

FROST: Flexible Round-Optimized Schnorr Threshold Signatures

CFRG Update for Threshold Signature Working Group, IETF 110

Chelsea Komlo^{1,2} Ian Goldberg¹

¹ University of Waterloo

² Zcash Foundation

March 2021

FROST: Summary

- ▶ Two-round Schnorr threshold signing protocol, or single-round with preprocessing.
- ▶ FROST specifically trades off robustness for round efficiency.
- ▶ Signing operations are secure when performed concurrently, against an adversary that controls up to $t - 1$ signers.
- ▶ Key generation be performed by either a trusted dealer or via a Distributed Key Generation (DKG) Protocol

FROST: Summary

- ▶ Two-round Schnorr threshold signing protocol, or single-round with preprocessing.
- ▶ FROST specifically trades off robustness for round efficiency.
- ▶ Signing operations are secure when performed concurrently, against an adversary that controls up to $t - 1$ signers.
- ▶ Key generation be performed by either a trusted dealer or via a Distributed Key Generation (DKG) Protocol

FROST: Summary

- ▶ Two-round Schnorr threshold signing protocol, or single-round with preprocessing.
- ▶ FROST specifically trades off robustness for round efficiency.
- ▶ Signing operations are secure when performed concurrently, against an adversary that controls up to $t - 1$ signers.
- ▶ Key generation be performed by either a trusted dealer or via a Distributed Key Generation (DKG) Protocol

FROST: Summary

- ▶ Two-round Schnorr threshold signing protocol, or single-round with preprocessing.
- ▶ FROST specifically trades off robustness for round efficiency.
- ▶ Signing operations are secure when performed concurrently, against an adversary that controls up to $t - 1$ signers.
- ▶ Key generation be performed by either a trusted dealer or via a Distributed Key Generation (DKG) Protocol

Current Status

- ▶ FROST was adopted as a working group item at the end of January.
- ▶ We are working on the first draft, focusing on implementation details not specified in our paper.
- ▶ We are writing a second proof of security using standard assumptions.
- ▶ Several parallel implementations exist, but these need to converge.

Current Status

- ▶ FROST was adopted as a working group item at the end of January.
- ▶ We are working on the first draft, focusing on implementation details not specified in our paper.
- ▶ We are writing a second proof of security using standard assumptions.
- ▶ Several parallel implementations exist, but these need to converge.

Current Status

- ▶ FROST was adopted as a working group item at the end of January.
- ▶ We are working on the first draft, focusing on implementation details not specified in our paper.
- ▶ We are writing a second proof of security using standard assumptions.
- ▶ Several parallel implementations exist, but these need to converge.

Current Status

- ▶ FROST was adopted as a working group item at the end of January.
- ▶ We are working on the first draft, focusing on implementation details not specified in our paper.
- ▶ We are writing a second proof of security using standard assumptions.
- ▶ Several parallel implementations exist, but these need to converge.

Feedback from Call for Adoption (summary)

- ▶ **Compatibility with EdDSA *verification* over Ed25519/Ed448.**
 - ▶ Using EdDSA-style deterministic nonces is insecure in a multi-signer setting.
 - ▶ Our draft will specify signatures compatible with verification specified in RFC 8032.
- ▶ Preprocessing may be difficult to perform securely.
- ▶ Option for either trusted dealer or DKG.

Feedback from Call for Adoption (summary)

- ▶ Compatibility with EdDSA *verification* over Ed25519/Ed448.
 - ▶ Using EdDSA-style deterministic nonces is insecure in a multi-signer setting.
 - ▶ Our draft will specify signatures compatible with verification specified in RFC 8032.
- ▶ Preprocessing may be difficult to perform securely.
- ▶ Option for either trusted dealer or DKG.

Feedback from Call for Adoption (summary)

- ▶ Compatibility with EdDSA *verification* over Ed25519/Ed448.
 - ▶ Using EdDSA-style deterministic nonces is insecure in a multi-signer setting.
 - ▶ Our draft will specify signatures compatible with verification specified in RFC 8032.
- ▶ Preprocessing may be difficult to perform securely.
- ▶ Option for either trusted dealer or DKG.

Feedback from Call for Adoption (summary)

- ▶ Compatibility with EdDSA *verification* over Ed25519/Ed448.
 - ▶ Using EdDSA-style deterministic nonces is insecure in a multi-signer setting.
 - ▶ Our draft will specify signatures compatible with verification specified in RFC 8032.

- ▶ Preprocessing may be difficult to perform securely.

- ▶ Option for either trusted dealer or DKG.

Feedback from Call for Adoption (summary)

- ▶ Compatibility with EdDSA *verification* over Ed25519/Ed448.
 - ▶ Using EdDSA-style deterministic nonces is insecure in a multi-signer setting.
 - ▶ Our draft will specify signatures compatible with verification specified in RFC 8032.

- ▶ Preprocessing may be difficult to perform securely.

- ▶ Option for either trusted dealer or DKG.

Next Steps

- ▶ Full specification for v1.
- ▶ Interoperable implementations.
- ▶ Specify prime-order curves, then adapt to curves with cofactors, considering:
 - ▶ Point validation during signing.
 - ▶ Publishing verification-compatible signatures (RFC 8032).

Next Steps

- ▶ Full specification for v1.
- ▶ Interoperable implementations.
- ▶ Specify prime-order curves, then adapt to curves with cofactors, considering:
 - ▶ Point validation during signing.
 - ▶ Publishing verification-compatible signatures (RFC 8032).

Next Steps

- ▶ Full specification for v1.
- ▶ Interoperable implementations.
- ▶ Specify prime-order curves, then adapt to curves with cofactors, considering:
 - ▶ Point validation during signing.
 - ▶ Publishing verification-compatible signatures (RFC 8032).

Next Steps

- ▶ Full specification for v1.
- ▶ Interoperable implementations.
- ▶ Specify prime-order curves, then adapt to curves with cofactors, considering:
 - ▶ Point validation during signing.
 - ▶ Publishing verification-compatible signatures (RFC 8032).

Next Steps

- ▶ Full specification for v1.
- ▶ Interoperable implementations.
- ▶ Specify prime-order curves, then adapt to curves with cofactors, considering:
 - ▶ Point validation during signing.
 - ▶ Publishing verification-compatible signatures (RFC 8032).

Roadmap

- ▶ **Within the core draft:**

- ▶ Trusted dealer
- ▶ Two round
- ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:

- ▶ Preprocessing (single-round signing)
- ▶ DKG (possibly more generally useful)
- ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ **Within the core draft:**

- ▶ Trusted dealer
- ▶ Two round
- ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:

- ▶ Preprocessing (single-round signing)
- ▶ DKG (possibly more generally useful)
- ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ Within the core draft:
 - ▶ Trusted dealer
 - ▶ Two round
 - ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:
 - ▶ Preprocessing (single-round signing)
 - ▶ DKG (possibly more generally useful)
 - ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ Within the core draft:
 - ▶ Trusted dealer
 - ▶ Two round
 - ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:
 - ▶ Preprocessing (single-round signing)
 - ▶ DKG (possibly more generally useful)
 - ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ Within the core draft:
 - ▶ Trusted dealer
 - ▶ Two round
 - ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:
 - ▶ Preprocessing (single-round signing)
 - ▶ DKG (possibly more generally useful)
 - ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ Within the core draft:
 - ▶ Trusted dealer
 - ▶ Two round
 - ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:
 - ▶ Preprocessing (single-round signing)
 - ▶ DKG (possibly more generally useful)
 - ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ Within the core draft:
 - ▶ Trusted dealer
 - ▶ Two round
 - ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:
 - ▶ Preprocessing (single-round signing)
 - ▶ DKG (possibly more generally useful)
 - ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ Within the core draft:
 - ▶ Trusted dealer
 - ▶ Two round
 - ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:
 - ▶ Preprocessing (single-round signing)
 - ▶ DKG (possibly more generally useful)
 - ▶ Share recovery/adding new participants

Questions?

Roadmap

- ▶ Within the core draft:
 - ▶ Trusted dealer
 - ▶ Two round
 - ▶ Non-signing signature aggregator.

- ▶ Possible future extensions:
 - ▶ Preprocessing (single-round signing)
 - ▶ DKG (possibly more generally useful)
 - ▶ Share recovery/adding new participants

Questions?

Extras: Protocol Specifics

FROST Sign: Round One

Participant i

$$(d_i, e_i) \xleftarrow{\$} \mathbb{Z}_q^* \times \mathbb{Z}_q^*$$

$$(D_i, E_i) = (g^{d_i}, g^{e_i})$$

Signature Aggregator

(D_i, E_i)



FROST Sign: Round One

Participant i

$$(d_i, e_i) \xleftarrow{\$} \mathbb{Z}_q^* \times \mathbb{Z}_q^*$$

$$(D_i, E_i) = (g^{d_i}, g^{e_i})$$

Signature Aggregator

(D_i, E_i)



FROST Sign: Round One

Participant i

$$(d_i, e_i) \xleftarrow{\$} \mathbb{Z}_q^* \times \mathbb{Z}_q^*$$

$$(D_i, E_i) = (g^{d_i}, g^{e_i})$$

Signature Aggregator

(D_i, E_i)



FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)



$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

z_i



Publish $\sigma = (R, z = \sum z_i)$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)



$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

z_i



$$\text{Publish } \sigma = (R, z = \sum z_i)$$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)

$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell^{(E_\ell) \rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

“binding value” to
bind signing shares
to ℓ , m , and B

$$\text{sig} = (R, z = \sum z_i)$$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)



$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

z_i



Publish $\sigma = (R, z = \sum z_i)$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)



$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

z_i



Publish $\sigma = (R, z = \sum z_i)$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)



$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

z_i



Publish $\sigma = (R, z = \sum z_i)$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)

$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

This step cannot be inverted by anyone who does not know (d_i, e_i) .

z_i

Publish $\sigma = (R, z = \sum z_i)$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)



$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

z_i



Publish $\sigma = (R, z = \sum z_i)$

FROST Sign: Round Two

Signer i

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)



$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

z_i



Publish $\sigma = (R, z = \sum z_i)$

FROST Sign: Round Two

Signer i

$$\rho_\ell = H_1(\ell, m, B), \ell \in S$$

$$R = \prod_{\ell \in S} D_\ell \cdot (E_\ell)^{\rho_\ell}$$

$$c = H_2(R, Y, m)$$

$$z_i = d_i + (e_i \cdot \rho_i) + \lambda_i \cdot s_i \cdot c$$

Signature Aggregator

$$B = ((1, D_1, E_1), \dots, (t, D_t, E_t))$$

(m, B)

Signature format
and verification
are identical to
single-party Schnorr.

z_i

Publish $\sigma = (R, z = \sum z_i)$