

Connection Setup in a Quantum Network

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draft-van-meter-qirg-quantum-connection-setup-00

QIRG @IRTF/IETF104

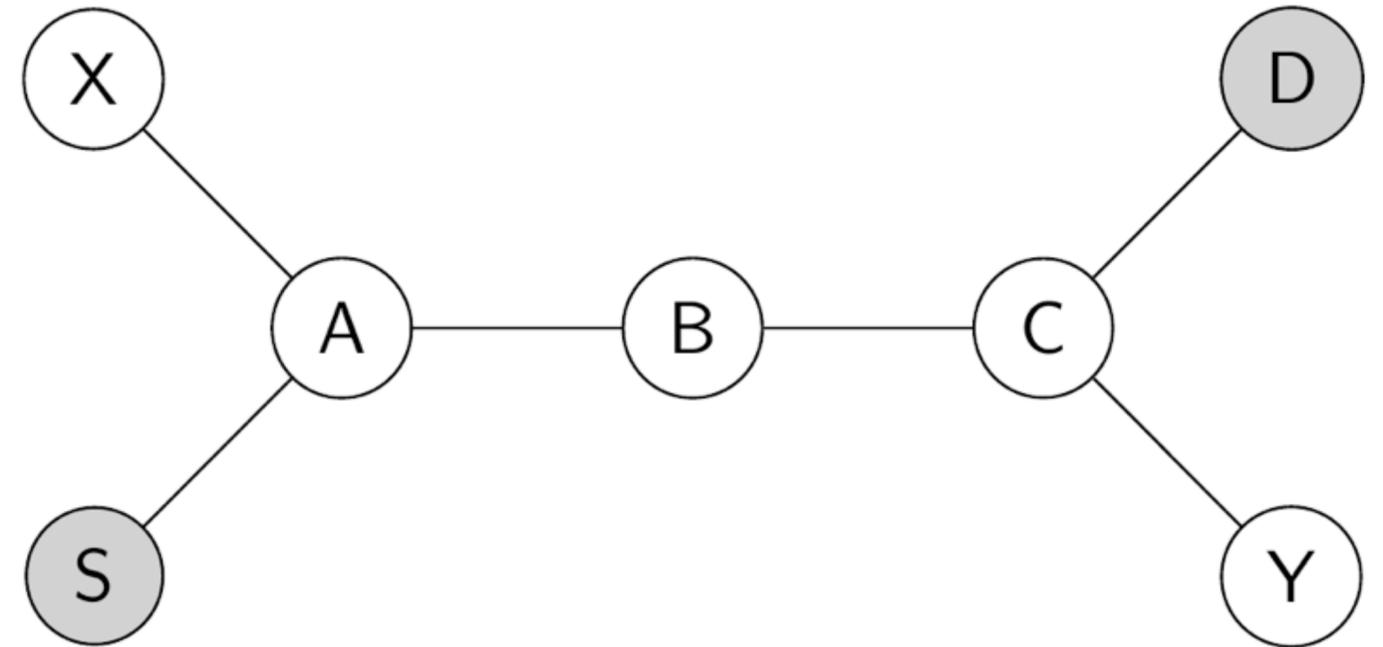
Prague

2019/3/26

Quantum Connection

Distribution of end-to-end Bell pairs:

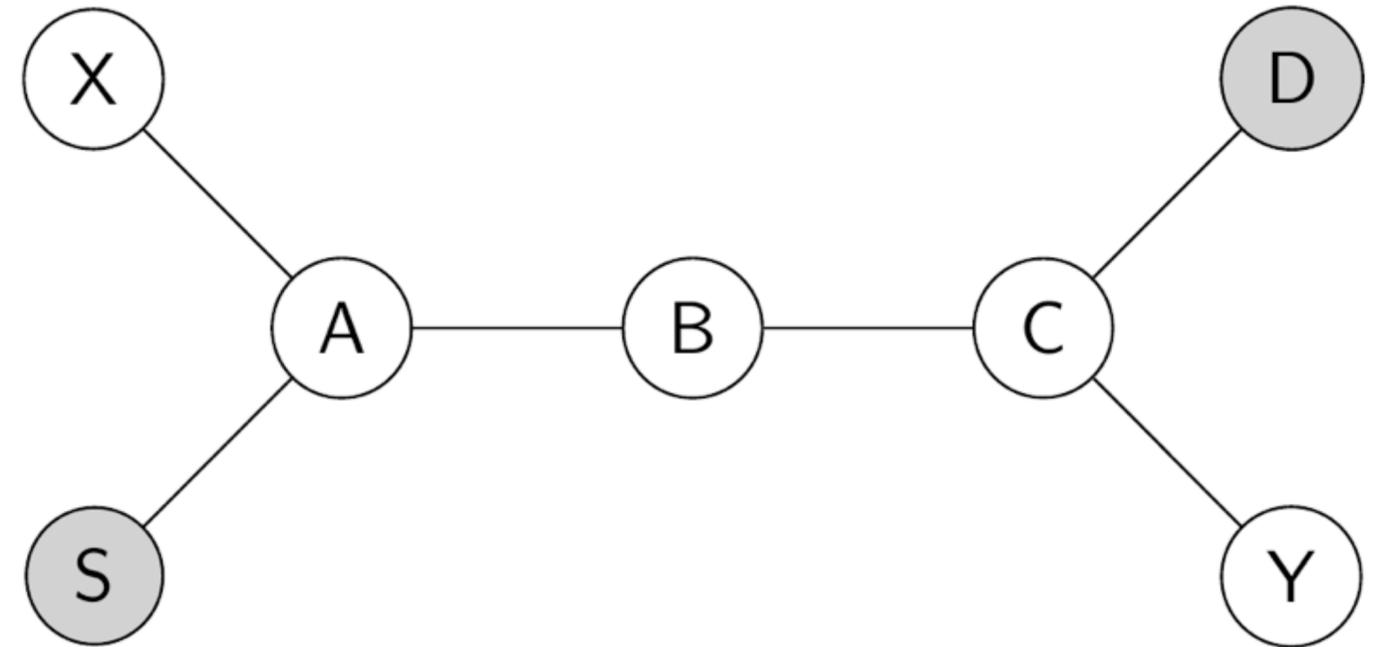
- On request from source node S
- Middle nodes perform entanglement swapping and error management



Quantum Connection

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- On request from source node S
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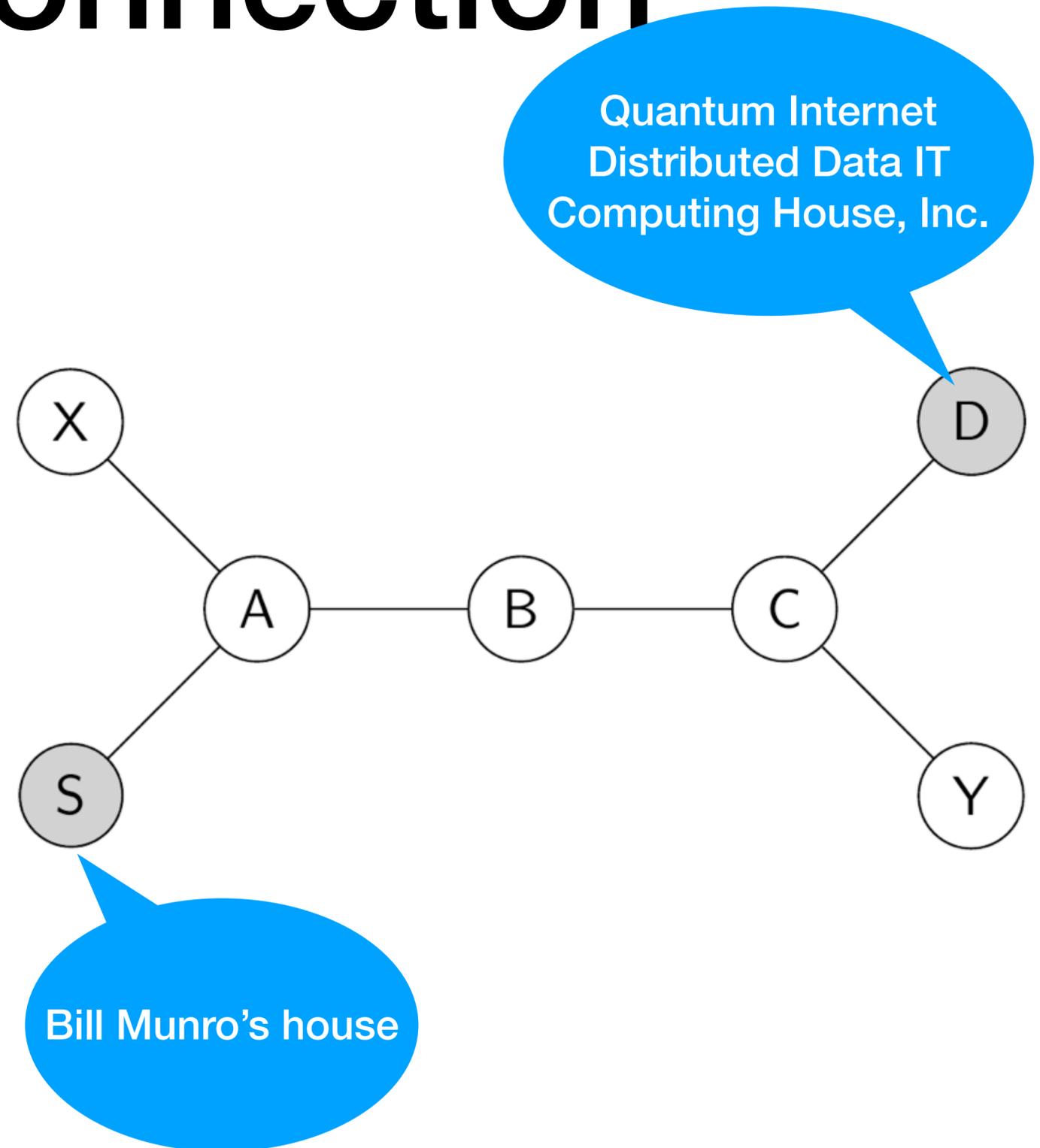


Bill Munro's house

Quantum Connection

Distribution of end-to-end Bell pairs:

- On request from source node S
- Middle nodes perform entanglement swapping and error management



Quantum Connection

QUIDDITCH

Distribution of end-to-end Bell pairs:

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- Middle nodes perform entanglement swapping and error management

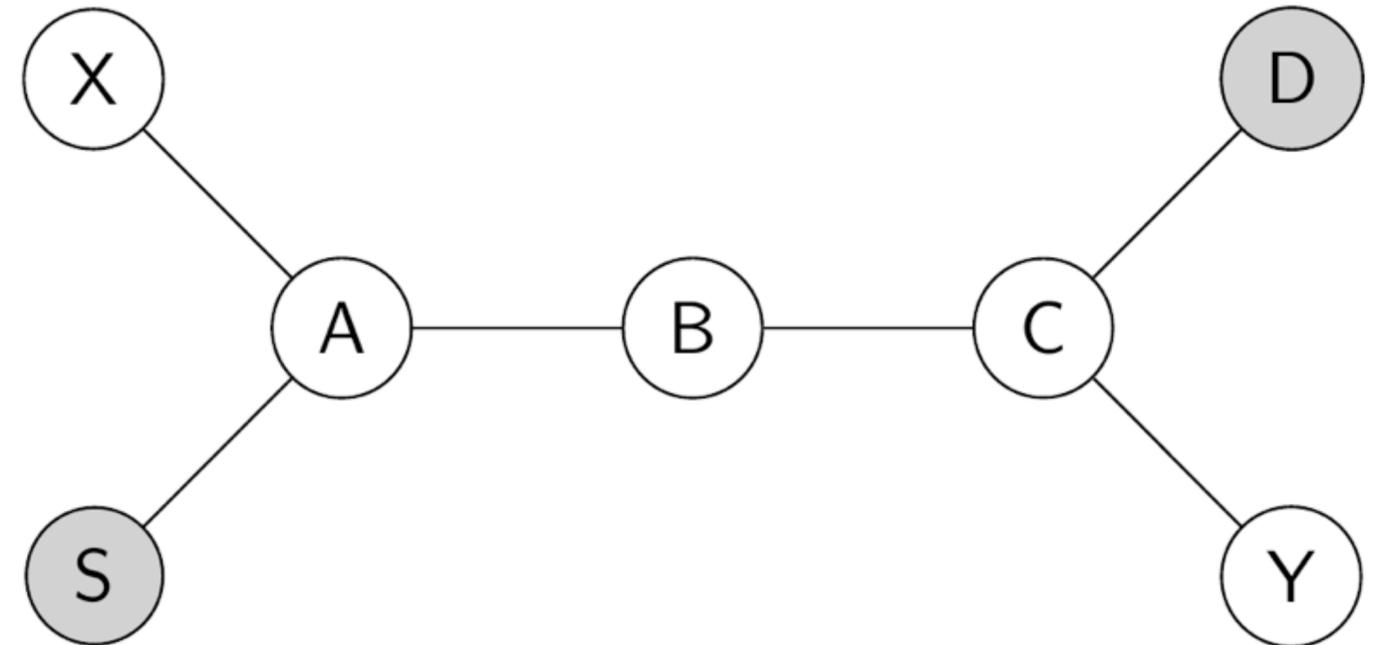


Bill Munro's house

Quantum Connection

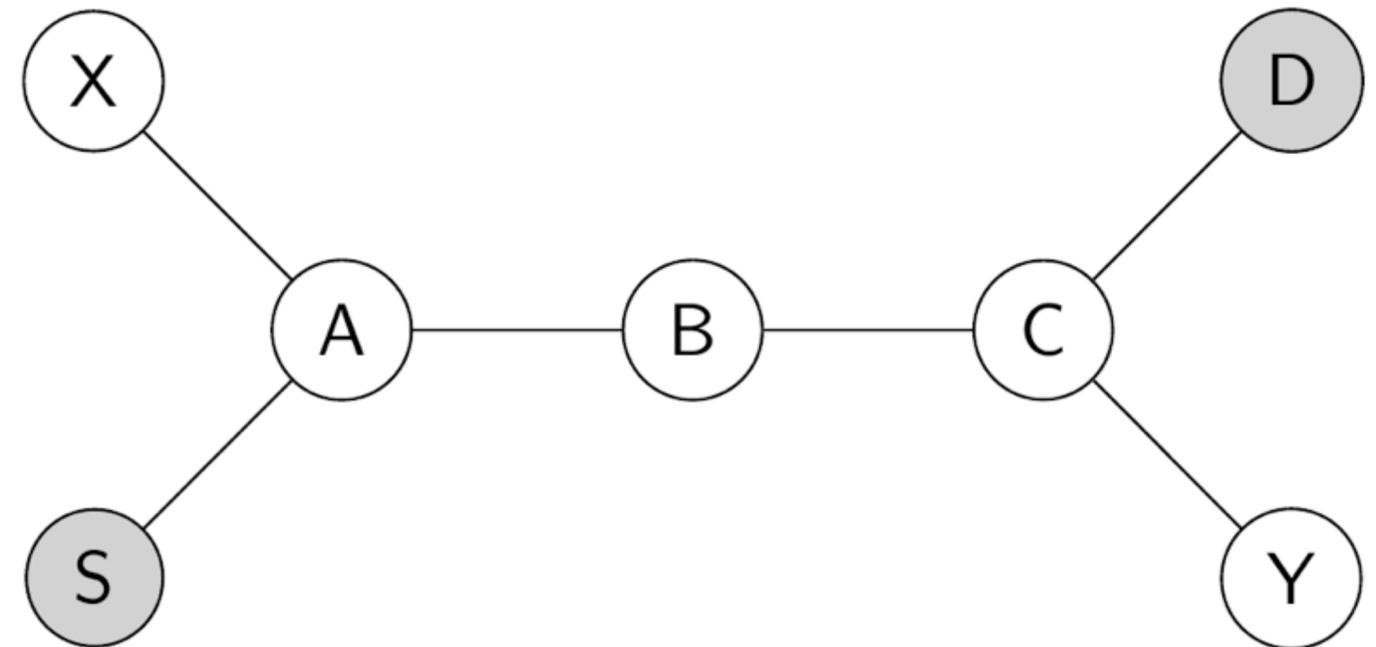
Distribution of end-to-end Bell pairs:

- On request from source node S
- Middle nodes perform entanglement swapping and error management



Stages of the Problem

- Need to select a path (routing)
(rdv et al., *Networking Science* 2013)
- **Plan sequences of operations**
- **Convey sequences to nodes**



Constraints/assumptions

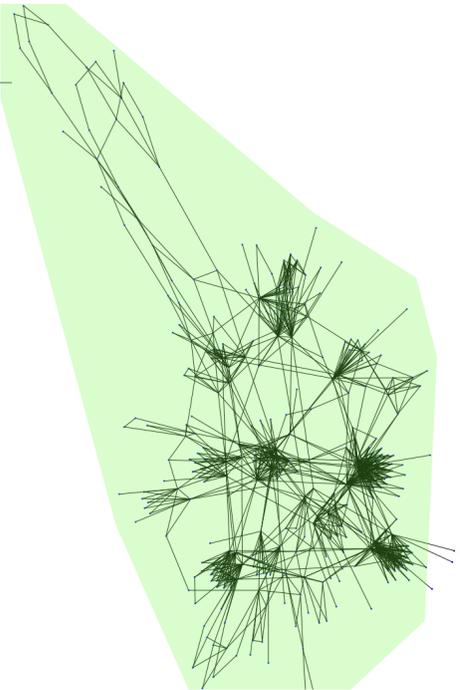
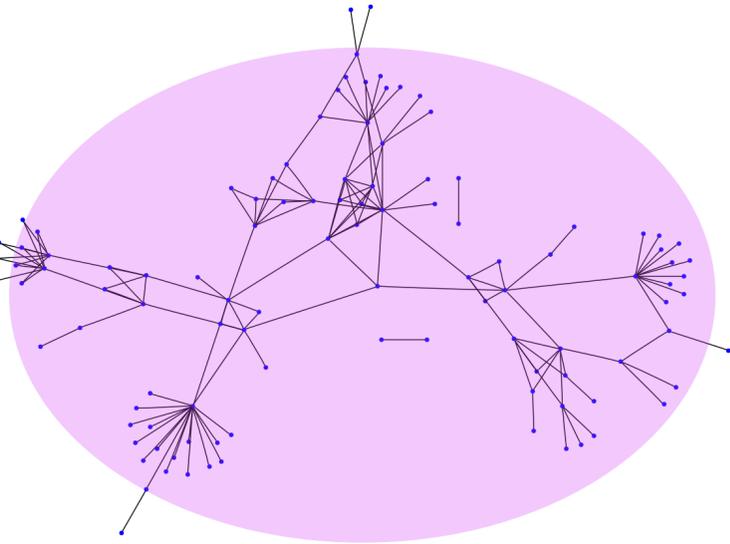
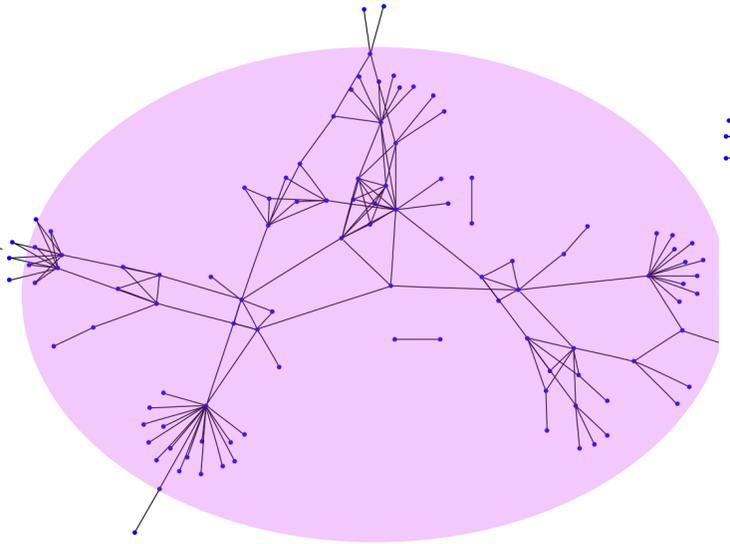
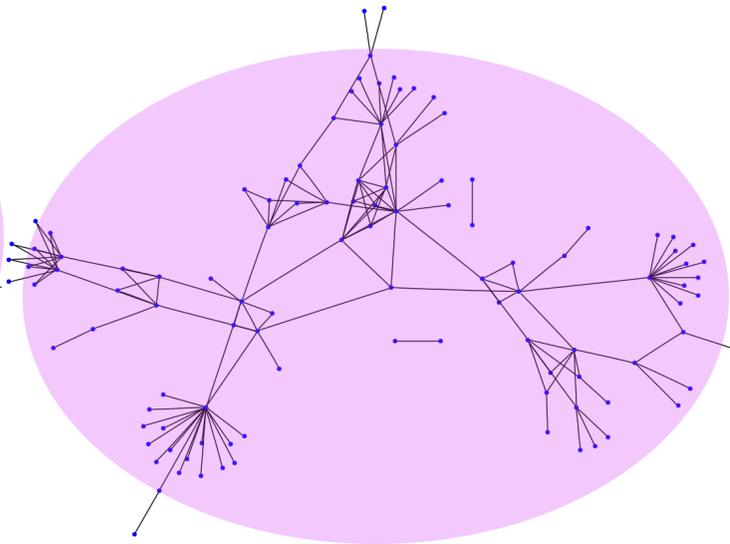
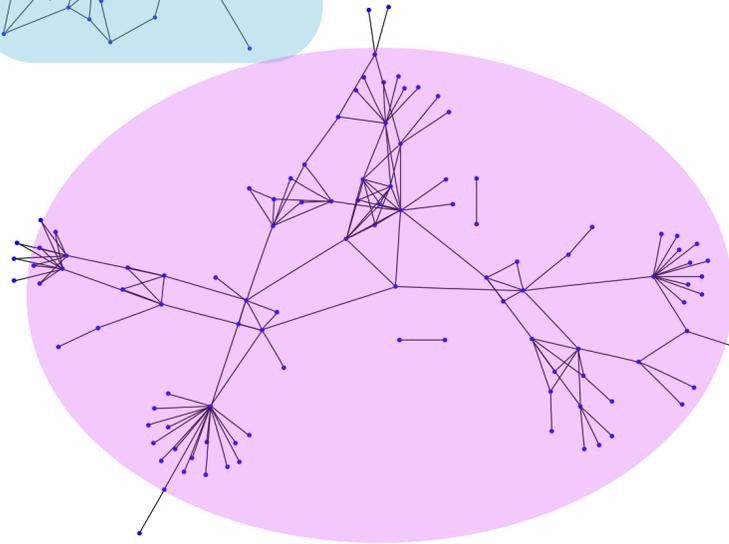
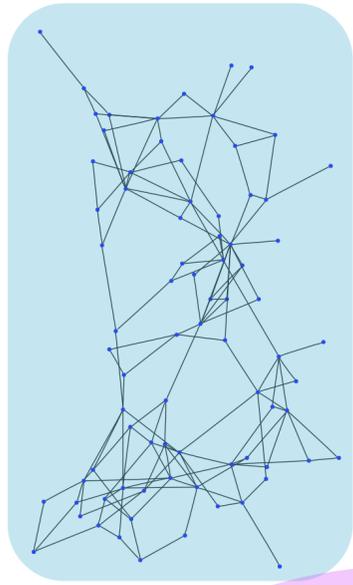
- Links are heterogeneous and not *a priori* known
- Resource management (multiplexing scheme) beyond today's scope, but critically important

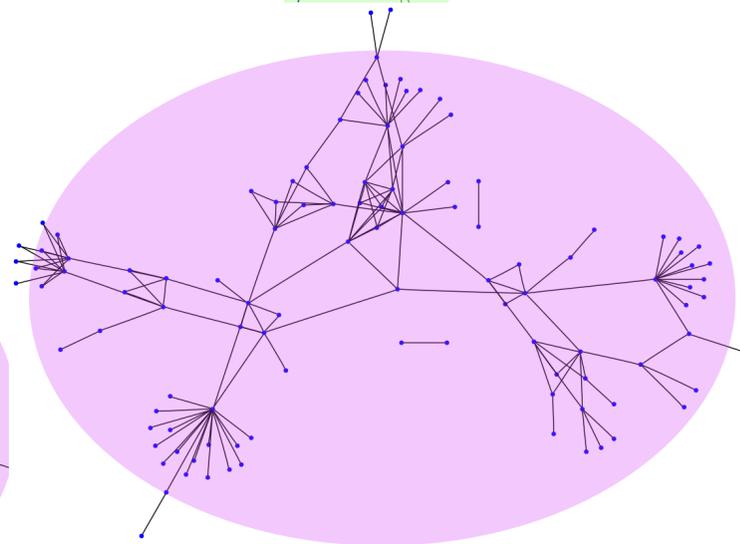
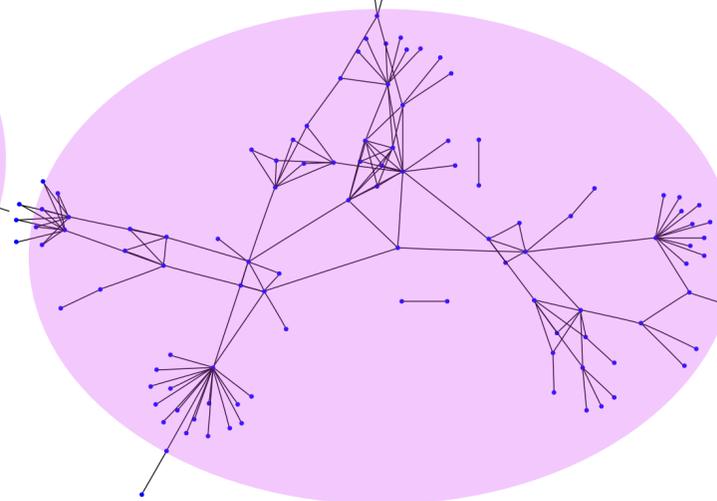
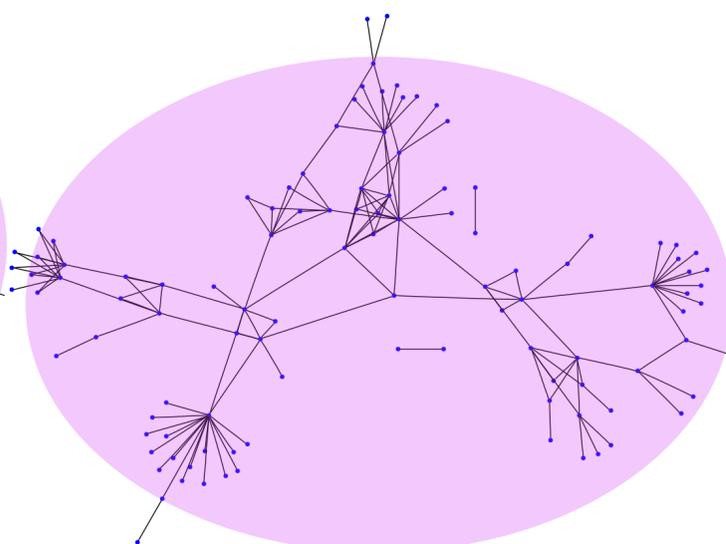
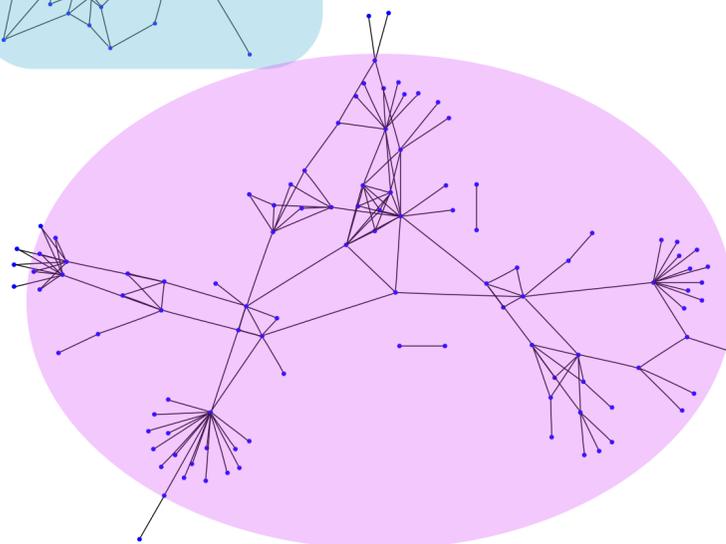
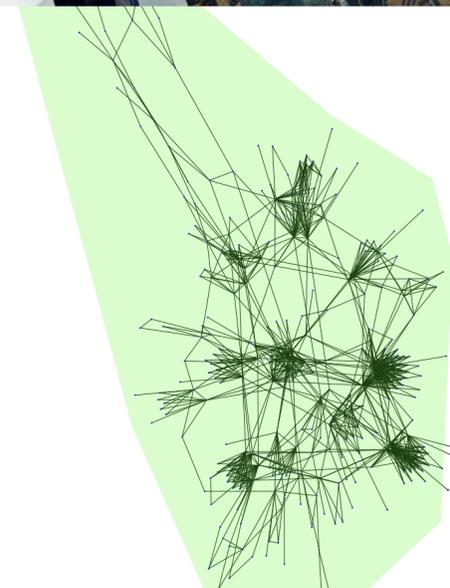
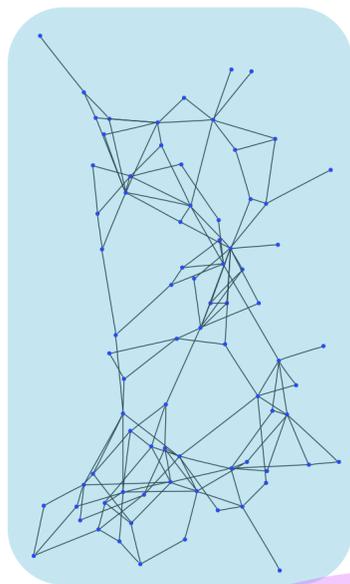
Information Each Node Holds

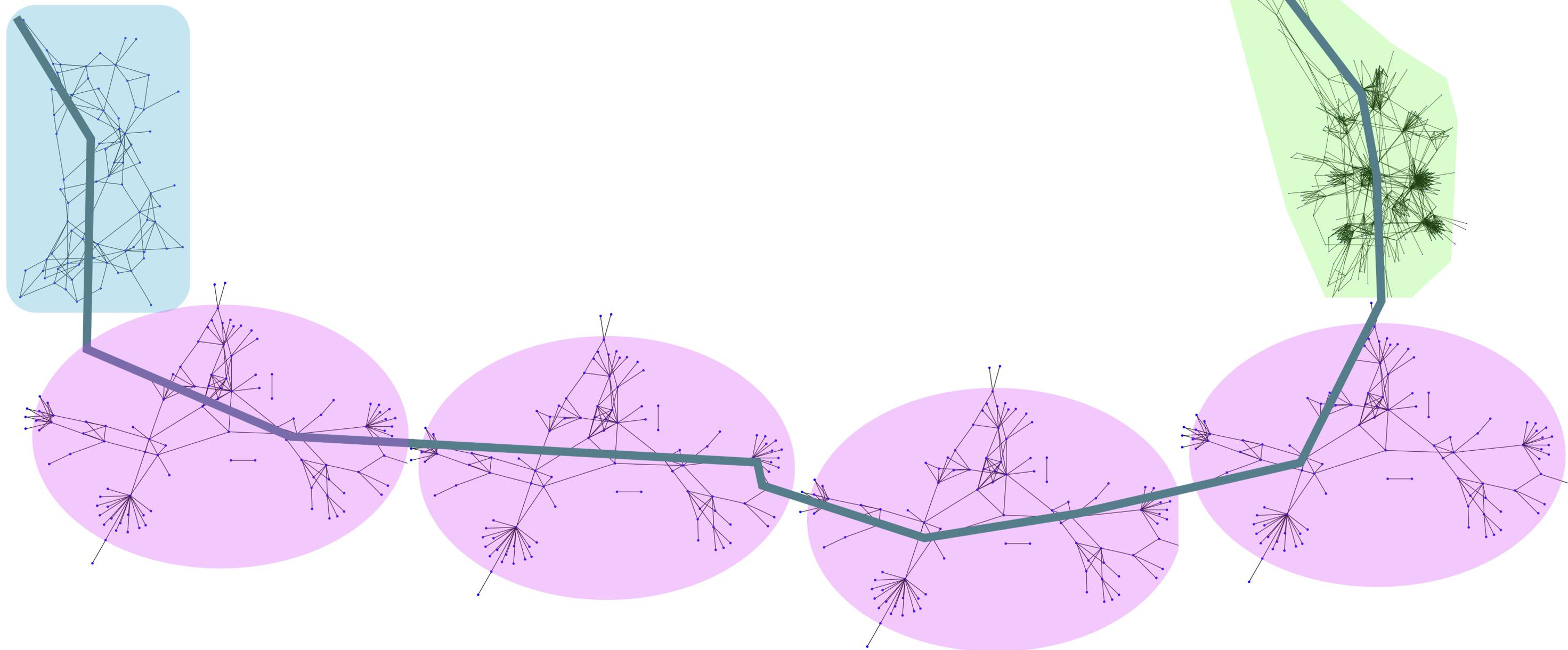
- Its own capabilities
 - amount of memory, memory lifetime
 - gate fidelities
- Link information
 - who neighbors are
 - link entanglement trial rate, success probability, fidelity (or full density matrix)
- Topology of the *local* network, with a routing metric
- Where the gateway to the outside world is

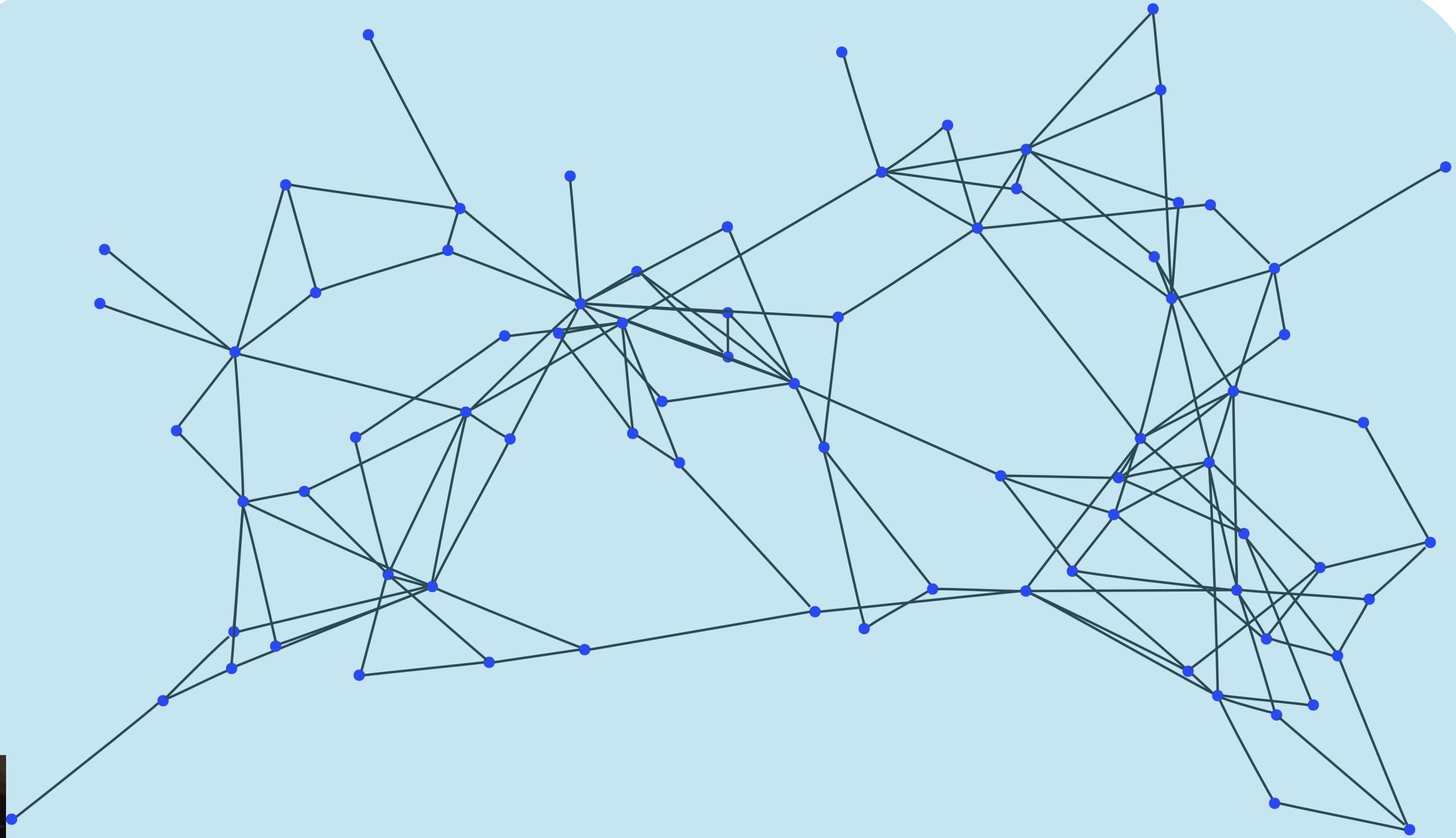
Information Each Node Does *Not* Have

- Full density matrix of the base Bell pairs generated by every node
- Number of qubits in every “QNIC” in the whole network
- Local gate fidelities for other nodes
- Anything at all about the internals of neighboring networks

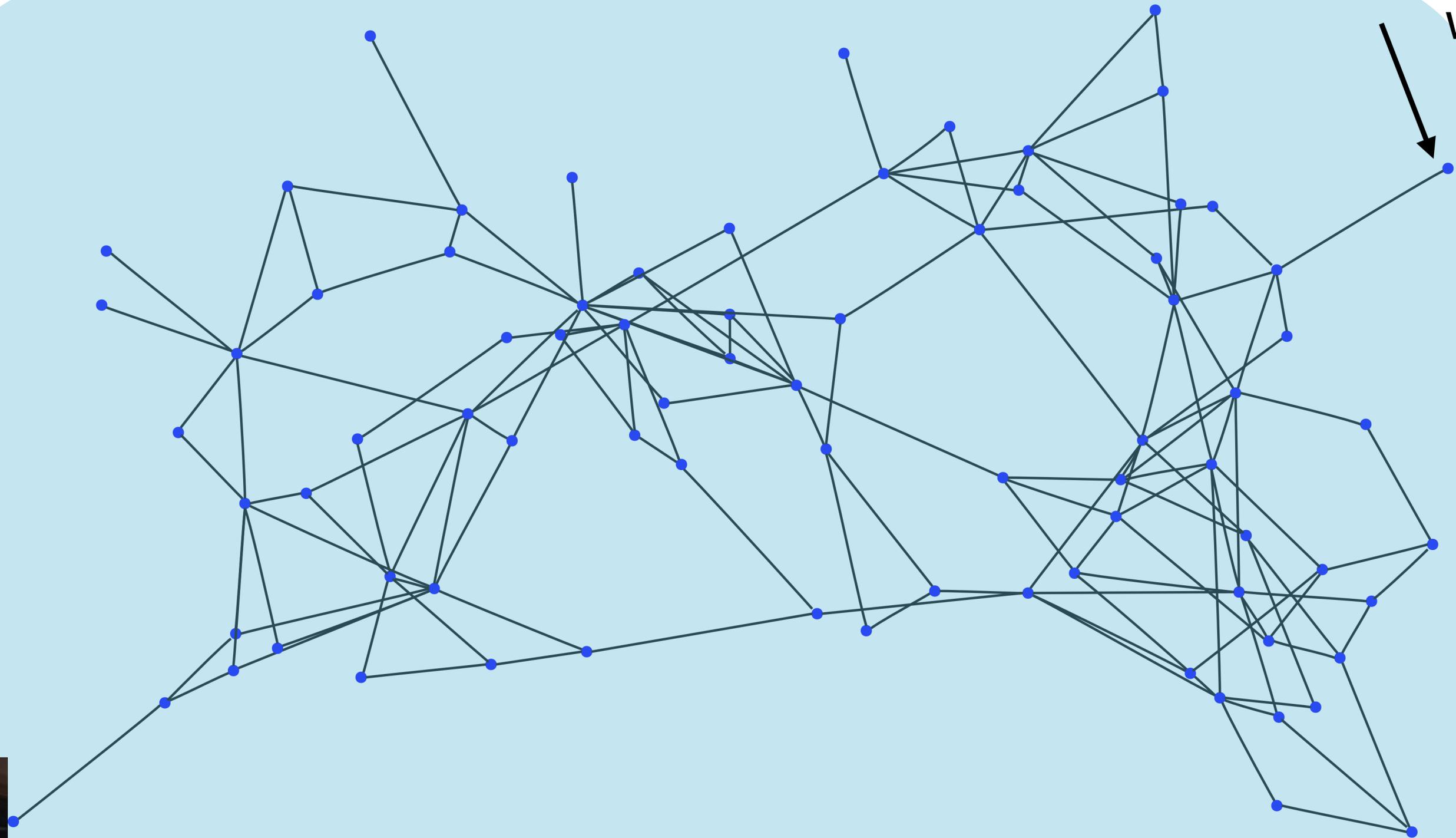




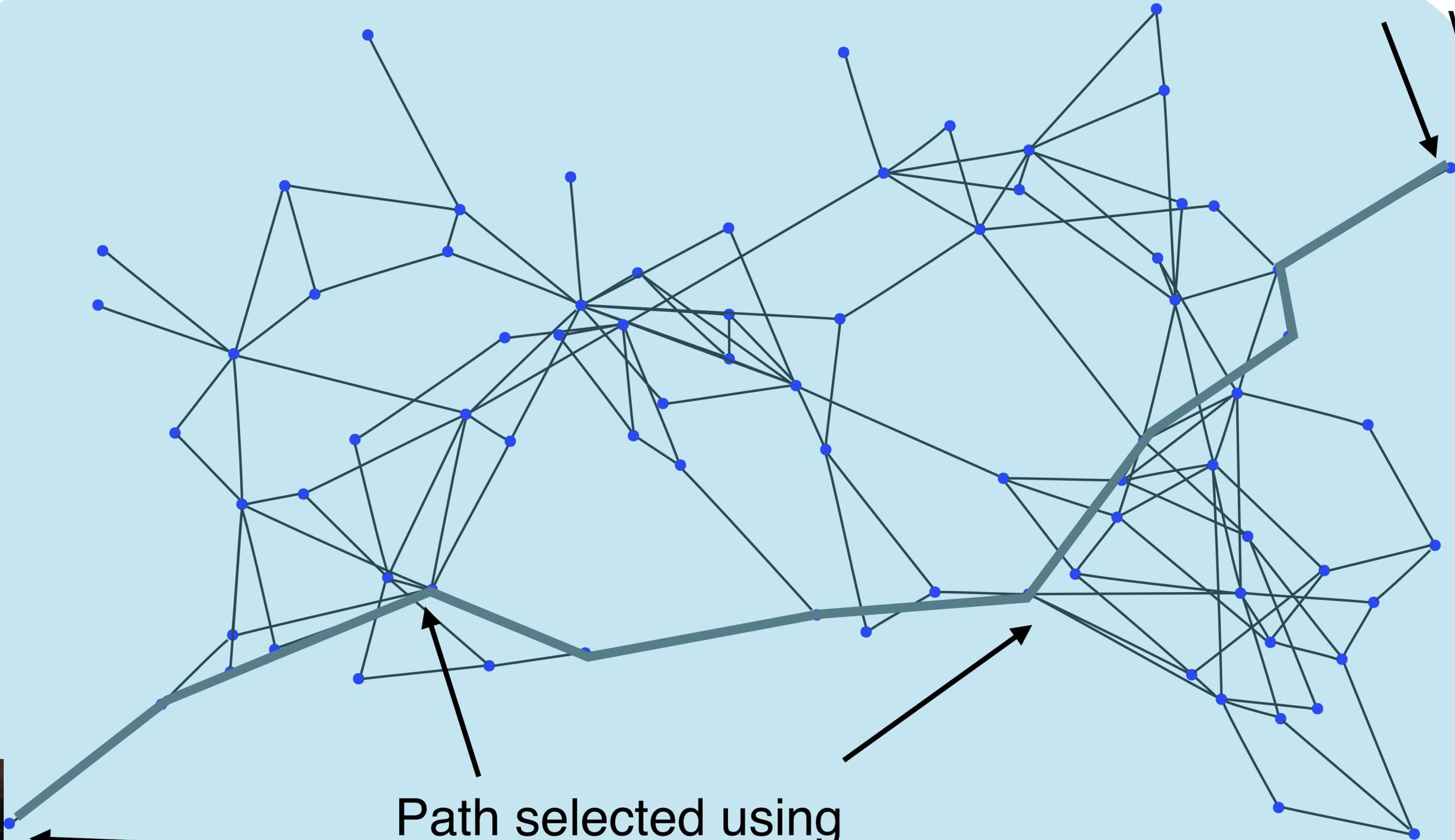




Gateway to the outer world

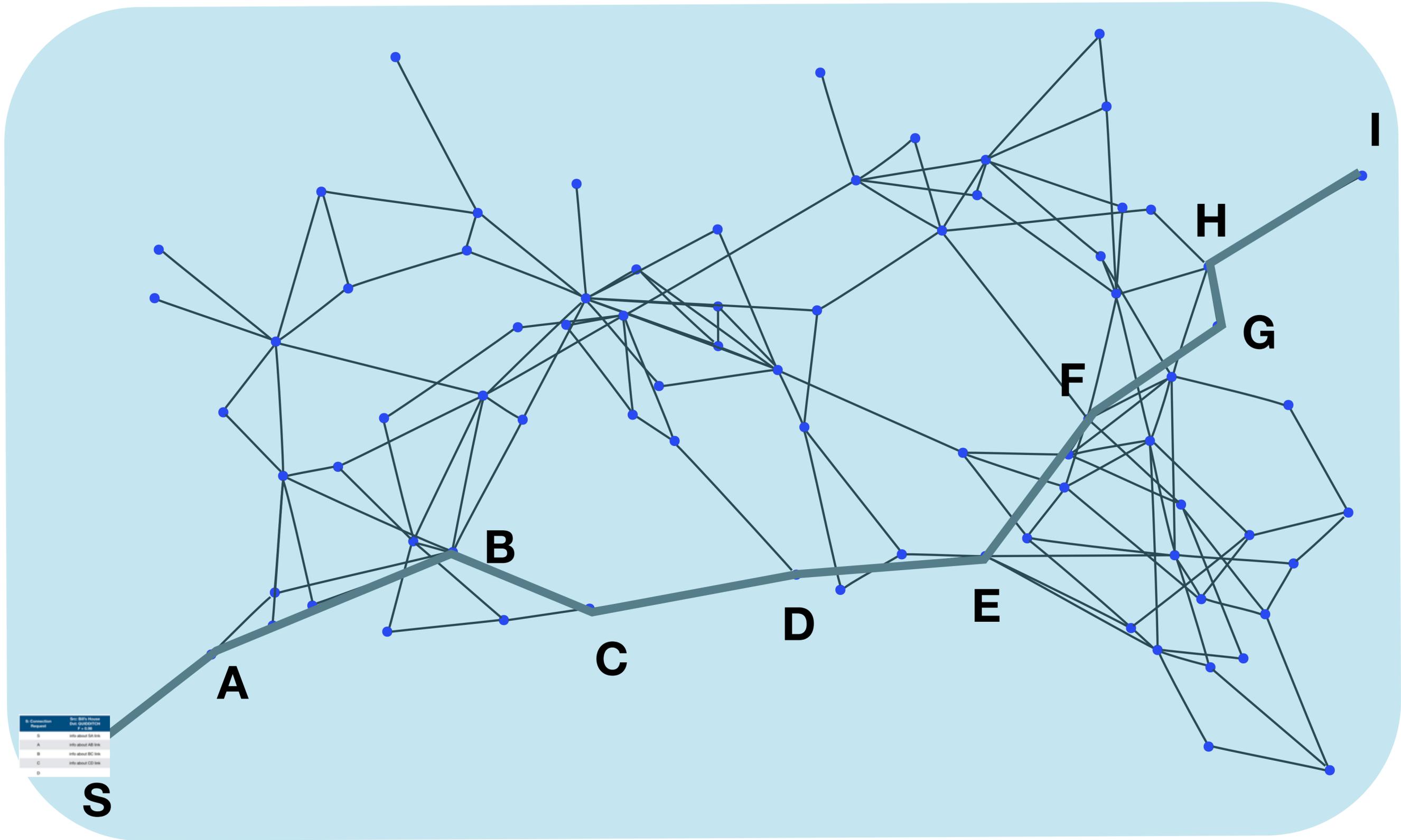


Gateway to the outer world



Path selected using minimal information



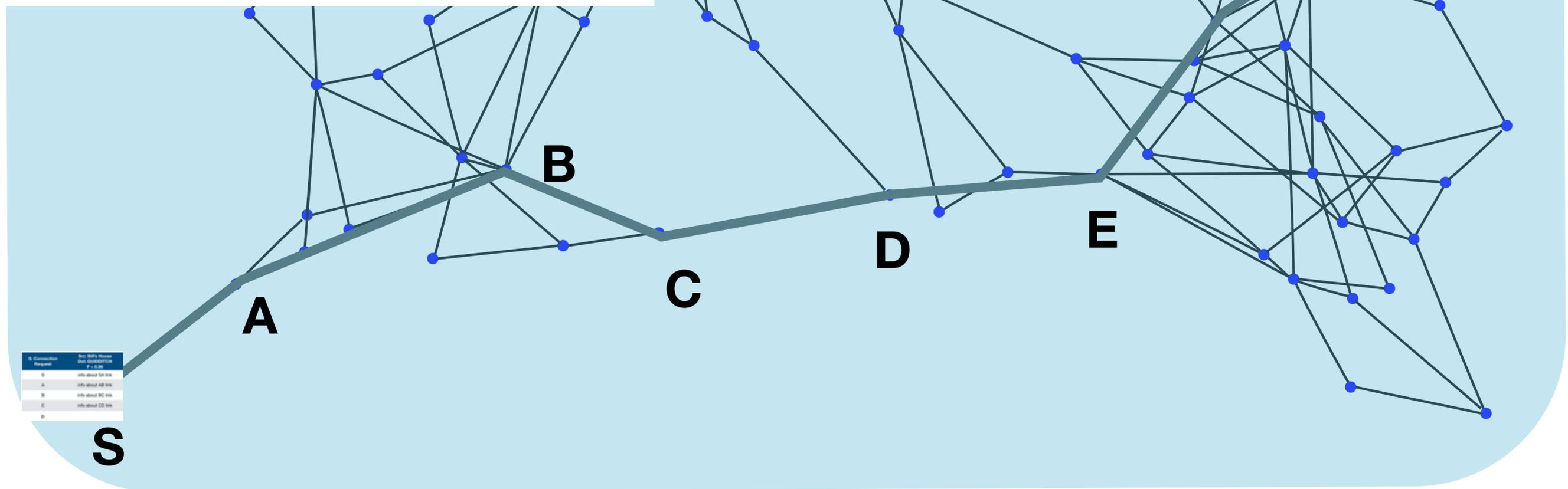


S: Connection Request

Src: Bill's House
Dst: QUIDDITCH
F = 0.98

S

info about SA link



S: Connection Request

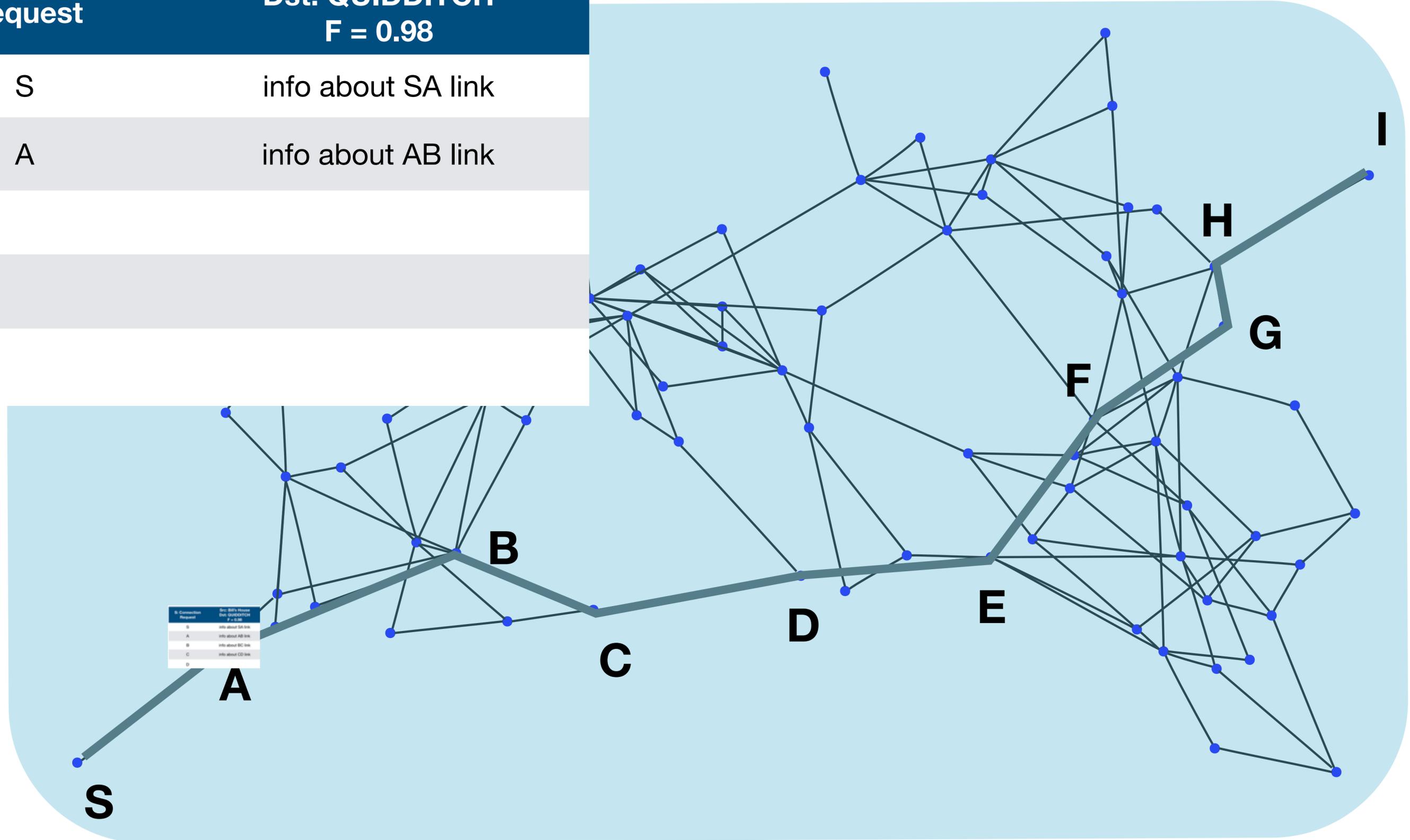
Src: Bill's House
Dst: QUIDDITCH
F = 0.98

S

info about SA link

A

info about AB link



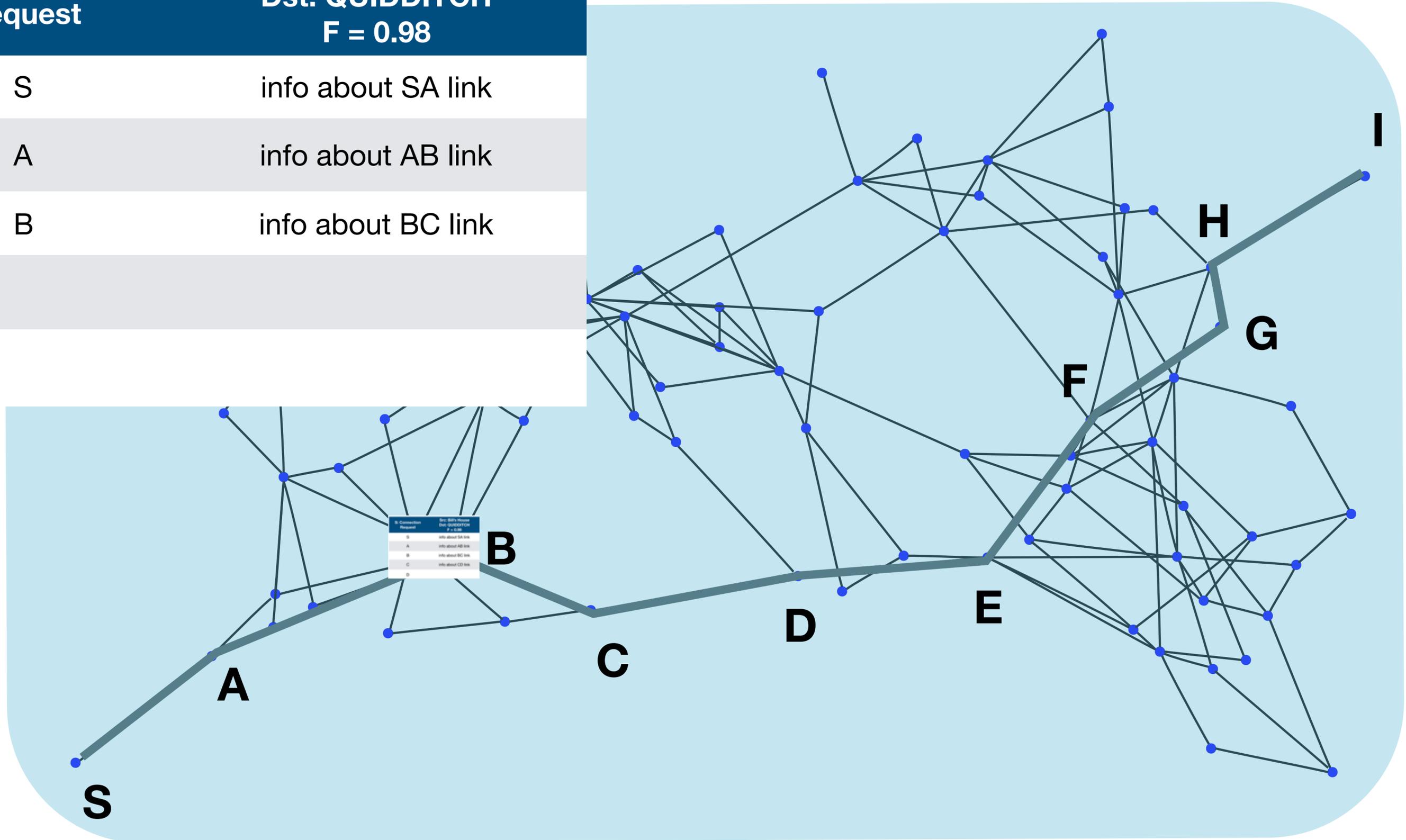
S: Connection Request

Src: Bill's House
Dst: QUIDDITCH
F = 0.98

S info about SA link

A info about AB link

B info about BC link



S: Connection Request

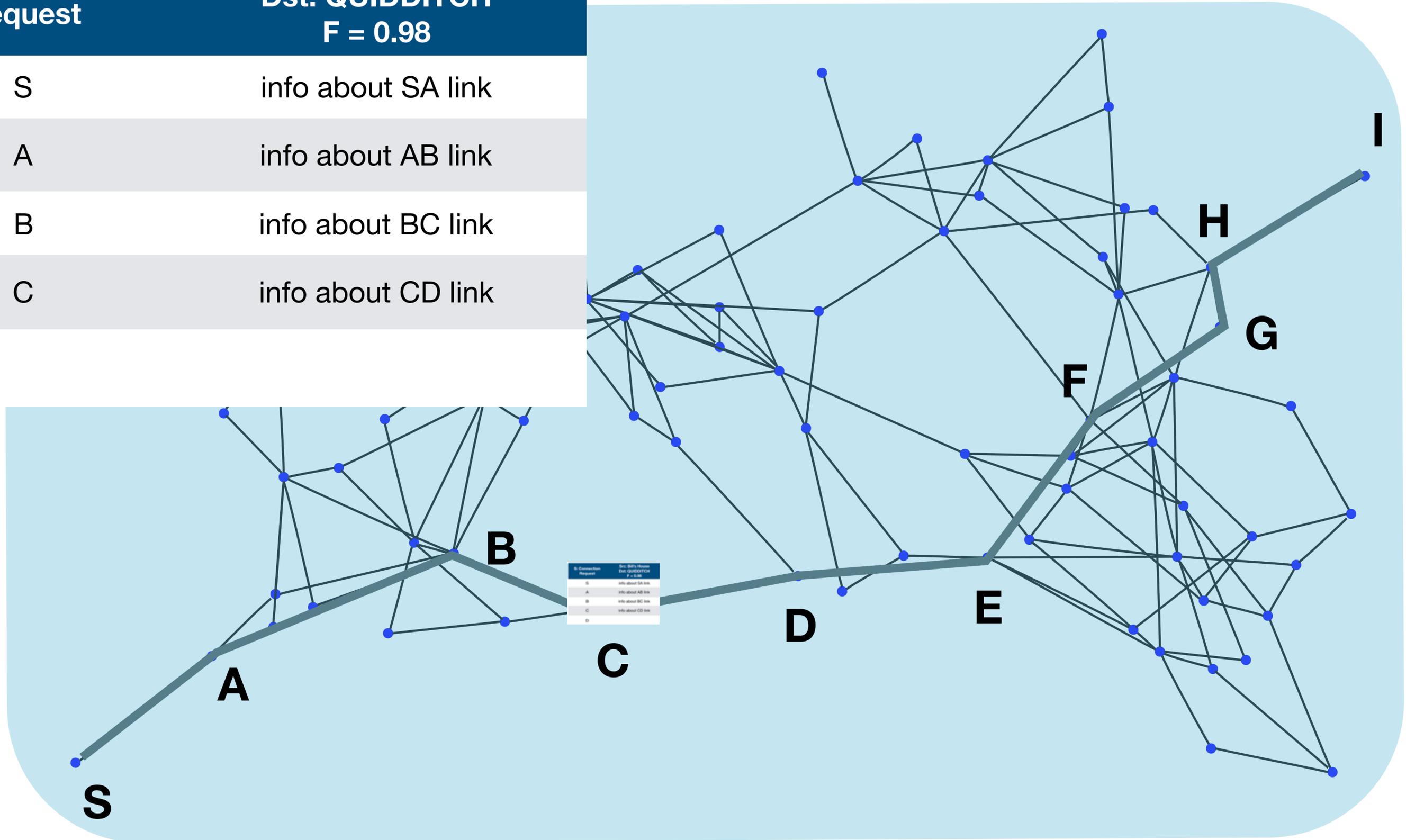
Src: Bill's House
Dst: QUIDDITCH
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S info about SA link

A info about AB link

B info about BC link

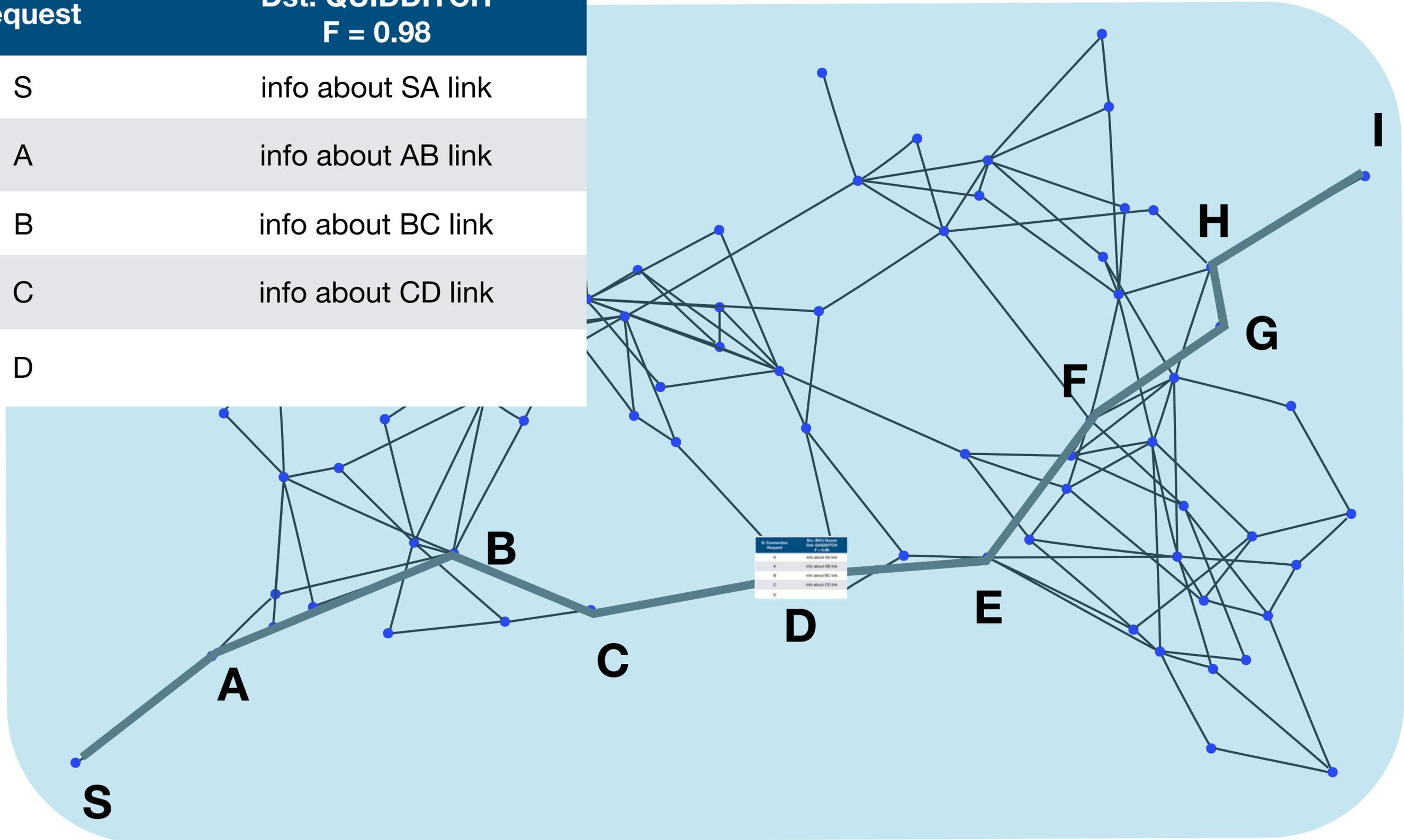
C info about CD link



S: Connection Request

Src: Bill's House
Dst: QUIDDITCH
F = 0.98

- S info about SA link
- A info about AB link
- B info about BC link
- C info about CD link
- D



S: Connection Request

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F = 0.98

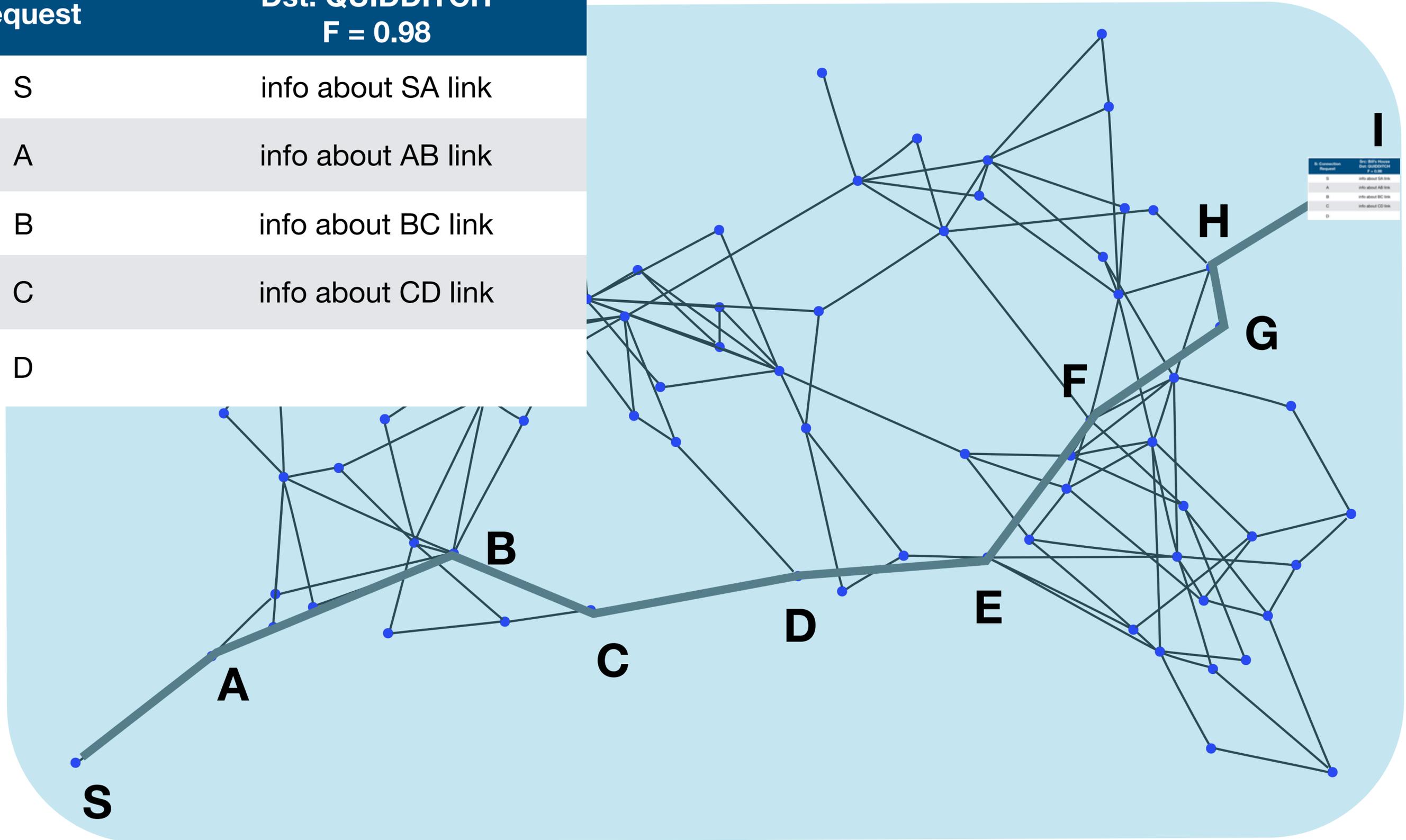
S info about SA link

A info about AB link

B info about BC link

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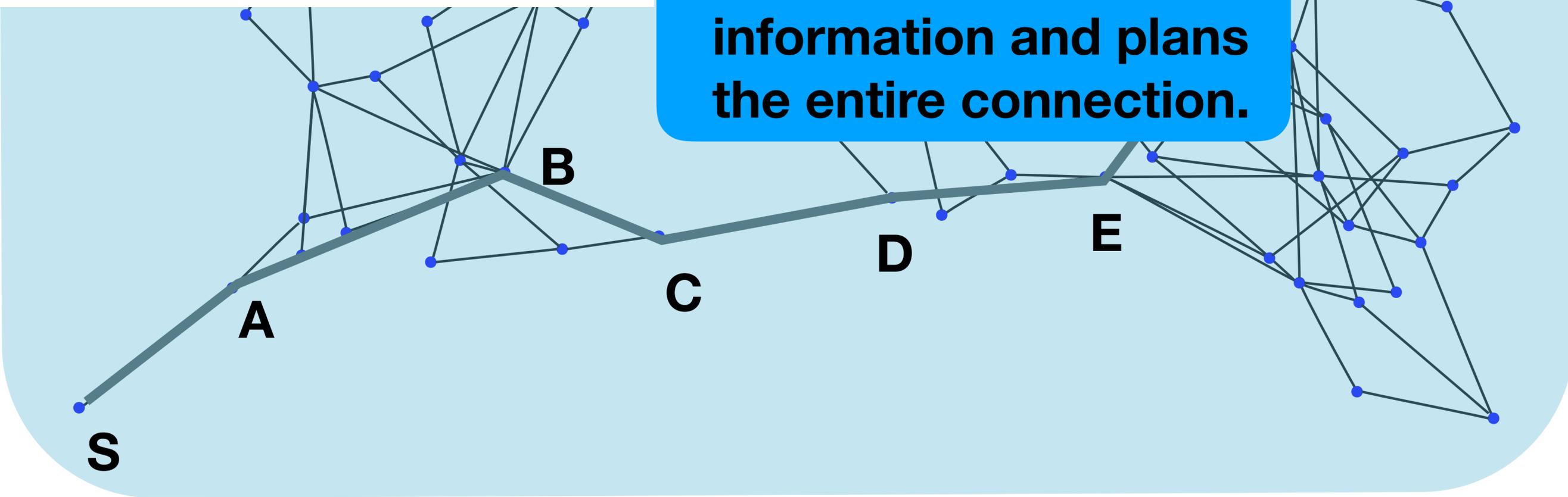
B info about BC link

C info about CD link

D

Node I now takes that information and plans the entire connection.

Node	Info
S	info about SA link
A	info about AB link
B	info about BC link
C	info about CD link
D	

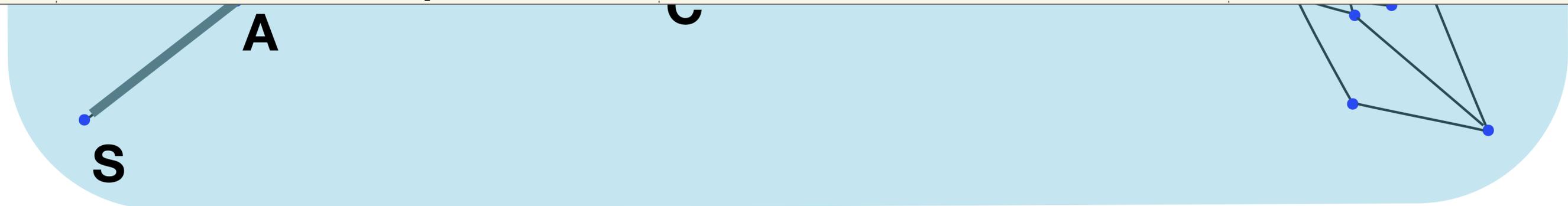


D: Path Setup	Src: Bill's House Dst: QUIDDITCH F = 0.98		
S	conditions to purify conditions to swap		
A	conditions to purify conditions to swap		
B	purify if $FG < 0.98$, $EF < 0.98$ else swap		
C	purify if $BC < 0.98$, $CD < 0.98$	purify if $AC < 0.98$, $CE < 0.98$ else swap	
D	purify if $CD < 0.98$, $DE < 0.98$ else swap		
E	purify if $DE < 0.98$, $EF < 0.98$	purify if $CE < 0.98$, $EG < 0.98$	purify if $AE < 0.98$, $EI < 0.98$ else swap
F	purify if $EF < 0.98$, $FG < 0.98$ else swap		
G	purify if $FG < 0.98$, $GH < 0.98$	purify if $EG < 0.98$, $GI < 0.98$ else swap	
H	purify if $GH < 0.98$, $HI < 0.98$ else swap		

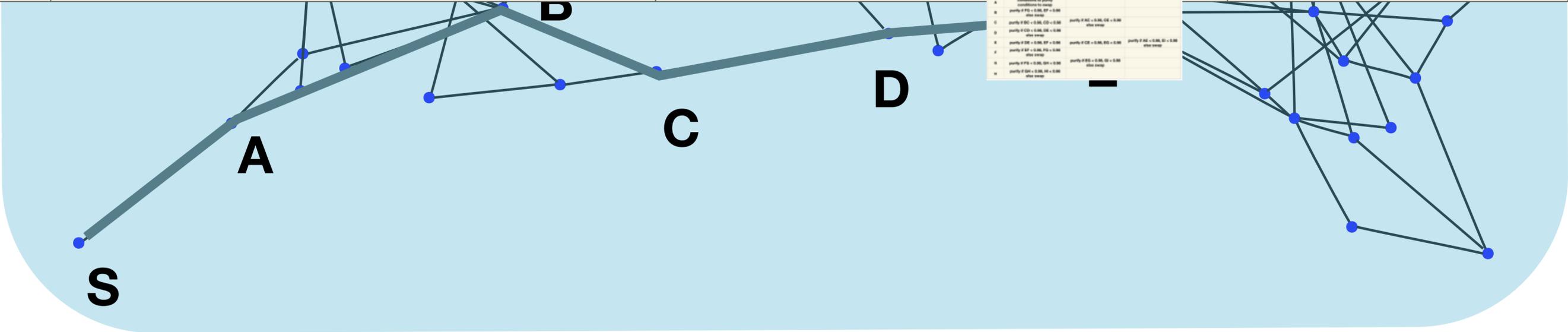
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S

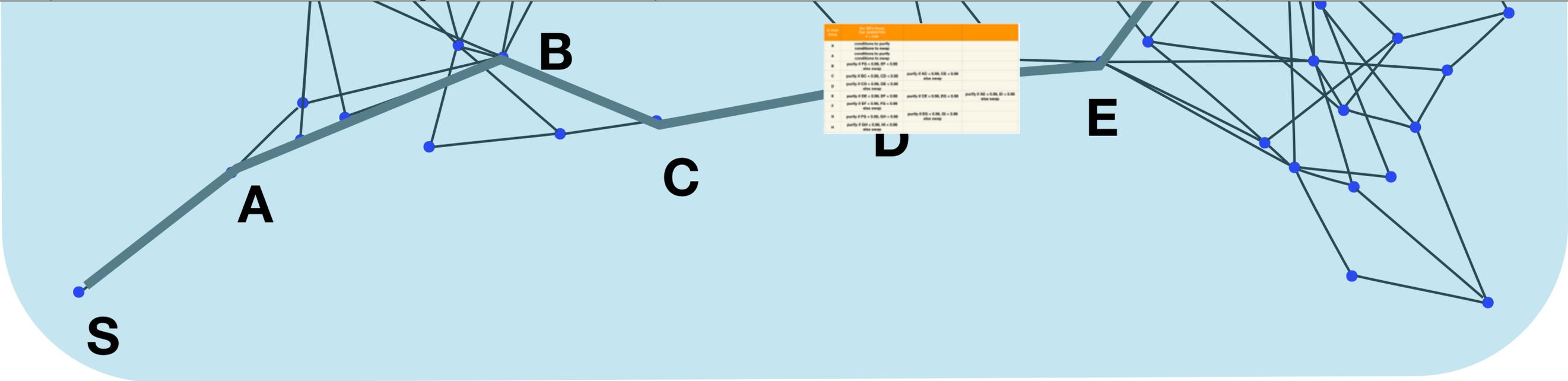
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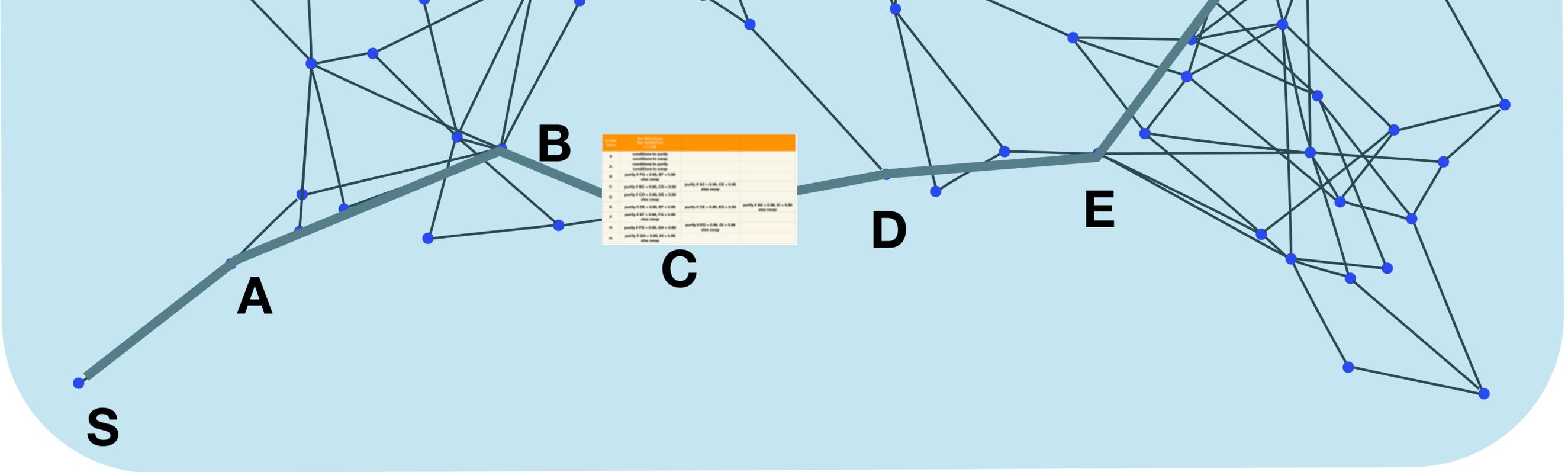
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D	purify if $CD < 0.98$, $DE < 0.98$ else swap		
E	purify if $DE < 0.98$, $EF < 0.98$	purify if $CE < 0.98$, $EG < 0.98$	purify if $AE < 0.98$, $EI < 0.98$ else swap



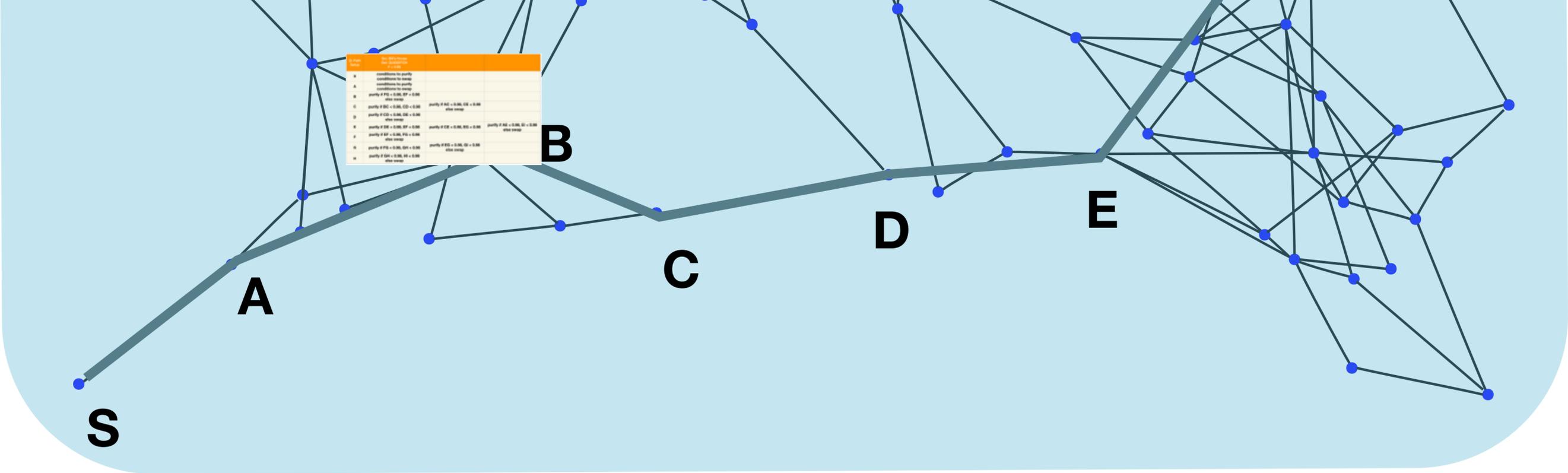
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S	conditions to purify conditions to swap		
A	conditions to purify conditions to swap		
B	purify if $FG < 0.98$, $EF < 0.98$ else swap		
C	purify if $BC < 0.98$, $CD < 0.98$	purify if $AC < 0.98$, $CE < 0.98$ else swap	



D: Path Setup	Src: Bill's House Dst: QUIDDITCH F = 0.98		
S	conditions to purify conditions to swap		
A	conditions to purify conditions to swap		
B	purify if $FG < 0.98$, $EF < 0.98$ else swap		

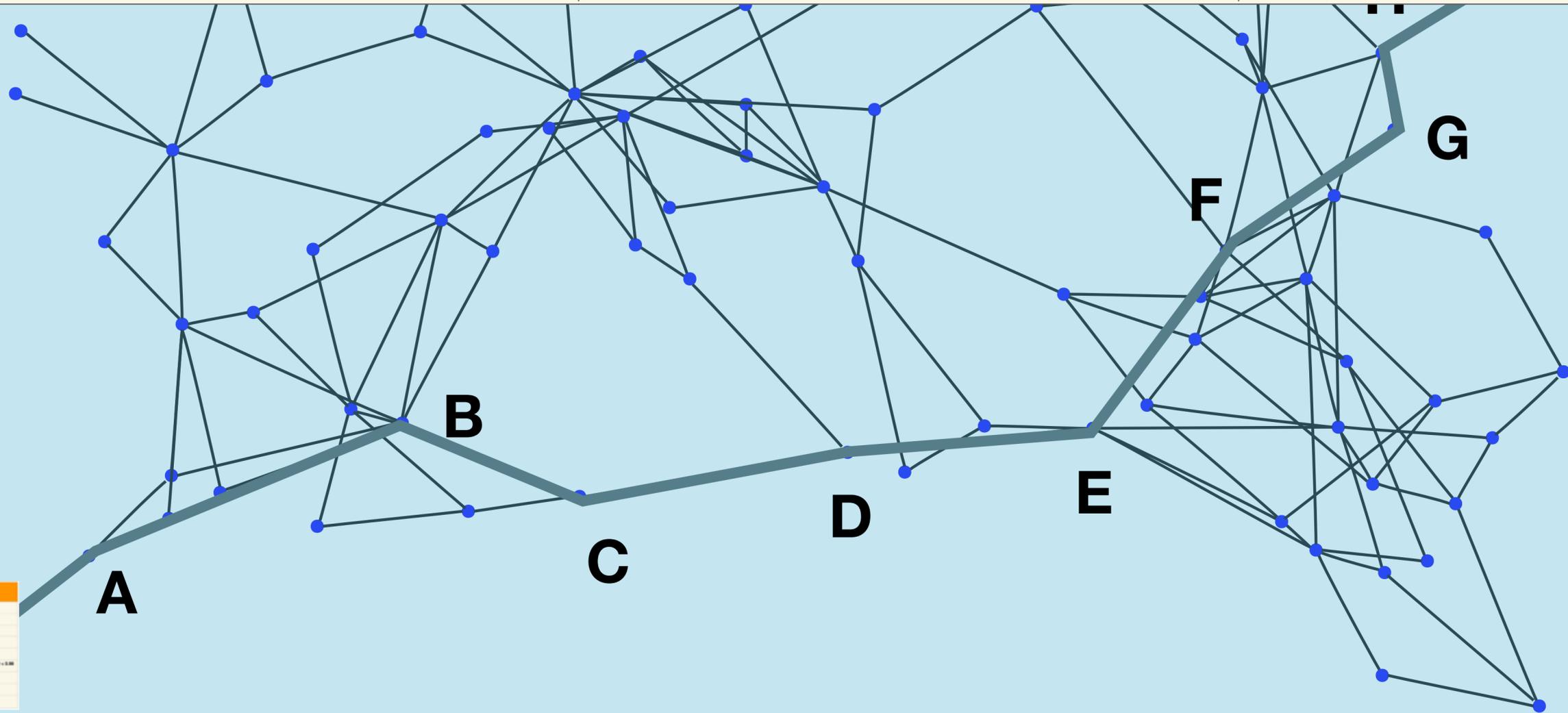


D: Path Setup

Src: Bill's House
Dst: QUIDDITCH
F = 0.98

S

conditions to purify
conditions to swap



Step	Condition	Priority
S	conditions to purify	
A	conditions to swap	
B	priority of PD = 0.98, EF = 0.98	
C	priority of BC = 0.98, CD = 0.98	
D	priority of CD = 0.98, DE = 0.98	
E	priority of DE = 0.98, EF = 0.98	
F	priority of EF = 0.98, FG = 0.98	
G	priority of FG = 0.98, GH = 0.98	
H	priority of GH = 0.98, HI = 0.98	

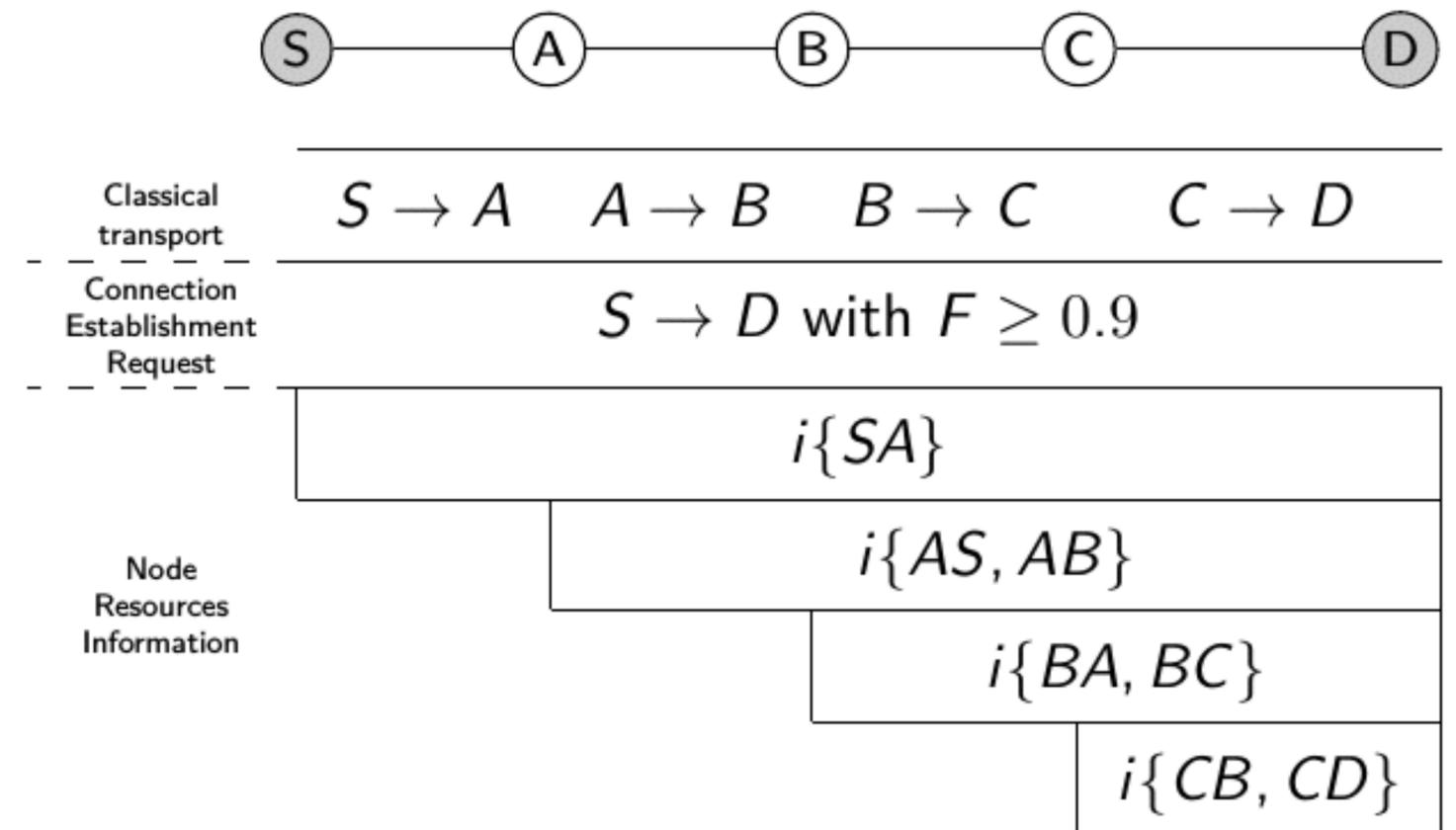
S

Connection Establishment Request

Used by D to establish rules and Bell pairs distribution.

Nodes provide information about the path:

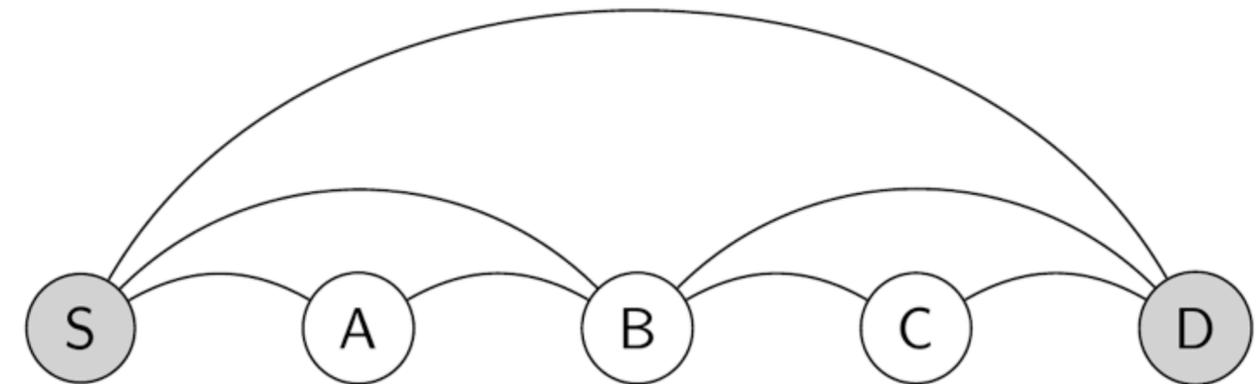
- Resources
- Quality of the link, etc.



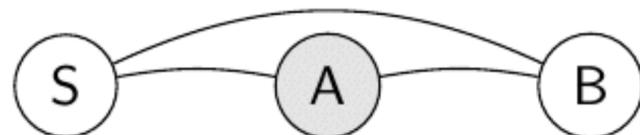
Connection Establishment (Response)

Destination node computes a swapping scheme.

Information provided by the middle nodes is important to create a consistent set of rules.



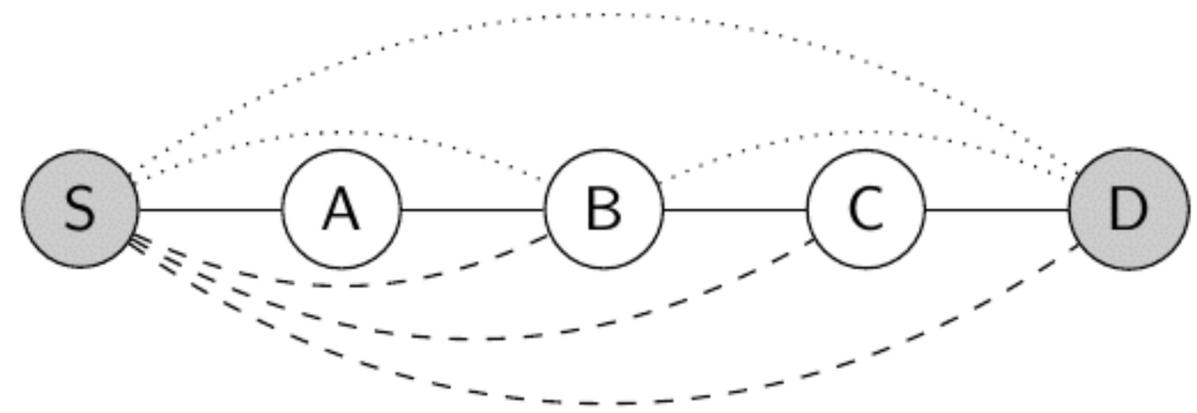
	Conditions	Actions
Pairs management	$A \sim x$ $F \leq 0.5$	Discard
	$A \sim x$ $A \sim x$ both $F \leq 0.95$	Purify
Swapping	$A \sim B$ $A \sim S$ both $F > 0.95$	Swap



Every node receives a set of rules that will be used to maintain a consistent distributed swapping protocol.

Challenges

- Decomposition choice:
swapping order hierarchical (top)
or hop-by-hop (bottom)
- Limiting classical messages
- Consistency of the behaviors of
every node
- Class of service



Comments from the ML

- Q: What about Segment Routing?
- A: Good thought. I'm not familiar w/ the current SR, but waypoint routing + circuit/reservation setup is what I have in mind.

Moreover, intended to be recursive, treating each network as a node in a larger graph (more than just two-layer IGP/EGP).