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J-PAKE: Password-Authenticated Key Exchange by Juggling

Abstract

This document specifies a Password-Authenticated Key Exchange by Juggling (J-PAKE) protocol. This protocol allows the establishment of a secure end-to-end communication channel between two remote parties over an insecure network solely based on a shared password, without requiring a Public Key Infrastructure (PKI) or any trusted third party.

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Table of Contents

[1](#) [1.1](#) [1.2](#) [2](#) [2.1](#) [2.2](#) [2.3](#) [3](#) [3.1](#) [3.2](#) [3.3](#) [4](#) [5](#) [6](#) [7](#) [7](#) [7](#) [8](#) [8](#) [9](#) [11](#) [12](#) [12](#) [12](#) [14](#) [15](#) [15](#)

- 1. Introduction
- 1.1. Requirements Language
- 1.2. Notation
- 2. J-PAKE over Finite Field
- 2.1. Protocol Setup
- 2.2. Two-Round Key Exchange
- 2.3. Computational Cost
- 3. J-PAKE over Elliptic Curve
- 3.1. Protocol Setup
- 3.2. Two-Round Key Exchange
- 3.3. Computational Cost
- 4. Three-Pass Variant
- 5. Key Confirmation
- 6. Security Considerations
- 7. IANA Considerations
- 8. References
- 8.1. Normative References
- 8.2. Informative References
- Acknowledgements
- Author's Address

1. Introduction

Password-Authenticated Key Exchange (PAKE) is a technique that aims to establish secure communication between two remote parties solely based on their shared password, without relying on a Public Key Infrastructure or any trusted third party [BM92]. The first PAKE protocol, called Encrypted Key Exchange (EKE), was proposed by Steven Bellovin and Michael Merrit in 1992 [BM92]. Other well-known PAKE

protocols include Simple Password Exponential Key Exchange (SPEKE) by David Jablon in 1996 [[Jab96](#)] and Secure Remote Password (SRP) by Tom Wu in 1998 [[Wu98](#)]. SRP has been revised several times to address reported security and efficiency issues. In particular, the version 6 of SRP, commonly known as SRP-6, is specified in [[RFC5054](#)].

This document specifies a PAKE protocol called Password-Authenticated

Key Exchange by Juggling (J-PAKE), which was designed by Feng Hao and

Peter Ryan in 2008 [[HR08](#)]. There are a few factors that may be considered in favor of J-PAKE. First, J-PAKE has security proofs, while equivalent proofs are lacking in EKE, SPEKE and SRP-6.

Second,

J-PAKE follows a completely different design approach from all other PAKE protocols, and is built upon a well-established Zero Knowledge Proof (ZKP) primitive: Schnorr NIZK proof [[RFC8235](#)]. Third, J-PAKE adopts novel engineering techniques to optimize the use of ZKP so that overall the protocol is sufficiently efficient for practical use. Fourth, J-PAKE is designed to work generically in both the

finite field and elliptic curve settings (i.e., DSA and ECDSA-like groups, respectively). Unlike SPEKE, it does not require any extra primitive to hash passwords onto a designated elliptic curve.

Unlike

SPAKE2 [AP05] and SESPAKE [SOAA15], it does not require a trusted setup (i.e., the so-called common reference model) to define a pair of generators whose discrete logarithm must be unknown. Finally, J-PAKE has been used in real-world applications at a relatively

large

scale, e.g., Firefox sync [MOZILLA], Pale moon sync [PALEMOON], and Google Nest products [ABM15]. It has been included into widely distributed open source libraries such as OpenSSL [BOINC], Network Security Services (NSS) [MOZILLA_NSS], and the Bouncy Castle [BOUNCY]. Since 2015, J-PAKE has been included in Thread [THREAD]

as

a standard key agreement mechanism for IoT (Internet of Things) applications, and also included in ISO/IEC 11770-4:2017 [ISO.11770-4].

1.1. Requirements Language

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in BCP 14 [RFC2119] [RFC8174] when, and only when, they appear in all capitals, as shown here.

1.2. Notation

The following notation is used in this document:

- o Alice: the assumed identity of the prover in the protocol
- o Bob: the assumed identity of the verifier in the protocol
- o s : a low-entropy secret shared between Alice and Bob
- o $a \mid b$: a divides b
- o $a \parallel b$: concatenation of a and b
- o $[a, b]$: the interval of integers between and including a and b
- o H : a secure cryptographic hash function
- o p : a large prime
- o q : a large prime divisor of $p-1$, i.e., $q \mid p-1$
- o Z_p^* : a multiplicative group of integers modulo p

- o G_q : a subgroup of Z_p^* with prime order q
- o g : a generator of G_q
- o g^d : g raised to the power of d
- o $a \bmod b$: a modulo b
- o F_p : a finite field of p elements, where p is a prime
- o $E(F_p)$: an elliptic curve defined over F_p
- o G : a generator of the subgroup over $E(F_p)$ with prime order n
- o n : the order of G
- o h : the cofactor of the subgroup generated by G , which is equal to the order of the elliptic curve divided by n
- o $P \times [b]$: multiplication of a point P with a scalar b over $E(F_p)$
- o $KDF(a)$: Key Derivation Function with input a
- o $MAC(\text{MacKey}, \text{MacData})$: MAC function with MacKey as the key and MacData as the input data

2. J-PAKE over Finite Field

2.1. Protocol Setup

When implemented over a finite field, J-PAKE may use the same group parameters as DSA [[FIPS186-4](#)]. Let p and q be two large primes such that $q \mid p-1$. Let G_q denote a subgroup of Z_p^* with prime order q . Let g be a generator for G_q . Any non-identity element in G_q can be

a generator. The two communicating parties, Alice and Bob, both agree on (p, q, g) , which can be hard-wired in the software code. They

can also use the method in NIST FIPS 186-4, [Appendix A \[FIPS186-4\]](#) to generate (p, q, g) . Here, DSA group parameters are used only as an example. Other multiplicative groups suitable for cryptography can also be used for the implementation, e.g., groups defined in [[RFC4419](#)]. A group setting that provides 128-bit security or above is recommended. The security proof of J-PAKE depends on the Decisional Diffie-Hellman (DDH) problem being intractable in the considered group.

Let s be a secret value derived from a low-entropy password shared between Alice and Bob. The value of s is REQUIRED to fall within the range of $[1, q-1]$. (Note that s must not be \emptyset for any non-empty

secret.) This range is defined as a necessary condition in [HR08] for proving the "on-line dictionary attack resistance", since s , $s+q$, $s+2q$, ..., are all considered equivalent values as far as the protocol specification is concerned. In a practical implementation, one may obtain s by taking a cryptographic hash of the password and wrapping the result with respect to modulo q . Alternatively, one may simply treat the password as an octet string and convert the string to an integer modulo q by following the method defined in Section 2.3.8 of [SEC1]. In either case, one MUST ensure s is not equal to 0 modulo q .

2.2. Two-Round Key Exchange

Round 1: Alice selects an ephemeral private key x_1 uniformly at random from $[0, q-1]$ and another ephemeral private key x_2 uniformly at random from $[1, q-1]$. Similarly, Bob selects an ephemeral private key x_3 uniformly at random from $[0, q-1]$ and another ephemeral private key x_4 uniformly at random from $[1, q-1]$.

- o Alice -> Bob: $g_1 = g^{x_1} \bmod p$, $g_2 = g^{x_2} \bmod p$ and ZKPs for x_1 and x_2
- o Bob -> Alice: $g_3 = g^{x_3} \bmod p$, $g_4 = g^{x_4} \bmod p$ and ZKPs for x_3 and x_4

In this round, the sender must send zero knowledge proofs to demonstrate the knowledge of the ephemeral private keys. A suitable technique is to use the Schnorr NIZK proof [RFC8235]. As an example,

suppose one wishes to prove the knowledge of the exponent for $D = g^d \bmod p$. The generated Schnorr NIZK proof will contain: $\{\text{UserID}, V = g^v \bmod p, r = v - d * c \bmod q\}$, where UserID is the unique identifier for the prover, v is a number chosen uniformly at random from $[0, q-1]$ and $c = H(g || V || D || \text{UserID})$. The "uniqueness" of UserID is defined from the user's perspective -- for example, if Alice communicates with several parties, she shall associate a unique identity with each party. Upon receiving a Schnorr NIZK proof, Alice shall check the prover's UserID is a valid identity and is different from her own identity. During the key exchange process using J-PAKE, each party shall ensure that the other party has been consistently using the same identity throughout the protocol execution. Details about the Schnorr NIZK proof, including the generation and the verification procedures, can be found in [RFC8235].

When this round finishes, Alice verifies the received ZKPs as specified in [\[RFC8235\]](#) and also checks that $g_4 \neq 1 \pmod p$. Similarly, Bob verifies the received ZKPs and also checks that $g_2 \neq 1 \pmod p$. If any of these checks fails, this session should be aborted.

Round 2:

- o Alice \rightarrow Bob: $A = (g_1 * g_3 * g_4)^{(x_2 * s)} \bmod p$ and a ZKP for $x_2 * s$
- o Bob \rightarrow Alice: $B = (g_1 * g_2 * g_3)^{(x_4 * s)} \bmod p$ and a ZKP for $x_4 * s$

In this round, the Schnorr NIZK proof is computed in the same way as in the previous round except that the generator is different. For Alice, the generator used is $(g_1 * g_3 * g_4)$ instead of g ; for Bob, the generator is $(g_1 * g_2 * g_3)$ instead of g . Since any non-identity element

in G_q can be used as a generator, Alice and Bob just need to ensure $g_1 * g_3 * g_4 \neq 1 \bmod p$ and $g_1 * g_2 * g_3 \neq 1 \bmod p$. With overwhelming probability, these inequalities are statistically guaranteed even when the user is communicating with an adversary (i.e., in an active attack). Nonetheless, for absolute guarantee, the receiving party shall explicitly check if these inequalities hold, and abort the session in case such a check fails.

When the second round finishes, Alice and Bob verify the received ZKPs. If the verification fails, the session is aborted.

Otherwise,

the two parties compute the common key material as follows:

- o Alice computes $K_a = (B / g_4^{(x_2 * s)})^{x_2} \bmod p$
- o Bob computes $K_b = (A / g_2^{(x_4 * s)})^{x_4} \bmod p$

Here, $K_a = K_b = g^{((x_1 + x_3) * x_2 * x_4 * s)} \bmod p$. Let K denote the same key

material held by both parties. Using K as input, Alice and Bob then apply a Key Derivation Function (KDF) to derive a common session key k . If the subsequent secure communication uses a symmetric cipher

in

an authenticated mode (say AES-GCM), then one key is sufficient, i.e., $k = \text{KDF}(K)$. Otherwise, the session key should comprise an encryption key (for confidentiality) and a MAC key (for integrity), i.e., $k = k_{\text{enc}} || k_{\text{mac}}$, where $k_{\text{enc}} = \text{KDF}(K || \text{"JPAKE_ENC"})$ and $k_{\text{mac}} = \text{KDF}(K || \text{"JPAKE_MAC"})$. The exact choice of the KDF is left to specific applications to define.

2.3. Computational Cost

The computational cost is estimated based on counting the number of modular exponentiations since they are the predominant cost factors. Note that it takes one exponentiation to generate a Schnorr NIZK proof and two to verify it [RFC8235]. For Alice, she needs to perform 8 exponentiations in the first round, 4 in the second round, and 2 in the final computation of the session key. Hence, that is

14

modular exponentiations in total. Based on the symmetry, the computational cost for Bob is exactly the same.

3. J-PAKE over Elliptic Curve

3.1. Protocol Setup

The J-PAKE protocol works basically the same in the elliptic curve (EC) setting, except that the underlying multiplicative group over a finite field is replaced by an additive group over an elliptic curve.

Nonetheless, the EC version of J-PAKE is specified here for completeness.

When implemented over an elliptic curve, J-PAKE may use the same EC parameters as ECDSA [[FIPS186-4](#)]. The FIPS 186-4 standard [[FIPS186-4](#)]

defines three types of curves suitable for ECDSA: pseudorandom curves

over prime fields, pseudorandom curves over binary fields, and special curves over binary fields called Koblitz curves or anomalous binary curves. All these curves that are suitable for ECDSA can also

be used to implement J-PAKE. However, for illustration purposes, only curves over prime fields are described in this document. Typically, such curves include NIST P-256, P-384, and P-521. When choosing a curve, a level of 128-bit security or above is recommended. Let $E(\mathbb{F}_p)$ be an elliptic curve defined over a finite field \mathbb{F}_p , where p is a large prime. Let G be a generator for the subgroup over $E(\mathbb{F}_p)$ of prime order n . Here, the NIST curves are used

only as an example. Other secure curves such as Curve25519 are also suitable for implementation. The security proof of J-PAKE relies on the assumption that the DDH problem is intractable in the considered group.

As before, let s denote the shared secret between Alice and Bob. The

value of s falls within $[1, n-1]$. In particular, note that s MUST not be equal to $0 \pmod n$.

3.2. Two-Round Key Exchange

Round 1: Alice selects ephemeral private keys x_1 and x_2 uniformly at random from $[1, n-1]$. Similarly, Bob selects ephemeral private keys x_3 and x_4 uniformly at random from $[1, n-1]$.

o Alice -> Bob: $G_1 = G \times [x_1]$, $G_2 = G \times [x_2]$ and ZKPs for x_1 and x_2

o Bob -> Alice: $G_3 = G \times [x_3]$, $G_4 = G \times [x_4]$ and ZKPs for x_3 and x_4

When this round finishes, Alice and Bob verify the received ZKPs as specified in [[RFC8235](#)]. As an example, to prove the knowledge of the discrete logarithm of $D = G \times [d]$ with respect to the base point G ,

the ZKP contains: $\{\text{UserID}, V = G \times [v], r = v - d * c \text{ mod } n\}$, where UserID is the unique identifier for the prover, v is a number chosen uniformly at random from $[1, n-1]$ and $c = H(G || V || D || \text{UserID})$.

The verifier shall check the prover's UserID is a valid identity and is different from its own identity. If the verification of the ZKP fails, the session is aborted.

Round 2:

- o Alice -> Bob: $A = (G1 + G3 + G4) \times [x2*s]$ and a ZKP for $x2*s$
- o Bob -> Alice: $B = (G1 + G2 + G3) \times [x4*s]$ and a ZKP for $x4*s$

When the second round finishes, Alice and Bob verify the received ZKPs. The ZKPs are computed in the same way as in the previous round

except that the generator is different. For Alice, the new generator

is $G1 + G3 + G4$; for Bob, it is $G1 + G2 + G3$. Alice and Bob shall check that these new generators are not points at infinity. If any of these checks fails, the session is aborted. Otherwise, the two parties compute the common key material as follows:

- o Alice computes $Ka = (B - (G4 \times [x2*s])) \times [x2]$
- o Bob computes $Kb = (A - (G2 \times [x4*s])) \times [x4]$

Here, $Ka = Kb = G \times [(x1+x3) \times (x2 \times x4 \times s)]$. Let K denote the same key material held by both parties. Using K as input, Alice and Bob then apply a Key Derivation Function (KDF) to derive a common session key k .

3.3. Computational Cost

In the EC setting, the computational cost of J-PAKE is estimated based on counting the number of scalar multiplications over the elliptic curve. Note that it takes one multiplication to generate a Schnorr NIZK proof and one to verify it [RFC8235]. For Alice, she has to perform 6 multiplications in the first round, 3 in the second round, and 2 in the final computation of the session key. Hence, that is 11 multiplications in total. Based on the symmetry, the computational cost for Bob is exactly the same.

4. Three-Pass Variant

The two-round J-PAKE protocol is completely symmetric, which significantly simplifies the security analysis. In practice, one party normally initiates the communication and the other party responds. In that case, the protocol will be completed in three passes instead of two rounds. The two-round J-PAKE protocol can be trivially changed to three passes without losing security. Take the finite field setting as an example, and assume Alice initiates the key exchange. The three-pass variant works as follows:

1. Alice -> Bob: $g_1 = g^{x_1} \bmod p$, $g_2 = g^{x_2} \bmod p$, ZKPs for x_1 and x_2 .
2. Bob -> Alice: $g_3 = g^{x_3} \bmod p$, $g_4 = g^{x_4} \bmod p$,
 $B = (g_1 * g_2 * g_3)^{(x_4 * s)} \bmod p$, ZKPs for x_3 , x_4 , and $x_4 * s$.
3. Alice -> Bob: $A = (g_1 * g_3 * g_4)^{(x_2 * s)} \bmod p$ and a ZKP for $x_2 * s$.

Both parties compute the session keys in exactly the same way as before.

5. Key Confirmation

The two-round J-PAKE protocol (or the three-pass variant) provides cryptographic guarantee that only the authenticated party who used the same password at the other end is able to compute the same session key. So far, the authentication is only implicit. The key confirmation is also implicit [[Stinson06](#)]. The two parties may use the derived key straight away to start secure communication by encrypting messages in an authenticated mode. Only the party with the same derived session key will be able to decrypt and read those messages.

For achieving explicit authentication, an additional key confirmation procedure should be performed. This provides explicit assurance that the other party has actually derived the same key. In this case, the key confirmation is explicit [[Stinson06](#)].

In J-PAKE, explicit key confirmation is recommended whenever the network bandwidth allows it. It has the benefit of providing explicit and immediate confirmation if the two parties have derived the same key and hence are authenticated to each other. This allows a practical implementation of J-PAKE to effectively detect online dictionary attacks (if any), and stop them accordingly by setting a threshold for the consecutively failed connection attempts.

To achieve explicit key confirmation, there are several methods available. They are generically applicable to all key exchange protocols, not just J-PAKE. In general, it is recommended that a different key from the session key be used for key confirmation -- say, $k' = \text{KDF}(K \parallel \text{"JPAKE_KC"})$. The advantage of using a different key for key confirmation is that the session key remains indistinguishable from random after the key confirmation process. (However, this perceived advantage is actually subtle and only theoretical.) Two explicit key confirmation methods are presented here.

The first method is based on the one used in the SPEKE protocol [[Jab96](#)]. Suppose Alice initiates the key confirmation. Alice sends to Bob $H(H(k'))$, which Bob will verify. If the verification is successful, Bob sends back to Alice $H(k')$, which Alice will verify. This key confirmation procedure needs to be completed in two rounds, as shown below.

1. Alice -> Bob: $H(H(k'))$
2. Bob -> Alice: $H(k')$

The above procedure requires two rounds instead of one, because the second message depends on the first. If both parties attempt to send

the first message at the same time without an agreed order, they cannot tell if the message that they receive is a genuine challenge or a replayed message, and consequently may enter a deadlock.

The second method is based on the unilateral key confirmation scheme specified in NIST SP 800-56A Revision 1 [[BJS07](#)]. Alice and Bob send to each other a MAC tag, which they will verify accordingly. This key confirmation procedure can be completed in one round.

In the finite field setting, it works as follows.

- o Alice -> Bob: $\text{MacTagAlice} = \text{MAC}(k', \text{"KC_1_U"} \parallel \text{Alice} \parallel \text{Bob} \parallel g1 \parallel g2 \parallel g3 \parallel g4)$
- o Bob -> Alice: $\text{MacTagBob} = \text{MAC}(k', \text{"KC_1_U"} \parallel \text{Bob} \parallel \text{Alice} \parallel g3 \parallel g4 \parallel g1 \parallel g2)$

In the EC setting, the key confirmation works basically the same.

- o Alice -> Bob: $\text{MacTagAlice} = \text{MAC}(k', \text{"KC_1_U"} \parallel \text{Alice} \parallel \text{Bob} \parallel G1 \parallel G2 \parallel G3 \parallel G4)$
- o Bob -> Alice: $\text{MacTagBob} = \text{MAC}(k', \text{"KC_1_U"} \parallel \text{Bob} \parallel \text{Alice} \parallel G3 \parallel G4 \parallel G1 \parallel G2)$

The second method assumes an additional secure MAC function (e.g., one may use HMAC) and is slightly more complex than the first method.

However, it can be completed within one round and it preserves the overall symmetry of the protocol implementation. For this reason, the second method is RECOMMENDED.

6. Security Considerations

A PAKE protocol is designed to provide two functions in one protocol execution. The first one is to provide zero-knowledge authentication

of a password. It is called "zero knowledge" because at the end of the protocol, the two communicating parties will learn nothing more than one bit information: whether the passwords supplied at two ends are equal. Therefore, a PAKE protocol is naturally resistant against

phishing attacks. The second function is to provide session key establishment if the two passwords are equal. The session key will be used to protect the confidentiality and integrity of the subsequent communication.

More concretely, a secure PAKE protocol shall satisfy the following security requirements [[HR10](#)].

1. Offline dictionary attack resistance: It does not leak any information that allows a passive/active attacker to perform offline exhaustive search of the password.
2. Forward secrecy: It produces session keys that remain secure even when the password is later disclosed.
3. Known-key security: It prevents a disclosed session key from affecting the security of other sessions.
4. Online dictionary attack resistance: It limits an active attacker to test only one password per protocol execution.

First, a PAKE protocol must resist offline dictionary attacks. A password is inherently weak. Typically, it has only about 20-30 bits entropy. This level of security is subject to exhaustive search. Therefore, in the PAKE protocol, the communication must not reveal any data that allows an attacker to learn the password through offline exhaustive search.

Second, a PAKE protocol must provide forward secrecy. The key exchange is authenticated based on a shared password. However, there is no guarantee on the long-term secrecy of the password. A secure PAKE scheme shall protect past session keys even when the password is later disclosed. This property also implies that if an attacker knows the password but only passively observes the key exchange, he cannot learn the session key.

Third, a PAKE protocol must provide known key security. A session

key lasts throughout the session. An exposed session key must not cause any global impact on the system, affecting the security of other sessions.

Finally, a PAKE protocol must resist online dictionary attacks. If the attacker is directly engaging in the key exchange, there is no way to prevent such an attacker trying a random guess of the password. However, a secure PAKE scheme should minimize the effect of the online attack. In the best case, the attacker can only guess exactly one password per impersonation attempt. Consecutively failed attempts can be easily detected, and the subsequent attempts shall be thwarted accordingly. It is recommended that the false authentication counter be handled in such a way that any error (which causes the session to fail during the key exchange or key confirmation) leads to incrementing the false authentication counter.

It has been proven in [[HR10](#)] that J-PAKE satisfies all of the four requirements based on the assumptions that the Decisional Diffie-Hellman problem is intractable and the underlying Schnorr NIZK proof is secure. An independent study that proves security of J-PAKE in a model with algebraic adversaries and random oracles can be found in [[ABM15](#)]. By comparison, it has been known that EKE has the problem of leaking partial information about the password to a passive attacker, hence not satisfying the first requirement [[Jas96](#)]. For SPEKE and SRP-6, an attacker may be able to test more than one password in one online dictionary attack (see [[Zha04](#)] and [[Hao10](#)]), hence they do not satisfy the fourth requirement in the strict theoretical sense. Furthermore, SPEKE is found vulnerable to an impersonation attack and a key-malleability attack [[HS14](#)]. These two attacks affect the SPEKE protocol specified in Jablon's original 1996 paper [[Jab96](#)] as well in the D26 draft of IEEE P1363.2 and the ISO/IEC 11770-4:2006 standard. As a result, the specification of SPEKE in ISO/IEC 11770-4:2006 has been revised to address the identified problems.

7. IANA Considerations

This document does not require any IANA actions.

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Hao
12]

Informational

[Page

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