

Verification-Friendly ECDSA

(and use with JOSE/COSE)

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Outline

1. ECC Signature Schemes:
 - ECDSA Signing and Verification
 - Speed-ups with ECDSA*
2. Putting ECDSA and ECDSA* into same format
 - JWS Example
 - General Approach for Reusing ECDSA Standard
3. Transitioning Considerations
4. Conclusions, next steps

ECDSA Algorithm

ECDSA:

Signature: $\underline{r} || \underline{s}$ in most-significant-bit/octet first order
Signing equation: $e = s \cdot k - d \cdot r \pmod{n}$, where $e = \text{Hash}(m)$, $R = kG$, $R \rightarrow r$
Verification: Compute $R' = (e/s)G + (r/s)Q$, where $Q = dG$;
check that $R' \rightarrow r$

Example: ECDSA, w/ P-256 and SHA-256 (FIPS 186-4, ANSI X9.62, etc.)

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ECDSA and ECDSA* have **same** security, but **different** formats

ECDSA* allows faster verification

speed-ups: ~1.3x make scalars small, which halves ECC doubles (single verify)
 up to ~6x amortize ECC doubles and common terms (batch verify)

(This uses alternative verification equation: $\lambda (-R + (e/s)G + (r/s)Q) = O$ for any $\lambda \neq 0$)

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ECDSA and ECDSA* have **same** security, but ~~different~~ **same** formats (with a trick)
(our examples assume prime-order curves)

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JWS Example

(RFC 7515, Appendix A.3)

JWS Protected Header:

```
{"alg": "ES256" }
```

JWS Payload:

```
{"iss": "joe",  
"exp": 1300819380,  
"http://example.com/is_root": true}
```

JWK Key:

```
{"kty": "EC",  
"crv": "P-256",  
"x": "f830J3D2xF1Bg8vub9tLe1gHMzV76e8Tus9uPHvRVEU",  
"y": "x_FEzRu9m36HLN_tue659LNpXW6pCyStikYjKIWI5a0" }
```

ECDSA signature ($r, \pm s$):

```
r: 0x0ed12153 79636c48 3c2f7f15 5807d402 a3b22803 3af97c7e 17819ac3 169ea665  
+s: 0xc50a07d3 8c3c70e5 d8f12daf 084a5480 a66590c5 f293509a 8f3f7f8a 83a354d5  
-s: 0x3af5f82b 73c38f1b 270ed250 f7b5ab7f 168169e7 b4844dea 647a4b38 78bfd07c
```

Option #1: with ECDSA signature ($r, +s$)

```
eyJhbGciOiJIJFUiI1NiJ9.
```

```
eyJpc3MiOiJqb2UiLA0KICJleHAiOiJlZMDA4MTkzODAsDQogImh0dHA6Ly9leGFtcGxlLmNvbS9pc19yb290Ijp0cnVlfQ.  
DtEhU31jbEg8L38VWAFUAqOyKAM6-Xx-F4GawxaepmXFCgfTjDxw5djxLa8ISlSAPmWQxfKTUJqPP3-Kg6NU1Q
```

Option #2: with ECDSA signature ($r, -s$)

```
eyJhbGciOiJIJFUiI1NiJ9.
```

```
eyJpc3MiOiJqb2UiLA0KICJleHAiOiJlZMDA4MTkzODAsDQogImh0dHA6Ly9leGFtcGxlLmNvbS9pc19yb290Ijp0cnVlfQ.  
DtEhU31jbEg8L38VWAFUAqOyKAM6-Xx-F4GawxaepmU69fgrc8OPGyc001D3tat_FoFp57SETepkeks4eL_QfA
```



with ECDSA ($r, +s$)...



with ECDSA ($r, -s$)...

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with ECDSA ($r, +s$)...



with ECDSA ($r, -s$)...

Option #1: with ECDSA signature ($r, +s$)

eyJhbGciOiJIJFUiI1NiJ9.

$R := (xR, yR)$, with yR odd



eyJpc3MiOiJqb2UiLA0KICJleHAiOjEzMDA4MTkzODAsDQogImh0dHA6Ly9leGFtcGxlLmNvbS9pc19yb290Ijp0cnVlfQ.
DtEhU31jbEg8L38VWAFUAqOyKAM6-Xx-F4GawxaepmXFCgfTjDxw5djxLa8ISlSAPmWQxfKTUJqPP3-Kg6NU1Q

Option #2: with ECDSA signature ($r, -s$)

eyJhbGciOiJIJFUiI1NiJ9.

$R := (xR, yR)$, with yR even



eyJpc3MiOiJqb2UiLA0KICJleHAiOjEzMDA4MTkzODAsDQogImh0dHA6Ly9leGFtcGxlLmNvbS9pc19yb290Ijp0cnVlfQ.
DtEhU31jbEg8L38VWAFUAqOyKAM6-Xx-F4GawxaepmU69fgrc8OPGyc001D3tat_FoFp57SETepkeks4eL_QfA

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```



with ECDSA ($r, -s$)...

Rule: Choose ECDSA option ($r, \pm s$) such that $R := (xR, yR)$ with yR even

Option #2: with ECDSA signature ($r, -s$)

eyJhbGciOiJFbGUzIiwiaWF0IjoiMTU5MjU0MjU0In0.

eyJpc3MiOiJqb2UiLA0KICJleHAiOiJ0IjEzMDA4MTkzODAsDQogImh0dHA6Ly9leGFtcGxlIjoiImNvbnVlfnQyLnQzIiwiaWF0IjoiMTU5MjU0MjU0In0.

$R := (xR, yR)$, with yR even, so $r \rightarrow R$ unique ($r = xR$ in practice)

DtEhU31jbEg8L38VWafUAqOyKAM6-Xx-F4GawxaepmU69fg8OPGyc001D3tat_FoFp57SETepkeks4eL_QfA

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ECDSA and ECDSA* have same security, but ~~different~~ same formats (with a trick)

ECDSA via modified ECDSA signing procedure*

- Step 1: Generate ECDSA signature (r, s) of message m , as usual;
- Step 2: Change (r, s) to $(r, -s)$ if ephemeral key R has y-coordinate with odd parity

ECDSA and ECDSA* have same format, since $R \rightarrow r$ map reversible ($r \rightarrow \pm R$ unique in practice)

Implementation of ECDSA*

ECDSA via modified ECDSA signing procedure*

- Step 1: Generate ECDSA signature (r, s) of message m , as usual;
- Step 2: Change (r, s) to $(r, -s)$ if ephemeral key R has y -coordinate with odd parity

Notes:

- If (r, s) is a valid ECDSA signature, then so is $(r, -s)$ — the so-called malleability
This modified ECDSA signature is still an ECDSA signature, so no security impact
- Any party can perform Step 2, since for valid signatures $R := (e/s)G + (r/s)Q$
This party does not have to be the signer and this can be done retroactively

Impact on ECDSA verifiers:

- If verifier knows that modified signing procedure was used, $R' \rightarrow r$ has unique preimage in practice for all prime-order curves (implicit point compression R) and speed-ups always work
- If verifier does not know that modified signing procedure was used, it can still verify ECDSA signatures as usual (but will not get single-verify and batch verification speed-ups)
- If verifier wishes to use ordinary ECDSA signature verification for whatever reason, it can do so

Transitioning towards ECDSA*

Applications with IETF protocols:

Everywhere, e.g., PKIX, CMS, Certificate Transparency, OpenPGP, COSE, JOSE, lake, etc.

JOSE:

- Define new "alg" field named "ES256vf" (ES256 with modified signing)
- Verifier who does not want to use speed-ups interprets this as "ES256"
This is possible since ECDSA signatures are also ECDSA signatures*
- Signer can use modified ECDSA signing procedure
Use of new label does not allow retroactively putting "ES256"-based JWS signatures into ECDSA format, since the new label is part of the "to-be-signed data"*
Note: this would be possible, if one would replace "ES256vf" by "ES256" before signing and verification, but this likely would create JWS processing anomalies

Alternatives:

- Put all existing ECDSA signatures retroactively into ECDSA* format ("Big Bang");
- Mandate in specific protocols.

Question is whether this would entice implementors enough to switch to always-on ECDSA*.

This also comes down to side-information re whether the modified signing procedure was followed that is not part of the JWS string (something JSON parsers may not be able to handle)

Conclusions & Question to Group

Summary:

- ECDSA verification can take advantage of ECDSA* speed-ups, similarly to EdDSA, both in single-verify and batch-verify cases
- Techniques useful in *all* settings, where use of the modified ECDSA signing procedure can be signalled
- Techniques known since 2005 (single-verify), 1995 (batch-verify), published in well-respected, peer-reviewed crypto conferences. {Also used in Bitcoin signing}

Why now, why here?

- techniques known for long; standardization incentive for implementation needed
- e-health initiatives (e.g., SmartHealth, IATA Pass (jws); EU digital covid certs (cose))

Question to Group:

- Does group support this work, once crypto review gating hurdle taken?
- How can we make this quick project, so that it can have real-life impact? (e.g., already reserving code points, so that this does not become a dead horse)
- Any volunteers for implementation, getting this done asap, etc.?
- Any pointers to iana templates, other than Section 9 of RFC 7515?