-sha256 }
  PUBLIC-KEYS { pk-xmss }
  SMIME-CAPS { IDENTIFIED BY xmss-with-SHA256 } }

sa-xmssWithSHA512 SIGNATURE-ALGORITHM ::= {
  IDENTIFIER xmss-with-SHA512
  PARAMS ARE absent
  HASHES { mda-sha512 }
  PUBLIC-KEYS { pk-xmss }
  SMIME-CAPS { IDENTIFIED BY xmss-with-SHA512 } }

pk-xmss PUBLIC-KEY ::= {
  IDENTIFIER id-xmss
  KEY XMSS-PublicKey
  PARAMS ARE absent
  CERT-KEY-USAGE
    { digitalSignature, nonRepudiation, keyCertSign, cRLSign } }

XMSS-PublicKey ::= OCTET STRING

--
-- XMSS^MT Keys and Signatures
--

-- XMSS^MT Object Identifiers

id-xmssmt OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) xmssmt(14) 0 }
```

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```
xmssmt-with-SHA256 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) xmssmt(14) 2 }

xmssmt-with-SHA512 OBJECT IDENTIFIER ::= { itu-t(0)
  identified-organization(4) etsi(0) reserved(127)
  etsi-identified-organization(0) isara(15) algorithms(1)
  asymmetric(1) xmssmt(14) 1 }

-- XMSS^MT Signature Algorithms and Public Key

sa-xmssmtWithSHA256 SIGNATURE-ALGORITHM ::= {
  IDENTIFIER xmssmt-with-SHA256
  PARAMS ARE absent
  HASHES { mda-sha256 }
  PUBLIC-KEYS { pk-xmssmt }
  SMIME-CAPS { IDENTIFIED BY xmssmt-with-SHA256 } }

sa-xmssmtWithSHA512 SIGNATURE-ALGORITHM ::= {
  IDENTIFIER xmssmt-with-SHA512
  PARAMS ARE absent
  HASHES { mda-sha512 }
  PUBLIC-KEYS { pk-xmssmt }
  SMIME-CAPS { IDENTIFIED BY xmssmt-with-SHA512 } }

pk-xmssmt PUBLIC-KEY ::= {
  IDENTIFIER id-xmssmt
  KEY XMSSMT-PublicKey
  PARAMS ARE absent
  CERT-KEY-USAGE
    { digitalSignature, nonRepudiation, keyCertSign, cRLSign } }

XMSSMT-PublicKey ::= OCTET STRING

END
```

[6.](#) Security Considerations

[6.1.](#) Algorithm Security Considerations

The cryptographic security of the signatures generated by the algorithms mentioned in this document depends only on the hash algorithms used within the signature algorithms and the pre-hash algorithm used to create an X.509 certificate's message digest. Grover's algorithm [[Grover96](#)] is a quantum search algorithm which gives a quadratic improvement in search time to brute-force pre-image attacks. The results of [[BBBV97](#)] show that this improvement is

optimal, however [[Fluhrer17](#)] notes that Grover's algorithm doesn't parallelize well. Thus, given a bounded amount of time to perform the attack and using a conservative estimate of the performance of a real quantum computer, the pre-image quantum security of SHA-256 is closer to 190 bits. All parameter sets for the signature algorithms in this document currently use SHA-256 internally and thus have at least 128 bits of quantum pre-image resistance, or 190 bits using the security assumptions in [[Fluhrer17](#)].

[Zhandry15] shows that hash collisions can be found using an algorithm with a lower bound on the number of oracle queries on the order of $2^{(n/3)}$ on the number of bits, however [[DJB09](#)] demonstrates that the quantum memory requirements would be much greater. Therefore a pre-hash using SHA-256 would have at least 128 bits of quantum collision-resistance as well as the pre-image resistance mentioned in the previous paragraph.

Given the quantum collision and pre-image resistance of SHA-256 estimated above, the algorithm identifiers hss-with-SHA256, xmss-with-SHA256 and xmssmt-with-SHA256 defined in this document provide 128 bits or more of quantum security. This is believed to be secure enough to protect X.509 certificates for well beyond any reasonable certificate lifetime, although the SHA-512 variants could be used if there are any doubts.

The algorithm identifiers hss-with-SHA512, xmss-with-SHA512 and xmssmt-with-SHA512 are defined in order to provide 256 bits of classical security (256 bits of brute-force pre-image resistance with the signature algorithms' SHA-256 and 256 bits of birthday attack collision resistance with the SHA-512 pre-hash).

[6.2.](#) Implementation Security Considerations

Implementations must protect the private keys. Compromise of the private keys may result in the ability to forge signatures. Along with the private key, the implementation must keep track of which leaf nodes in the tree have been used. Loss of integrity of this tracking data can cause an one-time key to be used more than once. As a result, when a private key and the tracking data are stored on non-volatile media or stored in a virtual machine environment, care must be taken to preserve confidentiality and integrity.

The generation of private keys relies on random numbers. The use of inadequate pseudo-random number generators (PRNGs) to generate these values can result in little or no security. An attacker may find it much easier to reproduce the PRNG environment that produced the keys, searching the resulting small set of possibilities, rather than brute force searching the whole key space. The generation of quality

random numbers is difficult. [[RFC4086](#)] offers important guidance in this area.

The generation of hash-based signatures also depends on random numbers. While the consequences of an inadequate pseudo-random number generator (PRNGs) to generate these values is much less severe than the generation of private keys, the guidance in [[RFC4086](#)] remains important.

[7.](#) Acknowledgements

Thanks for Russ Housley for the helpful suggestions.

This document uses a lot of text from similar documents ([[RFC3279](#)] and [[RFC8410](#)]) as well as [[I-D.ietf-lamps-cms-hash-sig](#)]. Thanks go to the authors of those documents. "Copying always makes things easier and less error prone" - [[RFC8411](#)].

[8.](#) IANA Considerations

IANA is requested to assign a module OID from the "SMI for PKIX Module Identifier" registry for the ASN.1 module in [Section 5](#).

[9.](#) References

9.1. Normative References

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[RFC8410]

Josefsson, S. and J. Schaad, "Algorithm Identifiers for Ed25519, Ed448, X25519, and X448 for Use in the Internet X.509 Public Key Infrastructure", [RFC 8410](#), DOI 10.17487/RFC8410, August 2018, <<https://www.rfc-editor.org/info/rfc8410>>.

[RFC8411]

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